

## OBJECTIVE TYPE QUESTIONS

Choose the correct or most suitable answer :

- (1) The rank of the matrix  $\begin{bmatrix} 1 & -1 & 2 \\ 2 & -2 & 4 \\ 4 & -4 & 8 \end{bmatrix}$  is  
 (1) 1 (2) 2 (3) 3 (4) 4
- (2) The rank of the diagonal matrix  $\begin{bmatrix} -1 & & & \\ & 2 & & \\ & & 0 & \\ & & & -4 \\ & & & & 0 \end{bmatrix}$   
 (1) 0 (2) 2 (3) 3 (4) 5
- (3) If  $A = [2 \ 0 \ 1]$ , then rank of  $AA^T$  is  
 (1) 1 (2) 2 (3) 3 (4) 0
- (4) If  $A = \begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}$ , then the rank of  $AA^T$  is  
 (1) 3 (2) 0 (3) 1 (4) 2
- (5) If the rank of the matrix  $\begin{bmatrix} \lambda & -1 & 0 \\ 0 & \lambda & -1 \\ -1 & 0 & \lambda \end{bmatrix}$  is 2, then  $\lambda$  is  
 (1) 1 (2) 2 (3) 3 (4) any real number
- (6) If  $A$  is a scalar matrix with scalar  $k \neq 0$ , of order 3, then  $A^{-1}$  is  
 (1)  $\frac{1}{k^2}I$  (2)  $\frac{1}{k^3}I$  (3)  $\frac{1}{k}I$  (4)  $kI$
- (7) If the matrix  $\begin{bmatrix} -1 & 3 & 2 \\ 1 & k & -3 \\ 1 & 4 & 5 \end{bmatrix}$  has an inverse then the values of  $k$   
 (1)  $k$  is any real number (2)  $k = -4$  (3)  $k \neq -4$  (4)  $k \neq 4$
- (8) If  $A = \begin{bmatrix} 2 & 1 \\ 3 & 4 \end{bmatrix}$ , then  $(\text{adj } A)A =$   
 (1)  $\begin{bmatrix} \frac{1}{5} & 0 \\ 0 & \frac{1}{5} \end{bmatrix}$  (2)  $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$  (3)  $\begin{bmatrix} 5 & 0 \\ 0 & -5 \end{bmatrix}$  (4)  $\begin{bmatrix} 5 & 0 \\ 0 & 5 \end{bmatrix}$

- (9) If  $A$  is a square matrix of order  $n$  then  $|\text{adj } A|$  is  
 (1)  $|A|^2$  (2)  $|A|^n$  (3)  $|A|^{n-1}$  (4)  $|A|$
- (10) The inverse of the matrix  $\begin{bmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{bmatrix}$  is  
 (1)  $\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$  (2)  $\begin{bmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ -1 & 0 & 0 \end{bmatrix}$  (3)  $\begin{bmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{bmatrix}$  (4)  $\begin{bmatrix} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$
- (11) If  $A$  is a matrix of order 3, then  $\det(kA)$   
 (1)  $k^3 \det(A)$  (2)  $k^2 \det(A)$  (3)  $k \det(A)$  (4)  $\det(A)$
- (12) If  $I$  is the unit matrix of order  $n$ , where  $k \neq 0$  is a constant, then  $\text{adj}(kI) =$   
 (1)  $k^n (\text{adj } I)$  (2)  $k (\text{adj } I)$  (3)  $k^2 (\text{adj } I)$  (4)  $k^{n-1} (\text{adj } I)$
- (13) If  $A$  and  $B$  are any two matrices such that  $AB = O$  and  $A$  is non-singular, then  
 (1)  $B = O$  (2)  $B$  is singular (3)  $B$  is non-singular (4)  $B = A$
- (14) If  $A = \begin{bmatrix} 0 & 0 \\ 0 & 5 \end{bmatrix}$ , then  $A^{12}$  is  
 (1)  $\begin{bmatrix} 0 & 0 \\ 0 & 60 \end{bmatrix}$  (2)  $\begin{bmatrix} 0 & 0 \\ 0 & 5^{12} \end{bmatrix}$  (3)  $\begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$  (4)  $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$
- (15) Inverse of  $\begin{bmatrix} 3 & 1 \\ 5 & 2 \end{bmatrix}$  is  
 (1)  $\begin{bmatrix} 2 & -1 \\ -5 & 3 \end{bmatrix}$  (2)  $\begin{bmatrix} -2 & 5 \\ 1 & -3 \end{bmatrix}$  (3)  $\begin{bmatrix} 3 & -1 \\ -5 & -3 \end{bmatrix}$  (4)  $\begin{bmatrix} -3 & 5 \\ 1 & -2 \end{bmatrix}$
- (16) In a system of 3 linear non-homogeneous equation with three unknowns, if  $\Delta = 0$  and  $\Delta_x = 0$ ,  $\Delta_y \neq 0$  and  $\Delta_z = 0$  then the system has  
 (1) unique solution (2) two solutions  
 (3) infinitely many solutions (4) no solutions
- (17) The system of equations  $ax + y + z = 0$  ;  $x + by + z = 0$  ;  $x + y + cz = 0$  has a non-trivial solution then  $\frac{1}{1-a} + \frac{1}{1-b} + \frac{1}{1-c} =$   
 (1) 1 (2) 2 (3) -1 (4) 0

(18) If  $ae^x + be^y = c$  ;  $pe^x + qe^y = d$  and  $\Delta_1 = \begin{vmatrix} a & b \\ p & q \end{vmatrix}$  ;  $\Delta_2 = \begin{vmatrix} c & b \\ d & q \end{vmatrix}$  ,

$\Delta_3 = \begin{vmatrix} a & c \\ p & d \end{vmatrix}$  then the value of  $(x, y)$  is

(1)  $\left(\frac{\Delta_2}{\Delta_1}, \frac{\Delta_3}{\Delta_1}\right)$  (2)  $\left(\log \frac{\Delta_2}{\Delta_1}, \log \frac{\Delta_3}{\Delta_1}\right)$

(3)  $\left(\log \frac{\Delta_1}{\Delta_3}, \log \frac{\Delta_1}{\Delta_2}\right)$  (4)  $\left(\log \frac{\Delta_1}{\Delta_2}, \log \frac{\Delta_1}{\Delta_3}\right)$

(19) If the equation  $-2x + y + z = l$   
 $x - 2y + z = m$   
 $x + y - 2z = n$

such that  $l + m + n = 0$ , then the system has

(1) a non-zero unique solution (2) trivial solution

(3) Infinitely many solution (4) No Solution

(20) If  $\vec{a}$  is a non-zero vector and  $m$  is a non-zero scalar then  $m\vec{a}$  is a unit vector if

(1)  $m = \pm 1$  (2)  $a = |m|$  (3)  $a = \frac{1}{|m|}$  (4)  $a = 1$

(21) If  $\vec{a}$  and  $\vec{b}$  are two unit vectors and  $\theta$  is the angle between them, then

$\left(\frac{\vec{a} + \vec{b}}{2}\right)$  is a unit vector if

(1)  $\theta = \frac{\pi}{3}$  (2)  $\theta = \frac{\pi}{4}$  (3)  $\theta = \frac{\pi}{2}$  (4)  $\theta = \frac{2\pi}{3}$

(22) If  $\vec{a}$  and  $\vec{b}$  include an angle  $120^\circ$  and their magnitude are 2 and  $\sqrt{3}$  then  $\vec{a} \cdot \vec{b}$  is equal to

(1)  $\sqrt{3}$  (2)  $-\sqrt{3}$  (3) 2 (4)  $-\frac{\sqrt{3}}{2}$

(23) If  $\vec{u} = \vec{a} \times (\vec{b} \times \vec{c}) + \vec{b} \times (\vec{c} \times \vec{a}) + \vec{c} \times (\vec{a} \times \vec{b})$ , then

(1)  $u$  is a unit vector (2)  $\vec{u} = \vec{a} + \vec{b} + \vec{c}$

(3)  $\vec{u} = \vec{0}$  (4)  $\vec{u} \neq \vec{0}$

(24) If  $\vec{a} + \vec{b} + \vec{c} = 0$ ,  $|\vec{a}| = 3$ ,  $|\vec{b}| = 4$ ,  $|\vec{c}| = 5$  then the angle between  $\vec{a}$  and  $\vec{b}$  is

- (1)  $\frac{\pi}{6}$                       (2)  $\frac{2\pi}{3}$                       (3)  $\frac{5\pi}{3}$                       (4)  $\frac{\pi}{2}$

(25) The vectors  $2\vec{i} + 3\vec{j} + 4\vec{k}$  and  $a\vec{i} + b\vec{j} + c\vec{k}$  are perpendicular when

- (1)  $a = 2$ ,  $b = 3$ ,  $c = -4$                       (2)  $a = 4$ ,  $b = 4$ ,  $c = 5$   
 (3)  $a = 4$ ,  $b = 4$ ,  $c = -5$                       (4)  $a = -2$ ,  $b = 3$ ,  $c = 4$

(26) The area of the parallelogram having a diagonal  $3\vec{i} + \vec{j} - \vec{k}$  and a side  $\vec{i} - 3\vec{j} + 4\vec{k}$  is

- (1)  $10\sqrt{3}$                       (2)  $6\sqrt{30}$                       (3)  $\frac{3}{2}\sqrt{30}$                       (4)  $3\sqrt{30}$

(27) If  $|\vec{a} + \vec{b}| = |\vec{a} - \vec{b}|$  then

- (1)  $\vec{a}$  is parallel to  $\vec{b}$   
 (2)  $\vec{a}$  is perpendicular to  $\vec{b}$   
 (3)  $|\vec{a}| = |\vec{b}|$   
 (4)  $\vec{a}$  and  $\vec{b}$  are unit vectors

(28) If  $\vec{p}$ ,  $\vec{q}$  and  $\vec{p} + \vec{q}$  are vectors of magnitude  $\lambda$  then the magnitude of  $|\vec{p} - \vec{q}|$  is

- (1)  $2\lambda$                       (2)  $\sqrt{3}\lambda$                       (3)  $\sqrt{2}\lambda$                       (4)  $1$

(29) If  $\vec{a} \times (\vec{b} \times \vec{c}) + \vec{b} \times (\vec{c} \times \vec{a}) + \vec{c} \times (\vec{a} \times \vec{b}) = \vec{x} \times \vec{y}$  then

- (1)  $\vec{x} = \vec{0}$                       (2)  $\vec{y} = \vec{0}$   
 (3)  $\vec{x}$  and  $\vec{y}$  are parallel (4)  $\vec{x} = \vec{0}$  or  $\vec{y} = \vec{0}$  or  $\vec{x}$  and  $\vec{y}$  are parallel

(30) If  $\vec{PR} = 2\vec{i} + \vec{j} + \vec{k}$ ,  $\vec{QS} = -\vec{i} + 3\vec{j} + 2\vec{k}$  then the area of the quadrilateral PQRS is

- (1)  $5\sqrt{3}$                       (2)  $10\sqrt{3}$                       (3)  $\frac{5\sqrt{3}}{2}$                       (4)  $\frac{3}{2}$



- (31) The projection of  $\vec{OP}$  on a unit vector  $\vec{OQ}$  equals thrice the area of parallelogram  $OPRQ$ . Then  $\angle POQ$  is
- (1)  $\tan^{-1} \frac{1}{3}$       (2)  $\cos^{-1} \left( \frac{3}{10} \right)$       (3)  $\sin^{-1} \left( \frac{3}{\sqrt{10}} \right)$       (4)  $\sin^{-1} \left( \frac{1}{3} \right)$
- (32) If the projection of  $\vec{a}$  on  $\vec{b}$  and projection of  $\vec{b}$  on  $\vec{a}$  are equal then the angle between  $\vec{a} + \vec{b}$  and  $\vec{a} - \vec{b}$  is
- (1)  $\frac{\pi}{2}$       (2)  $\frac{\pi}{3}$       (3)  $\frac{\pi}{4}$       (4)  $\frac{2\pi}{3}$
- (33) If  $\vec{a} \times (\vec{b} \times \vec{c}) = (\vec{a} \times \vec{b}) \times \vec{c}$  for non-coplanar vectors  $\vec{a}, \vec{b}, \vec{c}$  then
- (1)  $\vec{a}$  parallel to  $\vec{b}$       (2)  $\vec{b}$  parallel to  $\vec{c}$   
 (3)  $\vec{c}$  parallel to  $\vec{a}$       (4)  $\vec{a} + \vec{b} + \vec{c} = \vec{0}$
- (34) If a line makes  $45^\circ, 60^\circ$  with positive direction of axes  $x$  and  $y$  then the angle it makes with the  $z$  axis is
- (1)  $30^\circ$       (2)  $90^\circ$       (3)  $45^\circ$       (4)  $60^\circ$
- (35) If  $[\vec{a} \times \vec{b}, \vec{b} \times \vec{c}, \vec{c} \times \vec{a}] = 64$  then  $[\vec{a}, \vec{b}, \vec{c}]$  is
- (1) 32      (2) 8      (3) 128      (4) 0
- (36) If  $[\vec{a} + \vec{b}, \vec{b} + \vec{c}, \vec{c} + \vec{a}] = 8$  then  $[\vec{a}, \vec{b}, \vec{c}]$  is
- (1) 4      (2) 16      (3) 32      (4) -4
- (37) The value of  $[\vec{i} + \vec{j}, \vec{j} + \vec{k}, \vec{k} + \vec{i}]$  is equal to
- (1) 0      (2) 1      (3) 2      (4) 4
- (38) The shortest distance of the point  $(2, 10, 1)$  from the plane  $\vec{r} \cdot (3\vec{i} - \vec{j} + 4\vec{k}) = 2\sqrt{26}$  is
- (1)  $2\sqrt{26}$       (2)  $\sqrt{26}$       (3) 2      (4)  $\frac{1}{\sqrt{26}}$

- (39) The vector  $(\vec{a} \times \vec{b}) \times (\vec{c} \times \vec{d})$  is
- (1) perpendicular to  $\vec{a}, \vec{b}, \vec{c}$  and  $\vec{d}$
  - (2) parallel to the vectors  $(\vec{a} \times \vec{b})$  and  $(\vec{c} \times \vec{d})$
  - (3) parallel to the line of intersection of the plane containing  $\vec{a}$  and  $\vec{b}$  and the plane containing  $\vec{c}$  and  $\vec{d}$
  - (4) perpendicular to the line of intersection of the plane containing  $\vec{a}$  and  $\vec{b}$  and the plane containing  $\vec{c}$  and  $\vec{d}$
- (40) If  $\vec{a}, \vec{b}, \vec{c}$  are a right handed triad of mutually perpendicular vectors of magnitude  $a, b, c$  then the value of  $[\vec{a} \ \vec{b} \ \vec{c}]$  is
- (1)  $a^2 b^2 c^2$
  - (2) 0
  - (3)  $\frac{1}{2} abc$
  - (4)  $abc$
- (41) If  $\vec{a}, \vec{b}, \vec{c}$  are non-coplanar and  $[\vec{a} \times \vec{b}, \vec{b} \times \vec{c}, \vec{c} \times \vec{a}] = [\vec{a} + \vec{b}, \vec{b} + \vec{c}, \vec{c} + \vec{a}]$  then  $[\vec{a}, \vec{b}, \vec{c}]$  is
- (1) 2
  - (2) 3
  - (3) 1
  - (4) 0
- (42)  $\vec{r} = s\vec{i} + t\vec{j}$  is the equation of
- (1) a straight line joining the points  $\vec{i}$  and  $\vec{j}$
  - (2)  $xoy$  plane
  - (3)  $yoz$  plane
  - (4)  $zox$  plane
- (43) If the magnitude of moment about the point  $\vec{j} + \vec{k}$  of a force  $\vec{i} + a\vec{j} - \vec{k}$  acting through the point  $\vec{i} + \vec{j}$  is  $\sqrt{8}$  then the value of  $a$  is
- (1) 1
  - (2) 2
  - (3) 3
  - (4) 4

(44) The equation of the line parallel to  $\frac{x-3}{1} = \frac{y+3}{5} = \frac{2z-5}{3}$  and passing through the point (1, 3, 5) in vector form is

(1)  $\vec{r} = (\vec{i} + 5\vec{j} + 3\vec{k}) + t(\vec{i} + 3\vec{j} + 5\vec{k})$

(2)  $\vec{r} = \vec{i} + 3\vec{j} + 5\vec{k} + t(\vec{i} + 5\vec{j} + 3\vec{k})$

(3)  $\vec{r} = (\vec{i} + 5\vec{j} + \frac{3}{2}\vec{k}) + t(\vec{i} + 3\vec{j} + 5\vec{k})$

(4)  $\vec{r} = \vec{i} + 3\vec{j} + 5\vec{k} + t(\vec{i} + 5\vec{j} + \frac{3}{2}\vec{k})$

(45) The point of intersection of the line  $\vec{r} = (\vec{i} - \vec{k}) + t(3\vec{i} + 2\vec{j} + 7\vec{k})$  and the plane  $\vec{r} \cdot (\vec{i} + \vec{j} - \vec{k}) = 8$  is

(1) (8, 6, 22) (2) (-8, -6, -22) (3) (4, 3, 11) (4) (-4, -3, -11)

(46) The equation of the plane passing through the point (2, 1, -1) and the line of intersection of the planes  $\vec{r} \cdot (\vec{i} + 3\vec{j} - \vec{k}) = 0$  and  $\vec{r} \cdot (\vec{j} + 2\vec{k}) = 0$  is

(1)  $x + 4y - z = 0$

(2)  $x + 9y + 11z = 0$

(3)  $2x + y - z + 5 = 0$

(4)  $2x - y + z = 0$

(47) The work done by the force  $\vec{F} = \vec{i} + \vec{j} + \vec{k}$  acting on a particle, if the particle is displaced from A(3, 3, 3) to the point B(4, 4, 4) is

(1) 2 units

(2) 3 units

(3) 4 units

(4) 7 units

(48) If  $\vec{a} = \vec{i} - 2\vec{j} + 3\vec{k}$  and  $\vec{b} = 3\vec{i} + \vec{j} + 2\vec{k}$  then a unit vector perpendicular to  $\vec{a}$  and  $\vec{b}$  is

(1)  $\frac{\vec{i} + \vec{j} + \vec{k}}{\sqrt{3}}$

(2)  $\frac{\vec{i} - \vec{j} + \vec{k}}{\sqrt{3}}$

(3)  $\frac{-\vec{i} + \vec{j} + 2\vec{k}}{\sqrt{3}}$

(4)  $\frac{\vec{i} - \vec{j} - \vec{k}}{\sqrt{3}}$

(49) The point of intersection of the lines  $\frac{x-6}{-6} = \frac{y+4}{4} = \frac{z-4}{-8}$  and

$\frac{x+1}{2} = \frac{y+2}{4} = \frac{z+3}{-2}$  is

(1) (0, 0, -4)

(2) (1, 0, 0)

(3) (0, 2, 0)

(4) (1, 2, 0)

- (50) The point of intersection of the lines

$$\vec{r} = (-\vec{i} + 2\vec{j} + 3\vec{k}) + t(-2\vec{i} + \vec{j} + \vec{k}) \text{ and}$$

$$\vec{r} = (2\vec{i} + 3\vec{j} + 5\vec{k}) + s(\vec{i} + 2\vec{j} + 3\vec{k}) \text{ is}$$

- (1) (2, 1, 1) (2) (1, 2, 1) (3) (1, 1, 2) (4) (1, 1, 1)

- (51) The shortest distance between the lines
- $\frac{x-1}{2} = \frac{y-2}{3} = \frac{z-3}{4}$
- and

$$\frac{x-2}{3} = \frac{y-4}{4} = \frac{z-5}{5} \text{ is}$$

- (1)
- $\frac{2}{\sqrt{3}}$
- (2)
- $\frac{1}{\sqrt{6}}$
- (3)
- $\frac{2}{3}$
- (4)
- $\frac{1}{2\sqrt{6}}$

- (52) The shortest distance between the parallel lines

$$\frac{x-3}{4} = \frac{y-1}{2} = \frac{z-5}{-3} \text{ and } \frac{x-1}{4} = \frac{y-2}{2} = \frac{z-3}{3} \text{ is}$$

- (1) 3 (2) 2 (3) 1 (4) 0

- (53) The following two lines are
- $\frac{x-1}{2} = \frac{y-1}{-1} = \frac{z}{1}$
- and
- $\frac{x-2}{3} = \frac{y-1}{-5} = \frac{z-1}{2}$

- (1) parallel (2) intersecting (3) skew (4) perpendicular

- (54) The centre and radius of the sphere given by

$$x^2 + y^2 + z^2 - 6x + 8y - 10z + 1 = 0 \text{ is}$$

- (1) (-3, 4, -5), 49 (2) (-6, 8, -10), 1
- 
- (3) (3, -4, 5), 7 (4) (6, -8, 10), 7

- (55) The value of
- $\left[\frac{-1+i\sqrt{3}}{2}\right]^{100} + \left[\frac{-1-i\sqrt{3}}{2}\right]^{100}$
- is

- (1) 2 (2) 0 (3) -1 (4) 1

- (56) The modulus and amplitude of the complex number
- $[e^{3-i\pi/4}]^3$
- are respectively

- (1)
- $e^9, \frac{\pi}{2}$
- (2)
- $e^9, \frac{-\pi}{2}$
- (3)
- $e^6, \frac{-3\pi}{4}$
- (4)
- $e^9, \frac{-3\pi}{4}$

- (57) If
- $(m-5) + i(n+4)$
- is the complex conjugate of
- $(2m+3) + i(3n-2)$
- then
- $(n, m)$
- are

- (1)
- $(-\frac{1}{2}, -8)$
- (2)
- $(-\frac{1}{2}, 8)$
- (3)
- $(\frac{1}{2}, -8)$
- (4)
- $(\frac{1}{2}, 8)$

- (58) If  $x^2 + y^2 = 1$  then the value of  $\frac{1+x+iy}{1+x-iy}$  is  
 (1)  $x - iy$  (2)  $2x$  (3)  $-2iy$  (4)  $x + iy$
- (59) The modulus of the complex number  $2 + i\sqrt{3}$  is  
 (1)  $\sqrt{3}$  (2)  $\sqrt{13}$  (3)  $\sqrt{7}$  (4)  $7$
- (60) If  $A + iB = (a_1 + ib_1)(a_2 + ib_2)(a_3 + ib_3)$  then  $A^2 + B^2$  is  
 (1)  $a_1^2 + b_1^2 + a_2^2 + b_2^2 + a_3^2 + b_3^2$   
 (2)  $(a_1 + a_2 + a_3)^2 + (b_1 + b_2 + b_3)^2$   
 (3)  $(a_1^2 + b_1^2)(a_2^2 + b_2^2)(a_3^2 + b_3^2)$   
 (4)  $(a_1^2 + a_2^2 + a_3^2)(b_1^2 + b_2^2 + b_3^2)$
- (61) If  $a = 3 + i$  and  $z = 2 - 3i$  then the points on the Argand diagram representing  $az$ ,  $3az$  and  $-az$  are  
 (1) Vertices of a right angled triangle  
 (2) Vertices of an equilateral triangle  
 (3) Vertices of an isosceles triangle  
 (4) Collinear
- (62) The points  $z_1, z_2, z_3, z_4$  in the complex plane are the vertices of a parallelogram taken in order if and only if  
 (1)  $z_1 + z_4 = z_2 + z_3$  (2)  $z_1 + z_3 = z_2 + z_4$   
 (3)  $z_1 + z_2 = z_3 + z_4$  (iv)  $z_1 - z_2 = z_3 - z_4$
- (63) If  $z$  represents a complex number then  $\arg(z) + \arg(\bar{z})$  is  
 (1)  $\pi/4$  (2)  $\pi/2$  (3)  $0$  (4)  $\pi/4$
- (64) If the amplitude of a complex number is  $\pi/2$  then the number is  
 (1) purely imaginary (2) purely real  
 (3)  $0$  (4) neither real nor imaginary
- (65) If the point represented by the complex number  $iz$  is rotated about the origin through the angle  $\frac{\pi}{2}$  in the counter clockwise direction then the complex number representing the new position is  
 (1)  $iz$  (2)  $-iz$  (3)  $-z$  (4)  $z$
- (66) The polar form of the complex number  $(i^{25})^3$  is  
 (1)  $\cos \frac{\pi}{2} + i \sin \frac{\pi}{2}$  (2)  $\cos \pi + i \sin \pi$   
 (3)  $\cos \pi - i \sin \pi$  (4)  $\cos \frac{\pi}{2} - i \sin \frac{\pi}{2}$



(67) If  $P$  represents the variable complex number  $z$  and if  $|2z - 1| = 2|z|$  then the locus of  $P$  is

(1) the straight line  $x = \frac{1}{4}$

(2) the straight line  $y = \frac{1}{4}$

(3) the straight line  $z = \frac{1}{2}$

(4) the circle  $x^2 + y^2 - 4x - 1 = 0$

(68)  $\frac{1 + e^{-i\theta}}{1 + e^{i\theta}} =$

(1)  $\cos \theta + i \sin \theta$

(2)  $\cos \theta - i \sin \theta$

(3)  $\sin \theta - i \cos \theta$

(4)  $\sin \theta + i \cos \theta$

(69) If  $z_n = \cos \frac{n\pi}{3} + i \sin \frac{n\pi}{3}$  then  $z_1 z_2 \dots z_6$  is

(1) 1

(2) -1

(3)  $i$

(4)  $-i$

(70) If  $-\bar{z}$  lies in the third quadrant then  $z$  lies in the

(1) first quadrant

(2) second quadrant

(3) third quadrant

(4) fourth quadrant

(71) If  $x = \cos \theta + i \sin \theta$  the value of  $x^n + \frac{1}{x^n}$  is

(1)  $2 \cos n\theta$

(2)  $2 i \sin n\theta$

(3)  $2 \sin n\theta$

(4)  $2 i \cos n\theta$

(72) If  $a = \cos \alpha - i \sin \alpha$ ,  $b = \cos \beta - i \sin \beta$

$c = \cos \gamma - i \sin \gamma$  then  $(a^2 c^2 - b^2) / abc$  is

(1)  $\cos 2(\alpha - \beta + \gamma) + i \sin 2(\alpha - \beta + \gamma)$

(2)  $-2 \cos (\alpha - \beta + \gamma)$

(3)  $-2 i \sin (\alpha - \beta + \gamma)$

(4)  $2 \cos (\alpha - \beta + \gamma)$

(73)  $z_1 = 4 + 5i$ ,  $z_2 = -3 + 2i$  then  $\frac{z_1}{z_2}$  is

(1)  $\frac{2}{13} - \frac{22}{13}i$

(2)  $-\frac{2}{13} + \frac{22}{13}i$

(3)  $\frac{-2}{13} - \frac{23}{13}i$

(4)  $\frac{2}{13} + \frac{22}{13}i$

(74) The value of  $i + i^{22} + i^{23} + i^{24} + i^{25}$  is

(1)  $i$

(2)  $-i$

(3) 1

(4) -1

(75) The conjugate of  $i^{13} + i^{14} + i^{15} + i^{16}$  is

(1)  $1(2) - 1$

(3) 0

(4)  $-i$



- (76) If  $-i + 2$  is one root of the equation  $ax^2 - bx + c = 0$ , then the other root is  
 (1)  $-i - 2$  (2)  $i - 2$  (3)  $2 + i$  (4)  $2i + i$
- (77) The quadratic equation whose roots are  $\pm i\sqrt{7}$  is  
 (1)  $x^2 + 7 = 0$  (2)  $x^2 - 7 = 0$   
 (3)  $x^2 + x + 7 = 0$  (4)  $x^2 - x - 7 = 0$
- (78) The equation having  $4 - 3i$  and  $4 + 3i$  as roots is  
 (1)  $x^2 + 8x + 25 = 0$  (2)  $x^2 + 8x - 25 = 0$   
 (3)  $x^2 - 8x + 25 = 0$  (4)  $x^2 - 8x - 25 = 0$
- (79) If  $\frac{1-i}{1+i}$  is a root of the equation  $ax^2 + bx + 1 = 0$ , where  $a, b$  are real then  $(a, b)$  is  
 (1)  $(1, 1)$  (2)  $(1, -1)$  (3)  $(0, 1)$  (4)  $(1, 0)$
- (80) If  $-i + 3$  is a root of  $x^2 - 6x + k = 0$  then the value of  $k$  is  
 (1) 5 (2)  $\sqrt{5}$  (3)  $\sqrt{10}$  (4) 10
- (81) If  $\omega$  is a cube root of unity then the value of  $(1 - \omega + \omega^2)^4 + (1 + \omega - \omega^2)^4$  is  
 (1) 0 (2) 32 (3) -16 (4) -32
- (82) If  $\omega$  is the  $n$ th root of unity then  
 (1)  $1 + \omega^2 + \omega^4 + \dots = \omega + \omega^3 + \omega^5 + \dots$   
 (2)  $\omega^n = 0$  (3)  $\omega^n = 1$  (4)  $\omega = \omega^{n-1}$
- (83) If  $\omega$  is the cube root of unity then the value of  $(1 - \omega)(1 - \omega^2)(1 - \omega^4)(1 - \omega^8)$  is  
 (1) 9 (2) -9 (3) 16 (4) 32
- (84) The axis of the parabola  $y^2 - 2y + 8x - 23 = 0$  is  
 (1)  $y = -1$  (2)  $x = -3$  (3)  $x = 3$  (4)  $y = 1$
- (85)  $16x^2 - 3y^2 - 32x - 12y - 44 = 0$  represents  
 (1) an ellipse (2) a circle (3) a parabola (4) a hyperbola
- (86) The line  $4x + 2y = c$  is a tangent to the parabola  $y^2 = 16x$  then  $c$  is  
 (1) -1 (2) -2 (3) 4 (4) -4
- (87) The point of intersection of the tangents at  $t_1 = t$  and  $t_2 = 3t$  to the parabola  $y^2 = 8x$  is  
 (1)  $(6t^2, 8t)$  (2)  $(8t, 6t^2)$  (3)  $(t^2, 4t)$  (4)  $(4t, t^2)$

- (88) The length of the latus rectum of the parabola  $y^2 - 4x + 4y + 8 = 0$  is  
 (1) 8 (2) 6 (3) 4 (4) 2
- (89) The diretrix of the parabola  $y^2 = x + 4$  is  
 (1)  $x = \frac{15}{4}$  (2)  $x = -\frac{15}{4}$  (3)  $x = -\frac{17}{4}$  (4)  $x = \frac{17}{4}$
- (90) The length of the latus rectum of the parabola whose vertex is  $(2, -3)$  and the directrix  $x = 4$  is  
 (1) 2 (2) 4 (3) 6 (4) 8
- (91) The focus of the parabola  $x^2 = 16y$  is  
 (1)  $(4, 0)$  (2)  $(0, 4)$  (3)  $(-4, 0)$  (4)  $(0, -4)$
- (92) The vertex of the parabola  $x^2 = 8y - 1$  is  
 (1)  $(-\frac{1}{8}, 0)$  (2)  $(\frac{1}{8}, 0)$  (3)  $(0, \frac{1}{8})$  (4)  $(0, -\frac{1}{8})$
- (93) The line  $2x + 3y + 9 = 0$  touches the parabola  $y^2 = 8x$  at the point  
 (1)  $(0, -3)$  (2)  $(2, 4)$  (3)  $(-6, \frac{9}{2})$  (4)  $(\frac{9}{2}, -6)$
- (94) The tangents at the end of any focal chord to the parabola  $y^2 = 12x$  intersect on the line  
 (1)  $x - 3 = 0$  (2)  $x + 3 = 0$  (3)  $y + 3 = 0$  (4)  $y - 3 = 0$
- (95) The angle between the two tangents drawn from the point  $(-4, 4)$  to  $y^2 = 16x$  is  
 (1)  $45^\circ$  (2)  $30^\circ$  (3)  $60^\circ$  (4)  $90^\circ$
- (96) The eccentricity of the conic  $9x^2 + 5y^2 - 54x - 40y + 116 = 0$  is  
 (1)  $\frac{1}{3}$  (2)  $\frac{2}{3}$  (3)  $\frac{4}{9}$  (4)  $\frac{2}{\sqrt{5}}$
- (97) The length of the semi-major and the length of semi minor axis of the ellipse  $\frac{x^2}{144} + \frac{y^2}{169} = 1$  are  
 (1) 26, 12 (2) 13, 24 (3) 12, 26 (4) 13, 12
- (98) The distance between the foci of the ellipse  $9x^2 + 5y^2 = 180$  is  
 (1) 4 (2) 6 (3) 8 (4) 2

(99) If the length of major and semi-minor axes of an ellipse are 8, 2 and their corresponding equations are  $y - 6 = 0$  and  $x + 4 = 0$  then the equations of the ellipse is

(1)  $\frac{(x+4)^2}{4} + \frac{(y-6)^2}{16} = 1$

(2)  $\frac{(x+4)^2}{16} + \frac{(y-6)^2}{4} = 1$

(3)  $\frac{(x+4)^2}{16} - \frac{(y-6)^2}{4} = 1$

(4)  $\frac{(x+4)^2}{4} - \frac{(y-6)^2}{16} = 1$

(100) The straight line  $2x - y + c = 0$  is a tangent to the ellipse  $4x^2 + 8y^2 = 32$  if  $c$  is

(1)  $\pm 2\sqrt{3}$

(2)  $\pm 6$

(3) 36

(4)  $\pm 4$

(101) The sum of the distance of any point on the ellipse  $4x^2 + 9y^2 = 36$  from  $(\sqrt{5}, 0)$  and  $(-\sqrt{5}, 0)$  is

(1) 4

(2) 8

(3) 6

(4) 18

(102) The radius of the director circle of the conic  $9x^2 + 16y^2 = 144$  is

(1)  $\sqrt{7}$

(2) 4

(3) 3

(4) 5

(103) The locus of foot of perpendicular from the focus to a tangent of the curve  $16x^2 + 25y^2 = 400$  is

(1)  $x^2 + y^2 = 4$

(2)  $x^2 + y^2 = 25$

(3)  $x^2 + y^2 = 16$

(4)  $x^2 + y^2 = 9$

(104) The eccentricity of the hyperbola  $12y^2 - 4x^2 - 24x + 48y - 127 = 0$  is

(1) 4

(2) 3

(3) 2

(4) 6

(105) The eccentricity of the hyperbola whose latus rectum is equal to half of its conjugate axis is

(1)  $\frac{\sqrt{3}}{2}$

(2)  $\frac{5}{3}$

(3)  $\frac{3}{2}$

(4)  $\frac{\sqrt{5}}{2}$

(106) The difference between the focal distances of any point on the hyperbola

$\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$  is 24 and the eccentricity is 2. Then the equation of the hyperbola is

(1)  $\frac{x^2}{144} - \frac{y^2}{432} = 1$

(2)  $\frac{x^2}{432} - \frac{y^2}{144} = 1$

(3)  $\frac{x^2}{12} - \frac{y^2}{12\sqrt{3}} = 1$

(4)  $\frac{x^2}{12\sqrt{3}} - \frac{y^2}{12} = 1$

(107) The directrices of the hyperbola  $x^2 - 4(y - 3)^2 = 16$  are

(1)  $y = \pm \frac{8}{\sqrt{5}}$

(2)  $x = \pm \frac{8}{\sqrt{5}}$

(3)  $y = \pm \frac{\sqrt{5}}{8}$

(4)  $x = \pm \frac{\sqrt{5}}{8}$

- (108) The line  $5x - 2y + 4k = 0$  is a tangent to  $4x^2 - y^2 = 36$  then  $k$  is  
 (1)  $\frac{4}{9}$  (2)  $\frac{2}{3}$  (3)  $\frac{9}{4}$  (4)  $\frac{81}{16}$
- (109) The equation of the chord of contact of tangents from  $(2, 1)$  to the hyperbola  $\frac{x^2}{16} - \frac{y^2}{9} = 1$  is  
 (1)  $9x - 8y - 72 = 0$  (2)  $9x + 8y + 72 = 0$   
 (3)  $8x - 9y - 72 = 0$  (4)  $8x + 9y + 72 = 0$
- (110) The angle between the asymptotes to the hyperbola  $\frac{x^2}{16} - \frac{y^2}{9} = 1$  is  
 (1)  $\pi - 2 \tan^{-1} \left( \frac{3}{4} \right)$  (2)  $\pi - 2 \tan^{-1} \left( \frac{4}{3} \right)$   
 (3)  $2 \tan^{-1} \frac{3}{4}$  (4)  $2 \tan^{-1} \left( \frac{4}{3} \right)$
- (111) The asymptotes of the hyperbola  $36y^2 - 25x^2 + 900 = 0$  are  
 (1)  $y = \pm \frac{6}{5}x$  (2)  $y = \pm \frac{5}{6}x$  (3)  $y = \pm \frac{36}{25}x$  (4)  $y = \pm \frac{25}{36}x$
- (112) The product of the perpendiculars drawn from the point  $(8, 0)$  on the hyperbola to its asymptotes is  $\frac{x^2}{64} - \frac{y^2}{36} = 1$  is  
 (1)  $\frac{25}{576}$  (2)  $\frac{576}{25}$  (3)  $\frac{6}{25}$  (4)  $\frac{25}{6}$
- (113) The locus of the point of intersection of perpendicular tangents to the hyperbola  $\frac{x^2}{16} - \frac{y^2}{9} = 1$  is  
 (1)  $x^2 + y^2 = 25$  (2)  $x^2 + y^2 = 4$  (3)  $x^2 + y^2 = 3$  (4)  $x^2 + y^2 = 7$
- (114) The eccentricity of the hyperbola with asymptotes  $x + 2y - 5 = 0$ ,  $2x - y + 5 = 0$  is  
 (1) 3 (2)  $\sqrt{2}$  (3)  $\sqrt{3}$  (4) 2
- (115) Length of the semi-transverse axis of the rectangular hyperbola  $xy = 8$  is  
 (1) 2 (2) 4 (3) 16 (4) 8
- (116) The asymptotes of the rectangular hyperbola  $xy = c^2$  are  
 (1)  $x = c, y = c$  (2)  $x = 0, y = c$  (3)  $x = c, y = 0$  (4)  $x = 0, y = 0$
- (117) The co-ordinate of the vertices of the rectangular hyperbola  $xy = 16$  are  
 (1)  $(4, 4), (-4, -4)$  (2)  $(2, 8), (-2, -8)$   
 (3)  $(4, 0), (-4, 0)$  (4)  $(8, 0), (-8, 0)$

- (118) One of the foci of the rectangular hyperbola  $xy = 18$  is  
(1) (6, 6)                      (2) (3, 3)                      (3) (4, 4)                      (4) (5, 5)
- (119) The length of the latus rectum of the rectangular hyperbola  $xy = 32$  is  
(1)  $8\sqrt{2}$                       (2) 32                      (3) 8                      (4) 16
- (120) The area of the triangle formed by the tangent at any point on the rectangular hyperbola  $xy = 72$  and its asymptotes is  
(1) 36 (2) 18                      (3) 72                      (4) 144
- (121) The normal to the rectangular hyperbola  $xy = 9$  at  $\left(6, \frac{3}{2}\right)$  meets the curve again at  
(1)  $\left(\frac{3}{8}, 24\right)$                       (2)  $\left(-24, -\frac{3}{8}\right)$                       (3)  $\left(-\frac{3}{8}, -24\right)$                       (4)  $\left(24, \frac{3}{8}\right)$

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**KEY TO OBJECTIVE TYPE QUESTIONS**

Q.No	Key	Q.No	Key	Q.No	Key	Q.No	Key	Q.No	Key
1	1	26	4	51	2	76	3	101	3
2	3	27	2	52	1	77	1	102	4
3	1	28	2	53	3	78	3	103	2
4	3	29	4	54	3	79	4	104	3
5	1	30	3	55	3	80	4	105	4
6	3	31	1	56	4	81	3	106	1
7	3	32	1	57	1	82	3	107	2
8	4	33	3	58	4	83	1	108	3
9	3	34	4	59	3	84	4	109	1
10	3	35	2	60	3	85	4	110	3
11	1	36	1	61	4	86	4	111	2
12	4	37	3	62	2	87	1	112	2
13	1	38	3	63	3	88	3	113	1
14	2	39	3	64	1	89	3	114	2
15	1	40	4	65	3	90	4	115	2
16	4	41	1	66	4	91	2	116	4
17	1	42	2	67	1	92	3	117	1
18	2	43	2	68	2	93	4	118	1
19	3	44	4	69	2	94	2	119	4
20	3	45	2	70	4	95	4	120	4
21	4	46	2	71	1	96	2	121	3
22	2	47	2	72	3	97	4		
23	3	48	4	73	3	98	3		
24	4	49	1	74	1	99	2		
25	3	50	3	75	3	100	2		



## OBJECTIVE TYPE QUESTIONS

Choose the correct or most suitable answer :

- (1) The gradient of the curve  $y = -2x^3 + 3x + 5$  at  $x = 2$  is  
 (1)  $-20$             (2)  $27$             (3)  $-16$             (4)  $-21$
- (2) The rate of change of area  $A$  of a circle of radius  $r$  is  
 (1)  $2\pi r$             (2)  $2\pi r \frac{dr}{dt}$             (3)  $\pi r^2 \frac{dr}{dt}$             (4)  $\pi \frac{dr}{dt}$
- (3) The velocity  $v$  of a particle moving along a straight line when at a distance  $x$  from the origin is given by  $a + bv^2 = x^2$  where  $a$  and  $b$  are constants. Then the acceleration is  
 (1)  $\frac{b}{x}$             (2)  $\frac{a}{x}$             (3)  $\frac{x}{b}$             (4)  $\frac{x}{a}$
- (4) A spherical snowball is melting in such a way that its volume is decreasing at a rate of  $1 \text{ cm}^3 / \text{min}$ . The rate at which the diameter is decreasing when the diameter is  $10 \text{ cms}$  is  
 (1)  $\frac{-1}{50\pi} \text{ cm / min}$             (2)  $\frac{1}{50\pi} \text{ cm / min}$   
 (3)  $\frac{-11}{75\pi} \text{ cm / min}$             (4)  $\frac{-2}{75\pi} \text{ cm / min}$ .
- (5) The slope of the tangent to the curve  $y = 3x^2 + 3\sin x$  at  $x = 0$  is  
 (1)  $3$             (2)  $2$             (3)  $1$             (4)  $-1$
- (6) The slope of the normal to the curve  $y = 3x^2$  at the point whose  $x$  coordinate is  $2$  is  
 (1)  $\frac{1}{13}$             (2)  $\frac{1}{14}$             (3)  $\frac{-1}{12}$             (4)  $\frac{1}{12}$
- (7) The point on the curve  $y = 2x^2 - 6x - 4$  at which the tangent is parallel to the  $x$  - axis is  
 (1)  $\left(\frac{5}{2}, \frac{-17}{2}\right)$             (2)  $\left(\frac{-5}{2}, \frac{-17}{2}\right)$             (3)  $\left(\frac{-5}{2}, \frac{17}{2}\right)$             (4)  $\left(\frac{3}{2}, \frac{-17}{2}\right)$
- (8) The equation of the tangent to the curve  $y = \frac{x^3}{5}$  at the point  $(-1, -1/5)$  is  
 (1)  $5y + 3x = 2$             (2)  $5y - 3x = 2$             (3)  $3x - 5y = 2$             (4)  $3x + 3y = 2$

- (9) The equation of the normal to the curve  $\theta = \frac{1}{t}$  at the point  $(-3, -1/3)$  is  
 (1)  $3\theta = 27t - 80$  (2)  $5\theta = 27t - 80$   
 (3)  $3\theta = 27t + 80$  (4)  $\theta = \frac{1}{t}$
- (10) The angle between the curves  $\frac{x^2}{25} + \frac{y^2}{9} = 1$  and  $\frac{x^2}{8} - \frac{y^2}{8} = 1$  is  
 (1)  $\frac{\pi}{4}$  (2)  $\frac{\pi}{3}$  (3)  $\frac{\pi}{6}$  (4)  $\frac{\pi}{2}$
- (11) The angle between the curve  $y = e^{mx}$  and  $y = e^{-mx}$  for  $m > 1$  is  
 (1)  $\tan^{-1}\left(\frac{2m}{m^2-1}\right)$  (2)  $\tan^{-1}\left(\frac{2m}{1-m^2}\right)$   
 (3)  $\tan^{-1}\left(\frac{-2m}{1+m^2}\right)$  (4)  $\tan^{-1}\left(\frac{2m}{m^2+1}\right)$
- (12) The parametric equations of the curve  $x^{2/3} + y^{2/3} = a^{2/3}$  are  
 (1)  $x = a \sin^3 \theta$  ;  $y = a \cos^3 \theta$  (2)  $x = a \cos^3 \theta$  ;  $y = a \sin^3 \theta$   
 (3)  $x = a^3 \sin \theta$  ;  $y = a^3 \cos \theta$  (4)  $x = a^3 \cos \theta$  ;  $y = a^3 \sin \theta$
- (13) If the normal to the curve  $x^{2/3} + y^{2/3} = a^{2/3}$  makes an angle  $\theta$  with the  $x$ -axis then the slope of the normal is  
 (1)  $-\cot \theta$  (2)  $\tan \theta$  (3)  $-\tan \theta$  (4)  $\cot \theta$
- (14) If the length of the diagonal of a square is increasing at the rate of  $0.1 \text{ cm / sec}$ . What is the rate of increase of its area when the side is  $\frac{15}{\sqrt{2}} \text{ cm}$ ?  
 (1)  $1.5 \text{ cm}^2/\text{sec}$  (2)  $3 \text{ cm}^2/\text{sec}$  (3)  $3\sqrt{2} \text{ cm}^2/\text{sec}$  (4)  $0.15 \text{ cm}^2/\text{sec}$
- (15) What is the surface area of a sphere when the volume is increasing at the same rate as its radius?  
 (1) 1 (2)  $\frac{1}{2\pi}$  (3)  $4\pi$  (4)  $\frac{4\pi}{3}$
- (16) For what values of  $x$  is the rate of increase of  $x^3 - 2x^2 + 3x + 8$  is twice the rate of increase of  $x$   
 (1)  $\left(-\frac{1}{3}, -3\right)$  (2)  $\left(\frac{1}{3}, 3\right)$  (3)  $\left(-\frac{1}{3}, 3\right)$  (4)  $\left(\frac{1}{3}, 1\right)$
- (17) The radius of a cylinder is increasing at the rate of  $2 \text{ cm / sec}$  and its altitude is decreasing at the rate of  $3 \text{ cm / sec}$ . The rate of change of volume when the radius is  $3 \text{ cm}$  and the altitude is  $5 \text{ cm}$  is  
 (1)  $23\pi$  (2)  $33\pi$  (3)  $43\pi$  (4)  $53\pi$

- (18) If  $y = 6x - x^3$  and  $x$  increases at the rate of 5 units per second, the rate of change of slope when  $x = 3$  is  
 (1)  $-90$  units / sec (2)  $90$  units / sec  
 (3)  $180$  units / sec (4)  $-180$  units / sec
- (19) If the volume of an expanding cube is increasing at the rate of  $4\text{cm}^3 / \text{sec}$  then the rate of change of surface area when the volume of the cube is 8 cubic cm is  
 (1)  $8\text{cm}^2/\text{sec}$  (2)  $16\text{cm}^2 / \text{sec}$  (3)  $2\text{cm}^2 / \text{sec}$  (4)  $4\text{cm}^2 / \text{sec}$
- (20) The gradient of the tangent to the curve  $y = 8 + 4x - 2x^2$  at the point where the curve cuts the  $y$ -axis is  
 (1) 8 (2) 4 (3) 0 (4)  $-4$
- (21) The Angle between the parabolas  $y^2 = x$  and  $x^2 = y$  at the origin is  
 (1)  $2 \tan^{-1} \left( \frac{3}{4} \right)$  (2)  $\tan^{-1} \left( \frac{4}{3} \right)$  (3)  $\frac{\pi}{2}$  (4)  $\frac{\pi}{4}$
- (22) For the curve  $x = e^t \cos t$  ;  $y = e^t \sin t$  the tangent line is parallel to the  $x$ -axis when  $t$  is equal to  
 (1)  $-\frac{\pi}{4}$  (2)  $\frac{\pi}{4}$  (3) 0 (4)  $\frac{\pi}{2}$
- (23) If a normal makes an angle  $\theta$  with positive  $x$ -axis then the slope of the curve at the point where the normal is drawn is  
 (1)  $-\cot \theta$  (2)  $\tan \theta$  (3)  $-\tan \theta$  (4)  $\cot \theta$
- (24) The value of 'a' so that the curves  $y = 3e^x$  and  $y = \frac{a}{3} e^{-x}$  intersect orthogonally is  
 (1)  $-1$  (2) 1 (3)  $\frac{1}{3}$  (4) 3
- (25) If  $s = t^3 - 4t^2 + 7$ , the velocity when the acceleration is zero is  
 (1)  $\frac{32}{3}$  m/sec (2)  $\frac{-16}{3}$  m/sec (3)  $\frac{16}{3}$  m/sec (4)  $\frac{-32}{3}$  m/sec
- (26) If the velocity of a particle moving along a straight line is directly proportional to the square of its distance from a fixed point on the line. Then its acceleration is proportional to  
 (1)  $s$  (2)  $s^2$  (3)  $s^3$  (4)  $s^4$
- (27) The Rolle's constant for the function  $y = x^2$  on  $[-2, 2]$  is  
 (1)  $\frac{2\sqrt{3}}{3}$  (2) 0 (3) 2 (4)  $-2$

- (28) The 'c' of Lagranges Mean Value Theorem for the function  $f(x) = x^2 + 2x - 1$  ;  $a = 0$ ,  $b = 1$  is  
 (1) -1                      (2) 1                      (3) 0                      (4)  $\frac{1}{2}$
- (29) The value of c in Rolle's Theorem for the function  $f(x) = \cos \frac{x}{2}$  on  $[\pi, 3\pi]$  is  
 (1) 0                      (2)  $2\pi$                       (3)  $\frac{\pi}{2}$                       (4)  $\frac{3\pi}{2}$
- (30) The value of 'c' of Lagranges Mean Value Theorem for  $f(x) = \sqrt{x}$  when  $a = 1$  and  $b = 4$  is  
 (1)  $\frac{9}{4}$                       (2)  $\frac{3}{2}$                       (3)  $\frac{1}{2}$                       (4)  $\frac{1}{4}$
- (31)  $\lim_{x \rightarrow \infty} \frac{x^2}{e^x}$  is =  
 (1) 2                      (2) 0                      (3)  $\infty$                       (4) 1
- (32)  $\lim_{x \rightarrow 0} \frac{a^x - b^x}{c^x - d^x}$   
 (1)  $\infty$                       (2) 0                      (3)  $\log \frac{ab}{cd}$                       (4)  $\frac{\log(a/b)}{\log(c/d)}$
- (33) If  $f(a) = 2$ ;  $f'(a) = 1$  ;  $g(a) = -1$  ;  $g'(a) = 2$  then the value of  $\lim_{x \rightarrow a} \frac{g(x)f(a) - g(a)f(x)}{x - a}$  is  
 (1) 5                      (2) -5                      (3) 3                      (4) -3
- (34) Which of the following function is increasing in  $(0, \infty)$   
 (1)  $e^x$                       (2)  $\frac{1}{x}$                       (3)  $-x^2$                       (4)  $x^{-2}$
- (35) The function  $f(x) = x^2 - 5x + 4$  is increasing in  
 (1)  $(-\infty, 1)$                       (2)  $(1, 4)$                       (3)  $(4, \infty)$                       (4) everyw'
- (36) The function  $f(x) = x^2$  is decreasing in  
 (1)  $(-\infty, \infty)$                       (2)  $(-\infty, 0)$                       (3)  $(0, \infty)$                       (4)  $(-2, \infty)$



- (37) The function  $y = \tan x - x$  is
- (1) an increasing function in  $\left(0, \frac{\pi}{2}\right)$
  - (2) a decreasing function in  $\left(0, \frac{\pi}{2}\right)$
  - (3) increasing in  $\left(0, \frac{\pi}{4}\right)$  and decreasing in  $\left(\frac{\pi}{4}, \frac{\pi}{2}\right)$
  - (4) decreasing in  $\left(0, \frac{\pi}{4}\right)$  and increasing in  $\left(\frac{\pi}{4}, \frac{\pi}{2}\right)$
- (38) In a given semi circle of diameter 4 cm a rectangle is to be inscribed. The maximum area of the rectangle is
- (1) 2
  - (2) 4
  - (3) 8
  - (4) 16
- (39) The least possible perimeter of a rectangle of area  $100m^2$  is
- (1) 10
  - (2) 20
  - (3) 40
  - (4) 60
- (40) If  $f(x) = x^2 - 4x + 5$  on  $[0, 3]$  then the absolute maximum value is
- (1) 2
  - (2) 3
  - (3) 4
  - (4) 5
- (41) The curve  $y = -e^{-x}$  is
- (1) concave upward for  $x > 0$
  - (2) concave downward for  $x > 0$
  - (2) everywhere concave upward
  - (4) everywhere concave downward
- (42) Which of the following curves is concave down?
- (1)  $y = -x^2$
  - (2)  $y = x^2$
  - (3)  $y = e^x$
  - (4)  $y = x^2 + 2x - 3$
- (43) The point of inflexion of the curve  $y = x^4$  is at
- (1)  $x = 0$
  - (2)  $x = 3$
  - (3)  $x = 12$
  - (4) nowhere
- (44) The curve  $y = ax^3 + bx^2 + cx + d$  has a point of inflexion at  $x = 1$  then
- (1)  $a + b = 0$
  - (2)  $a + 3b = 0$
  - (3)  $3a + b = 0$
  - (4)  $3a + b = 1$
- (45) If  $u = x^y$  then  $\frac{\partial u}{\partial x}$  is equal to
- (1)  $yx^{y-1}$
  - (2)  $u \log x$
  - (3)  $u \log y$
  - (4)  $xy^{x-1}$
- (46) If  $u = \sin^{-1}\left(\frac{x^4 + y^4}{x^2 + y^2}\right)$  and  $f = \sin u$  then  $f$  is a homogeneous function of degree
- (1) 0
  - (2) 1
  - (3) 2
  - (4) 4
- (47) If  $u = \frac{1}{\sqrt{x^2 + y^2}}$ , then  $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y}$  is equal to
- (1)  $\frac{1}{2}u$
  - (2)  $u$
  - (3)  $\frac{3}{2}u$
  - (4)  $-u$

- (48) The curve  $y^2(x-2) = x^2(1+x)$  has  
 (1) an asymptote parallel to  $x$ -axis (2) an asymptote parallel to  $y$ -axis  
 (3) asymptotes parallel to both axes (4) no asymptotes
- (49) If  $x = r \cos \theta$ ,  $y = r \sin \theta$ , then  $\frac{\partial r}{\partial x}$  is equal to  
 (1)  $\sec \theta$  (2)  $\sin \theta$  (3)  $\cos \theta$  (4)  $\operatorname{cosec} \theta$
- (50) Identify the true statements in the following :  
 (i) If a curve is symmetrical about the origin, then it is symmetrical about both axes.  
 (ii) If a curve is symmetrical about both the axes, then it is symmetrical about the origin.  
 (iii) A curve  $f(x, y) = 0$  is symmetrical about the line  $y = x$  if  $f(x, y) = f(y, x)$ .  
 (iv) For the curve  $f(x, y) = 0$ , if  $f(x, y) = f(-y, -x)$ , then it is symmetrical about the origin.  
 (1) (ii), (iii) (2) (i), (iv) (3) (i), (iii) (4) (ii), (iv)
- (51) If  $u = \log \left( \frac{x^2 + y^2}{xy} \right)$  then  $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y}$  is  
 (1) 0 (2)  $u$  (3)  $2u$  (4)  $u^{-1}$
- (52) The percentage error in the 11th root of the number 28 is approximately \_\_\_\_\_ times the percentage error in 28.  
 (1)  $\frac{1}{28}$  (2)  $\frac{1}{11}$  (3) 11 (4) 28
- (53) The curve  $a^2y^2 = x^2(a^2 - x^2)$  has  
 (1) only one loop between  $x = 0$  and  $x = a$   
 (2) two loops between  $x = 0$  and  $x = a$   
 (3) two loops between  $x = -a$  and  $x = a$   
 (4) no loop
- (54) An asymptote to the curve  $y^2(a + 2x) = x^2(3a - x)$  is  
 (1)  $x = 3a$  (2)  $x = -a/2$  (3)  $x = a/2$  (4)  $x = 0$
- (55) In which region the curve  $y^2(a + x) = x^2(3a - x)$  does not lie?  
 (1)  $x > 0$  (2)  $0 < x < 3a$  (3)  $x \leq -a$  and  $x > 3a$  (4)  $-a < x < 3a$
- (56) If  $u = y \sin x$ , then  $\frac{\partial^2 u}{\partial x \partial y}$  is equal to  
 (1)  $\cos x$  (2)  $\cos y$  (3)  $\sin x$  (4) 0



- (57) If  $u = f\left(\frac{y}{x}\right)$  then  $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y}$  is equal to  
 (1) 0 (2) 1 (3)  $2u$  (4)  $u$
- (58) The curve  $9y^2 = x^2(4 - x^2)$  is symmetrical about  
 (1) y-axis (2) x-axis (3)  $y = x$  (4) both the axes
- (59) The curve  $ay^2 = x^2(3a - x)$  cuts the y-axis at  
 (1)  $x = -3a, x = 0$  (2)  $x = 0, x = 3a$  (3)  $x = 0, x = a$  (4)  $x = 0$
- (60) The value of  $\int_0^{\pi/2} \frac{\cos^{5/3} x}{\cos^{5/3} x + \sin^{5/3} x} dx$  is  
 (1)  $\frac{\pi}{2}$  (2)  $\frac{\pi}{4}$  (3) 0 (4)  $\pi$
- (61) The value of  $\int_0^{\pi/2} \frac{\sin x - \cos x}{1 + \sin x \cos x} dx$  is  
 (1)  $\frac{\pi}{2}$  (2) 0 (3)  $\frac{\pi}{4}$  (4)  $\pi$
- (62) The value of  $\int_0^1 x(1-x)^4 dx$  is  
 (1)  $\frac{1}{12}$  (2)  $\frac{1}{30}$  (3)  $\frac{1}{24}$  (4)  $\frac{1}{20}$
- (63) The value of  $\int_{-\pi/2}^{\pi/2} \left(\frac{\sin x}{2 + \cos x}\right) dx$  is  
 (1) 0 (2) 2 (3)  $\log 2$  (4)  $\log 4$
- (64) The value of  $\int_0^{\pi} \sin^4 x dx$  is  
 (1)  $3\pi/16$  (2)  $3/16$  (3) 0 (4)  $3\pi/8$
- (65) The value of  $\int_0^{\pi/4} \cos^3 2x dx$  is  
 (1)  $\frac{2}{3}$  (2)  $\frac{1}{3}$  (3) 0 (4)  $\frac{2\pi}{3}$

- (66) The value of  $\int_0^{\pi} \sin^2 x \cos^3 x \, dx$  is  
 (1)  $\pi$  (2)  $\pi/2$  (3)  $\pi/4$  (4) 0
- (67) The area bounded by the line  $y = x$ , the  $x$ -axis, the ordinates  $x = 1$ ,  $x = 2$  is  
 (1)  $\frac{3}{2}$  (2)  $\frac{5}{2}$  (3)  $\frac{1}{2}$  (4)  $\frac{7}{2}$
- (68) The area of the region bounded by the graph of  $y = \sin x$  and  $y = \cos x$  between  $x = 0$  and  $x = \frac{\pi}{4}$  is  
 (1)  $\sqrt{2} + 1$  (2)  $\sqrt{2} - 1$  (3)  $2\sqrt{2} - 2$  (4)  $2\sqrt{2} + 2$
- (69) The area between the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  and its auxiliary circle is  
 (1)  $\pi b(a - b)$  (2)  $2\pi a(a - b)$  (3)  $\pi a(a - b)$  (4)  $2\pi b(a - b)$
- (70) The area bounded by the parabola  $y^2 = x$  and its latus rectum is  
 (1)  $\frac{4}{3}$  (2)  $\frac{1}{6}$  (3)  $\frac{2}{3}$  (4)  $\frac{8}{3}$
- (71) The volume of the solid obtained by revolving  $\frac{x^2}{9} + \frac{y^2}{16} = 1$  about the minor axis is  
 (1)  $48\pi$  (2)  $64\pi$  (3)  $32\pi$  (4)  $128\pi$
- (72) The volume, when the curve  $y = \sqrt{3 + x^2}$  from  $x = 0$  to  $x = 4$  is rotated about  $x$ -axis is  
 (1)  $100\pi$  (2)  $\frac{100}{9}\pi$  (3)  $\frac{100}{3}\pi$  (4)  $\frac{100}{3}$
- (73) The volume generated when the region bounded by  $y = x$ ,  $y = 1$ ,  $x = 0$  is rotated about  $y$ -axis is  
 (1)  $\frac{\pi}{4}$  (2)  $\frac{\pi}{2}$  (3)  $\frac{\pi}{3}$  (4)  $\frac{2\pi}{3}$
- (74) Volume of solid obtained by revolving the area of the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  about major and minor axes are in the ratio  
 (1)  $b^2 : a^2$  (2)  $a^2 : b^2$  (3)  $a : b$  (4)  $b : a$
- (75) The volume generated by rotating the triangle with vertices at  $(0, 0)$ ,  $(3, 0)$  and  $(3, 3)$  about  $x$ -axis is  
 (1)  $18\pi$  (2)  $2\pi$  (3)  $36\pi$  (4)  $9\pi$

- (76) The length of the arc of the curve  $x^{2/3} + y^{2/3} = 4$  is  
 (1) 48 (2) 24  
 (3) 12 (4) 96
- (77) The surface area of the solid of revolution of the region bounded by  $y = 2x$ ,  $x = 0$  and  $x = 2$  about  $x$ -axis is  
 (1)  $8\sqrt{5}\pi$  (2)  $2\sqrt{5}\pi$  (3)  $\sqrt{5}\pi$  (4)  $4\sqrt{5}\pi$
- (78) The curved surface area of a sphere of radius 5, intercepted between two parallel planes of distance 2 and 4 from the centre is  
 (1)  $20\pi$  (2)  $40\pi$  (3)  $10\pi$  (4)  $30\pi$
- (79) The integrating factor of  $\frac{dy}{dx} + 2\frac{y}{x} = e^{4x}$  is  
 (1)  $\log x$  (2)  $x^2$  (3)  $e^x$  (4)  $x$
- (80) If  $\cos x$  is an integrating factor of the differential equation  $\frac{dy}{dx} + Py = Q$  then  $P =$   
 (1)  $-\cot x$  (2)  $\cot x$  (3)  $\tan x$  (4)  $-\tan x$
- (81) The integrating factor of  $dx + xdy = e^{-y} \sec^2 y dy$  is  
 (1)  $e^x$  (2)  $e^{-x}$  (3)  $e^y$  (4)  $e^{-y}$
- (82) Integrating factor of  $\frac{dy}{dx} + \frac{1}{x \log x} \cdot y = \frac{2}{x^2}$  is  
 (1)  $e^x$  (2)  $\log x$  (3)  $\frac{1}{x}$  (4)  $e^{-x}$
- (83) Solution of  $\frac{dx}{dy} + mx = 0$ , where  $m < 0$  is  
 (1)  $x = ce^{my}$  (2)  $x = ce^{-my}$  (3)  $x = my + c$  (4)  $x = c$
- (84)  $y = cx - c^2$  is the general solution of the differential equation  
 (1)  $(y')^2 - xy' + y = 0$  (2)  $y'' = 0$   
 (3)  $y' = c$  (4)  $(y')^2 + xy' + y = 0$
- (85) The differential equation  $\left(\frac{dx}{dy}\right)^2 + 5y^{1/3} = x$  is  
 (1) of order 2 and degree 1  
 (2) of order 1 and degree 2  
 (3) of order 1 and degree 6  
 (4) of order 1 and degree 3
- (86) The differential equation of all non-vertical lines in a plane is  
 (1)  $\frac{dy}{dx} = 0$  (2)  $\frac{d^2y}{dx^2} = 0$  (3)  $\frac{dy}{dx} = m$  (4)  $\frac{d^2y}{dx^2} = m$

(87) The differential equation of all circles with centre at the origin is

- (1)  $x dy + y dx = 0$  (2)  $x dy - y dx = 0$   
 (3)  $x dx + y dy = 0$  (4)  $x dx - y dy = 0$

(88) The integrating factor of the differential equation  $\frac{dy}{dx} + py = Q$  is

- (1)  $\int p dx$  (2)  $\int Q dx$  (3)  $e^{\int Q dx}$  (4)  $e^{\int p dx}$

(89) The complementary function of  $(D^2 + 1)y = e^{2x}$  is

- (1)  $(Ax + B)e^x$  (2)  $A \cos x + B \sin x$  (3)  $(Ax + B)e^{2x}$  (4)  $(Ax + B)e^{-x}$

(90) A particular integral of  $(D^2 - 4D + 4)y = e^{2x}$  is

- (1)  $\frac{x^2}{2} e^{2x}$  (2)  $x e^{2x}$  (3)  $x e^{-2x}$  (4)  $\frac{x}{2} e^{-2x}$

(91) The differential equation of the family of lines  $y = mx$  is

- (1)  $\frac{dy}{dx} = m$  (2)  $y dx - x dy = 0$   
 (3)  $\frac{d^2 y}{dx^2} = 0$  (4)  $y dx + x dy = 0$

(92) The degree of the differential equation  $\sqrt{1 + \left(\frac{dy}{dx}\right)^{1/3}} = \frac{d^2 y}{dx^2}$

- (1) 1 (2) 2 (3) 3 (4) 6

(93) The degree of the differential equation  $c = \frac{\left[1 + \left(\frac{dy}{dx}\right)^3\right]^{2/3}}{\frac{d^3 y}{dx^3}}$  where  $c$  is a

constant is

- (1) 1 (2) 3 (3) -2 (4) 2

(94) The amount present in a radio active element disintegrates at a rate proportional to its amount. The differential equation corresponding to the above statement is ( $k$  is negative)

- (1)  $\frac{dp}{dt} = \frac{k}{p}$  (2)  $\frac{dp}{dt} = kt$  (3)  $\frac{dp}{dt} = kp$  (4)  $\frac{dp}{dt} = -kt$

(95) The differential equation satisfied by all the straight lines in  $xy$  plane is

- (1)  $\frac{dy}{dx} = \text{a constant}$  (2)  $\frac{d^2 y}{dx^2} = 0$  (3)  $y + \frac{dy}{dx} = 0$  (4)  $\frac{d^2 y}{dx^2} + y = 0$

(96) If  $y = ke^{\lambda x}$  then its differential equation is

(1)  $\frac{dy}{dx} = \lambda y$       (2)  $\frac{dy}{dx} = ky$       (3)  $\frac{dy}{dx} + ky = 0$       (4)  $\frac{dy}{dx} = e^{\lambda x}$

(97) The differential equation obtained by eliminating  $a$  and  $b$  from  $y = ae^{3x} + be^{-3x}$  is

(1)  $\frac{d^2y}{dx^2} + ay = 0$       (2)  $\frac{d^2y}{dx^2} - 9y = 0$       (3)  $\frac{d^2y}{dx^2} - 9\frac{dy}{dx} = 0$       (4)  $\frac{d^2y}{dx^2} + 9x = 0$

(98) The differential equation formed by eliminating  $A$  and  $B$  from the relation  $y = e^x (A \cos x + B \sin x)$  is

(1)  $y_2 + y_1 = 0$       (2)  $y_2 - y_1 = 0$   
 (3)  $y_2 - 2y_1 + 2y = 0$       (4)  $y_2 - 2y_1 - 2y = 0$

(99) If  $\frac{dy}{dx} = \frac{x-y}{x+y}$  then

(1)  $2xy + y^2 + x^2 = c$       (2)  $x^2 + y^2 - x + y = c$   
 (3)  $x^2 + y^2 - 2xy = c$       (4)  $x^2 - y^2 - 2xy = c$

(100) If  $f'(x) = \sqrt{x}$  and  $f(1) = 2$  then  $f(x)$  is

(1)  $-\frac{2}{3}(x\sqrt{x} + 2)$       (2)  $\frac{3}{2}(x\sqrt{x} + 2)$   
 (3)  $\frac{2}{3}(x\sqrt{x} + 2)$       (4)  $\frac{2}{3}x(\sqrt{x} + 2)$

(101) On putting  $y = vx$ , the homogeneous differential equation  $x^2 dy + y(x+y)dx = 0$  becomes

(1)  $x dv + (2v + v^2)dx = 0$       (2)  $v dx + (2x + x^2)dv = 0$   
 (3)  $v^2 dx - (x + x^2)dv = 0$       (4)  $v dv + (2x + x^2)dx = 0$

(102) The integrating factor of the differential equation  $\frac{dy}{dx} - y \tan x = \cos x$  is

(1)  $\sec x$       (2)  $\cos x$       (3)  $e^{\tan x}$       (4)  $\cot x$

(103) The P.I. of  $(3D^2 + D - 14)y = 13e^{2x}$  is

(1)  $26x e^{2x}$       (2)  $13x e^{2x}$       (3)  $x e^{2x}$       (4)  $x^2/2 e^{2x}$

(104) The particular integral of the differential equation  $f(D)y = e^{ax}$  where  $f(D) = (D - a)g(D)$ ,  $g(a) \neq 0$  is

(1)  $me^{ax}$       (2)  $\frac{e^{ax}}{g(a)}$       (3)  $g(a)e^{ax}$       (4)  $\frac{xe^{ax}}{g(a)}$



- (105) Which of the following are statements?  
 (i) May God bless you. (ii) Rose is a flower  
 (iii) Milk is white. (iv) 1 is a prime number  
 (1) (i), (ii), (iii) (2) (i), (ii), (iv) (3) (i), (iii), (iv) (4) (ii), (iii), (iv)
- (106) If a compound statement is made up of three simple statements, then the number of rows in the truth table is  
 (1) 8 (2) 6 (3) 4 (4) 2
- (107) If  $p$  is  $T$  and  $q$  is  $F$ , then which of the following have the truth value  $T$ ?  
 (i)  $p \vee q$  (ii)  $\sim p \vee q$  (iii)  $p \vee \sim q$  (iv)  $p \wedge \sim q$   
 (1) (i), (ii), (iii) (2) (i), (ii), (iv)  
 (3) (i), (iii), (iv) (4) (ii), (iii), (iv)
- (108) The number of rows in the truth table of  $\sim [p \wedge (\sim q)]$  is  
 (1) 2 (2) 4 (3) 6 (4) 8
- (109) The conditional statement  $p \rightarrow q$  is equivalent to  
 (1)  $p \vee q$  (2)  $p \vee \sim q$  (3)  $\sim p \vee q$  (4)  $p \wedge q$
- (110) Which of the following is a tautology?  
 (1)  $p \vee q$  (2)  $p \wedge q$  (3)  $p \vee \sim p$  (4)  $p \wedge \sim p$
- (111) Which of the following is a contradiction?  
 (1)  $p \vee q$  (2)  $p \wedge q$  (3)  $p \vee \sim p$  (4)  $p \wedge \sim p$
- (112)  $p \leftrightarrow q$  is equivalent to  
 (1)  $p \rightarrow q$  (2)  $q \rightarrow p$  (3)  $(p \rightarrow q) \vee (q \rightarrow p)$  (4)  $(p \rightarrow q) \wedge (q \rightarrow p)$
- (113) Which of the following is not a binary operation on  $R$ ?  
 (1)  $a * b = ab$  (2)  $a * b = a - b$   
 (3)  $a * b = \sqrt{ab}$  (4)  $a * b = \sqrt{a^2 + b^2}$
- (114) A monoid becomes a group if it also satisfies the  
 (1) closure axiom (2) associative axiom  
 (3) identity axiom (4) inverse axiom
- (115) Which of the following is not a group?  
 (1)  $(\mathbb{Z}_n, +_n)$  (2)  $(\mathbb{Z}, +)$  (3)  $(\mathbb{Z}, \cdot)$  (4)  $(\mathbb{R}, +)$
- (116) In the set of integers with operation  $*$  defined by  $a * b = a + b - ab$ , the value of  $3 * (4 * 5)$  is  
 (1) 25 (2) 15 (3) 10 (4) 5
- (117) The order of  $[7]$  in  $(\mathbb{Z}_9, +_9)$  is  
 (1) 9 (2) 6 (3) 3 (4) 1
- (118) In the multiplicative group of cube root of unity, the order of  $w^2$  is  
 (1) 4 (2) 3 (3) 2 (4) 1



(119) The value of  $[3]_{+11} ([5]_{+11} [6])$  is

- (1) [0]                      (2) [1]                      (3) [2]                      (4) [3]

(120) In the set of real numbers  $R$ , an operation  $*$  is defined by

$$a * b = \sqrt{a^2 + b^2}. \text{ Then the value of } (3 * 4) * 5 \text{ is}$$

- (1) 5                      (2)  $5\sqrt{2}$                       (3) 25                      (4) 50

(121) Which of the following is correct?

- (1) An element of a group can have more than one inverse.  
 (2) If every element of a group is its own inverse, then the group is abelian.  
 (3) The set of all  $2 \times 2$  real matrices forms a group under matrix multiplication.  
 (4)  $(a * b)^{-1} = a^{-1} * b^{-1}$  for all  $a, b \in G$

(122) The order of  $-i$  in the multiplicative group of 4<sup>th</sup> roots of unity is

- (1) 4                      (ii) 3                      (3) 2                      (4) 1

(123) In the multiplicative group of  $n$ th roots of unity, the inverse of  $\omega^k$  is ( $k < n$ )

- (1)  $\omega^{1/k}$                       (2)  $\omega^{-1}$                       (3)  $\omega^{n-k}$                       (4)  $\omega^{n/k}$

(124) In the set of integers under the operation  $*$  defined by  $a * b = a + b - 1$ , the identity element is

- (1) 0                      (2) 1                      (3)  $a$                       (4)  $b$

(125) If  $f(x) = \begin{cases} kx^2, & 0 < x < 3 \\ 0, & \text{elsewhere} \end{cases}$  is a probability density function then the value of  $k$  is

- (1)  $\frac{1}{3}$                       (2)  $\frac{1}{6}$                       (3)  $\frac{1}{9}$                       (4)  $\frac{1}{12}$

(126) If  $f(x) = \frac{A}{\pi} \frac{1}{16 + x^2}, -\infty < x < \infty$

is a p.d.f of a continuous random variable  $X$ , then the value of  $A$  is

- (1) 16                      (2) 8                      (3) 4                      (4) 1

(127) A random variable  $X$  has the following probability distribution

$X$	0	1	2	3	4	5
$P(X = x)$	$1/4$	$2a$	$3a$	$4a$	$5a$	$1/4$

Then  $P(1 \leq x \leq 4)$  is

- (1)  $\frac{10}{21}$                       (2)  $\frac{2}{7}$                       (3)  $\frac{1}{14}$                       (4)  $\frac{1}{2}$

(128) A random variable  $X$  has the following probability mass function as follows :

$X$	-2	3	1
$P(X = x)$	$\frac{\lambda}{6}$	$\frac{\lambda}{4}$	$\frac{\lambda}{12}$

Then the value of  $\lambda$  is

- (1) 1                      (2) 2                      (3) 3                      (4) 4

(129)  $X$  is a discrete random variable which takes the values 0, 1, 2 and

$P(X = 0) = \frac{144}{169}$ ,  $P(X = 1) = \frac{1}{169}$  then the value of  $P(X = 2)$  is

- (1)  $\frac{145}{169}$                       (2)  $\frac{24}{169}$                       (3)  $\frac{2}{169}$                       (4)  $\frac{143}{169}$

(130) A random variable  $X$  has the following p.d.f

$X$	0	1	2	3	4	5	6	7
$P(X = x)$	0	$k$	$2k$	$2k$	$3k$	$k^2$	$2k^2$	$7k^2 + k$

The value of  $k$  is

- (1)  $\frac{1}{8}$                       (2)  $\frac{1}{10}$                       (3) 0                      (4) -1 or  $\frac{1}{10}$

(131) Given  $E(X + c) = 8$  and  $E(X - c) = 12$  then the value of  $c$  is

- (1) -2                      (2) 4                      (3) -4                      (4) 2

(132)  $X$  is a random variable taking the values 3, 4 and 12 with probabilities

$\frac{1}{3}$ ,  $\frac{1}{4}$  and  $\frac{5}{12}$ . Then  $E(X)$  is

- (1) 5                      (2) 7                      (3) 6                      (4) 3

(133) Variance of the random variable  $X$  is 4. Its mean is 2. Then  $E(X^2)$  is

- (1) 2                      (2) 4                      (3) 6                      (4) 8

- (134)  $\mu_2 = 20$ ,  $\mu_2' = 276$  for a discrete random variable  $X$ . Then the mean of the random variable  $X$  is  
 (1) 16                      (2) 5                      (3) 2                      (4) 1
- (135)  $\text{Var}(4X + 3)$  is  
 (1) 7                      (2)  $16 \text{Var}(X)$                       (3) 19                      (4) 0
- (136) In 5 throws of a die, getting 1 or 2 is a success. The mean number of successes is  
 (1)  $\frac{5}{3}$                       (2)  $\frac{3}{5}$                       (3)  $\frac{5}{9}$                       (4)  $\frac{9}{5}$
- (137) The mean of a binomial distribution is 5 and its standard deviation is 2. Then the value of  $n$  and  $p$  are  
 (1)  $(\frac{4}{5}, 25)$                       (2)  $(25, \frac{4}{5})$                       (3)  $(\frac{1}{5}, 25)$                       (4)  $(25, \frac{1}{5})$
- (138) If the mean and standard deviation of a binomial distribution are 12 and 2 respectively. Then the value of its parameter  $p$  is  
 (1)  $\frac{1}{2}$                       (2)  $\frac{1}{3}$                       (3)  $\frac{2}{3}$                       (4)  $\frac{1}{4}$
- (139) In 16 throws of a die getting an even number is considered a success. Then the variance of the successes is  
 (1) 4                      (2) 6                      (3) 2                      (4) 256
- (140) A box contains 6 red and 4 white balls. If 3 balls are drawn at random, the probability of getting 2 white balls without replacement, is  
 (1)  $\frac{1}{20}$                       (2)  $\frac{18}{125}$                       (3)  $\frac{4}{25}$                       (4)  $\frac{3}{10}$
- (141) If 2 cards are drawn from a well shuffled pack of 52 cards, the probability that they are of the same colours without replacement, is  
 (1)  $\frac{1}{2}$                       (2)  $\frac{26}{51}$                       (3)  $\frac{25}{51}$                       (4)  $\frac{25}{102}$
- (142) If in a Poisson distribution  $P(X = 0) = k$  then the variance is  
 (1)  $\log \frac{1}{k}$                       (2)  $\log k$                       (3)  $e^\lambda$                       (4)  $\frac{1}{k}$
- (143) If a random variable  $X$  follows Poisson distribution such that  $E(X^2) = 30$  then the variance of the distribution is  
 (1) 6                      (2) 5                      (3) 30                      (4) 25

- (144) The distribution function  $F(X)$  of a random variable  $X$  is
- (1) a decreasing function
  - (2) a non-decreasing function
  - (3) a constant function
  - (4) increasing first and then decreasing
- (145) For a Poisson distribution with parameter  $\lambda = 0.25$  the value of the 2<sup>nd</sup> moment about the origin is
- (1) 0.25
  - (2) 0.3125
  - (3) 0.0625
  - (4) 0.025
- (146) In a Poisson distribution if  $P(X = 2) = P(X = 3)$  then the value of its parameter  $\lambda$  is
- (1) 6
  - (2) 2
  - (3) 3
  - (4) 0
- (147) If  $f(x)$  is a p.d.f of a normal distribution with mean  $\mu$  then  $\int_{-\infty}^{\infty} f(x) dx$  is
- (1) 1
  - (2) 0.5
  - (3) 0
  - (4) 0.25
- (148) The random variable  $X$  follows normal distribution
- $$f(x) = ce^{\frac{-1/2(x-100)^2}{25}}$$
- Then the value of  $c$  is
- (1)  $\sqrt{2\pi}$
  - (2)  $\frac{1}{\sqrt{2\pi}}$
  - (3)  $5\sqrt{2\pi}$
  - (4)  $\frac{1}{5\sqrt{2\pi}}$
- (149) If  $f(x)$  is a p.d.f. of a normal variate  $X$  and  $X \sim N(\mu, \sigma^2)$  then  $\int_{-\infty}^{\mu} f(x) dx$  is
- (1) undefined
  - (2) 1
  - (3) .5
  - (4) -.5
- (150) The marks secured by 400 students in a Mathematics test were normally distributed with mean 65. If 120 students got more marks above 85, the number of students securing marks between 45 and 65 is
- (1) 120
  - (2) 20
  - (3) 80
  - (4) 160

**KEY TO OBJECTIVE TYPE QUESTIONS**

Q.No	Key	Q.No	Key	Q.No	Key	Q.No	Key	Q.No	Key
1	4	31	2	61	2	91	2	121	2
2	2	32	4	62	2	92	4	122	1
3	3	33	1	63	1	93	2	123	3
4	2	34	1	64	4	94	3	124	2
5	1	35	3	65	2	95	2	125	3
6	3	36	2	66	4	96	1	126	3
7	4	37	1	67	1	97	2	127	4
8	2	38	2	68	2	98	3	128	2
9	3	39	3	69	3	99	4	129	2
10	4	40	4	70	2	100	3	130	2
11	1	41	4	71	2	101	1	131	1
12	2	42	1	72	3	102	2	132	2
13	2	43	4	73	3	103	3	133	4
14	1	44	3	74	4	104	4	134	1
15	1	45	1	75	4	105	4	135	2
16	4	46	3	76	1	106	1	136	1
17	2	47	4	77	1	107	3	137	4
18	1	48	2	78	1	108	2	138	3
19	1	49	3	79	2	109	3	139	1
20	2	50	1	80	4	110	3	140	4
21	3	51	1	81	3	111	4	141	3
22	1	52	2	82	2	112	4	142	1
23	1	53	3	83	2	113	3	143	2
24	2	54	2	84	1	114	4	144	2
25	2	55	3	85	2	115	3	145	2
26	3	56	1	86	2	116	1	146	3
27	2	57	1	87	3	117	1	147	1
28	4	58	4	88	4	118	2	148	4
29	2	59	4	89	2	119	4	149	3
30	1	60	2	90	1	120	2	150	3