

# QUARTERLY COMMON EXAMINATION - 2022

10 - Std

## MATHEMATICS

Reg. No. 

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Time : 2.30 hrs.

Marks : 100

**I Choose the best answer.**

14 X 1 = 14

1. If there are 1024 relations from a set  $A = \{1, 2, 3, 4, 5\}$  to a set  $B$ , then number of elements in  $B$  is  
a) 3                      b) 2                      c) 8                      d) 4
2. If  $f(x) = x^2 - x$  then  $f(x-1) - f(x+1) =$                       a)  $4x$                       b)  $2 - 2x$                       c)  $2 - 4x$                       d)  $4x - 2$
3. The sum of the exponents of the prime factors in the prime factorization of 1729 is  
a) 1                      b) 2                      c) 3                      d) 4
4.  $7^{44} \equiv \dots \pmod{100}$                       a)  $1^2$                       b) 2                      c) 3                      d) 4
5.  $y^2 + \frac{1}{y^2}$  is not equal to  
a)  $\frac{y^4 + 1}{y^2}$                       b)  $\left(y + \frac{1}{y}\right)^2$                       c)  $\left[y - \frac{1}{y}\right]^2 + 2$                       d)  $\left(y + \frac{1}{y}\right)^2 - 2$
6.  $\frac{a^2}{a^2 - b^2} + \frac{b^2}{b^2 - a^2} =$                       a)  $a - b$                       b)  $a + b$                       c)  $a^2 - b^2$                       d) 1
7. Graph of a linear polynomial is a  
a) straight line                      b) circle                      c) parabola                      d) hyperbola
8. In  $\triangle LMN$ ,  $\angle L = 60^\circ$ ,  $\angle M = 50^\circ$ . If  $\triangle LMN \sim \triangle PQR$  then the value of  $\angle R$  is  
a)  $40^\circ$                       b)  $70^\circ$                       c)  $30^\circ$                       d)  $110^\circ$
9. If in  $\triangle ABC$ ,  $DE \parallel BC$ ,  $AB = 3.6$  cm,  $AC = 2.4$  cm and  $AD = 2.1$  cm then the length of  $AE$  is  
a) 1.4 cm                      b) 1.8 cm                      c) 1.2 cm                      d) 1.05 cm
10. The straight line given by the equation  $x = 11$  is  
a) parallel to  $x$  axis                      b) parallel to  $y$  axis  
c) passing through the origin                      d) passing through the point  $(0, 11)$
11. If slope of the line  $PQ$  is  $\frac{1}{\sqrt{3}}$ , then, slope of the perpendicular bisector of  $PQ$  is  
a)  $\sqrt{3}$                       b)  $-\sqrt{3}$                       c)  $\frac{1}{\sqrt{3}}$                       d) 0
12. The equation of a line passing through the origin and perpendicular to the line  $7x - 3y + 4 = 0$  is  
a)  $7x - 3y + 4 = 0$                       b)  $3x - 7y + 4 = 0$                       c)  $3x + 7y = 0$                       d)  $7x - 3y = 0$
13. If  $\sin \theta = \cos \theta$  then  $2 \tan^2 \theta + \sin^2 \theta - 1$  is equal to                      a)  $-\frac{3}{2}$                       b)  $\frac{3}{2}$                       c)  $\frac{2}{3}$                       d)  $-\frac{2}{3}$
14. Variance of first 20 natural number is  
a) 32.25                      b) 44.25                      c) 33.25                      d) 30

**II Note : Answer any 10 questions. Question No. 20 is compulsory.**

10 X 2 = 20

15. If  $A \times B = \{(3, 2), (3, 4), (5, 2), (5, 4)\}$ , then find  $A$  and  $B$ .
16. If  $f(x) = 3x + 2$ ,  $g(x) = 6x - k$  and if  $f \circ g = g \circ f$ , then find the value of  $k$ .
17. Find the least number that is divisible by the first ten natural numbers.
18. If  $13824 = 2^a \times 3^b$  then find  $a$  and  $b$ .
19. Which term of an A.P 16, 11, 6, 1, ..... is ..... 54?

20. Find the excluded values of the following expression  $\frac{7p+2}{8p^2+13p+5}$ .

10 STD Maths Page - 1



21. Find the square root of  $\frac{400x^4y^{12}z^{16}}{100x^8y^4z^4}$ .
22. In  $\triangle ABC$  - D and E are points on the sides AB and AC respectively such that  $DE \parallel BC$ .  
If  $\frac{AD}{DB} = \frac{3}{4}$  and  $AC = 15\text{cm}$ , find AE.
23. Show that the points  $(-3, -4)$ ,  $(7, 2)$  and  $(12, 5)$  are collinear.
24. Find the slope of a line joining the points  $(5, \sqrt{5})$  with the origin.  $(0, 0)$
25. Find the equation of a straight line whose slope is  $-\frac{5}{4}$  and it passes through  $(-1, 2)$ .

26. Prove that :  $\sqrt{\frac{1+\sin\theta}{1-\sin\theta}} = \sec\theta + \tan\theta$ .

27. Find the range and co-efficient of range of the data 63, 89, 98, 125, 79, 108, 117, 68.

28. If  $P = \frac{a}{a+b}$ ,  $Q = \frac{b}{a+b}$  then find  $\frac{1}{P^2 - Q^2}$  Simplify:  $\frac{x^2 - 16}{x + 4} - \frac{x - 4}{x + 4}$   $(3b)$   $396, 504, 636$  H.C.F.

**III Note : Answer any 10 questions. Question No. 42 is compulsory.**

$10 \times 5 = 50$

29. Let  $f:A \rightarrow B$  be a function defined by  $f(x) = \frac{x}{2} - 1$  where  $A = \{2, 4, 6, 10, 12\}$ ,  $B = \{0, 1, 2, 4, 5, 9\}$  represent  $f$  by i) set of ordered pairs ii) as table iii) an arrow diagram iv) a graph.

30. If  $f(x) = 2x + 3$ ,  $g(x) = 1 - 2x$  and  $h(x) = 3x$ . Prove that  $f \circ (g \circ h) = (f \circ g) \circ h$ .

31. Find the sum of the all natural number between 100 and 1000 which are divisible by 11.  $108 + 119 + 130 + \dots$

32. Rekha has 15 square colour papers of sizes 10cm, 11cm, 12cm ..... 24cm. How much area can be decorated with these colour papers?  $990$

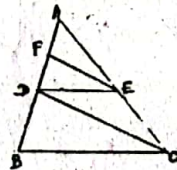
33. Solve :  $x + y + z = 5$ ,  $2x - y + z = 9$ ,  $x - 2y + 3z - 16 = 0$ .

34. If  $36x^4 - 60x^3 + 61x^2 - mx + n$  is a perfect square, find the values of  $m$  and  $n$ .

35. Solve :  $px^2 - (p + q)x + (p + q)^2 = 0$  by formula method.

36. State and prove Angle Bisector theorem.

37. In figure  $DE \parallel BC$  and  $CD \parallel EF$  prove that  $AD^2 = AB \times AF$ .



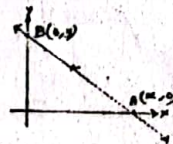
38. Find the area of the quadrilateral formed by the points  $(8, 6)$ ,  $(5, 11)$ ,  $(-5, 12)$  and  $(-4, 3)$ .

39. Find the equation of the perpendicular bisector of the line joining the points  $A(-4, 2)$  and  $B(6, 4)$ .

40. Prove that :  $\left( \frac{\cos^3 A - \sin^3 A}{\cos A - \sin A} \right) - \left( \frac{\cos^3 A + \sin^3 A}{\cos A + \sin A} \right) = 2\sin A \cos A$ .

41. The scores of a Cricketer in 7 matches are 70, 80, 60, 50, 40, 90, 95. Find the standard deviation.

42. A straight line cuts the co-ordinate axes at A and B. If the mid point of AB is  $(2, 3)$  find the equation of AB.



$2 \times 8 = 16$

**IV Note : Answer the following questions.**

43. a) construct a triangle similar to a given triangle ABC with its sides equal to  $\frac{6}{5}$  of the corresponding sides of the triangle ABC. (Scale factor  $\frac{6}{5}$ ) (OR)

- b) Construct a  $\triangle PQR$  which the base  $PQ = 4.5\text{cm}$ ,  $\angle R = 35^\circ$  and the median from R to RG is 6cm.

44. a) A bus is travelling at a uniform speed 50km/hr. Draw the distance - time graph and hence find i) the constant of variation. ii) how far will it travel in  $1\frac{1}{2}$  hour. iii) the time required to cover a distance of 300km from the graph. (OR)

Draw the graph of  $xy = 24$ ,  $x, y > 0$ . Using the graph find, i)  $y$  when  $x = 3$ , ii)  $x$  when  $y = 12$ .