# Sun Juition Center

poon thotta pathai hindu mission hospital opposite villupuram

# +2 Mathematics

Model Question paper

Life is a good circle you choose the best radius...

*Cell* 9629216361

## sun Tuition center -9629216361

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## HIGHER SECONDARY SECOND YEAR

## **MATHEMATICS**

## **MODEL OUESTION PAPER - 1**

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[Maximum Marks:90

Instructions:

- Check the question paper for fairness of printing. If there is any (a) lack of fairness, inform the Hall Supervisor immediately.
- Use Blue or Black ink to write and underline and pencil to draw (b) diagrams.

## PART – I

Note:

(i) All questions are compulsory.

 $20 \times 1 = 20$ 

- (ii) Choose the correct or most suitable answer from the given four alternatives. Write the option code and the corresponding answer.
- 1. If A and B are orthogonal, then  $(AB)^{T}(AB)$  is

(a) A

(b) B

(c) I

2. If A is a non-singular matrix such that  $A^{-1} = \begin{bmatrix} 5 & 3 \\ -2 & -1 \end{bmatrix}$ , then  $(A^T)^{-1} = \begin{bmatrix} 5 & 3 \\ -2 & -1 \end{bmatrix}$ 

(a)  $\begin{bmatrix} -5 & 3 \\ 2 & 1 \end{bmatrix}$  (b)  $\begin{bmatrix} 5 & 3 \\ -2 & -1 \end{bmatrix}$  (c)  $\begin{bmatrix} -1 & -3 \\ 2 & 5 \end{bmatrix}$  (d)  $\begin{bmatrix} 5 & -2 \\ 3 & -1 \end{bmatrix}$ 

3.  $i^n + i^{n+1} + i^{n+2} + i^{n+3}$  is

(c) -1

(d) *i* 

4. The product of all four values of  $\left(\cos\frac{\pi}{3} + i\sin\frac{\pi}{3}\right)^{\frac{1}{4}}$  is

(a) -2

(b) -1

(d) 2

5. A polynomial equation in x of degree n always has

(a) n distinct roots

(b) n real roots

(c) n imaginary roots

(d) at most one root.

6. If  $\sin^{-1} x + \sin^{-1} y = \frac{2\pi}{3}$ , then  $\cos^{-1} x + \cos^{-1} y$  is equal to

(a)  $\frac{2\pi}{2}$ 

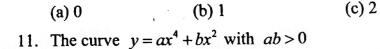
(b)  $\frac{\pi}{3}$ 

(c)  $\frac{\pi}{6}$ 

7. The equation of the directrix of the parabola  $y^2 = x + 4$  is

(a)  $x = \frac{15}{4}$  (b)  $x = -\frac{15}{4}$  (c)  $x = -\frac{17}{4}$ 

	(a) $15 < m < 65$	(b) $35 < m < 85$	` '	(u) 35 (	
9.	If the line $\frac{x-1}{3}$ =	$\frac{y-2}{4} = \frac{z-3}{\lambda}$ is p	perpendicular to the plane	$r\cdot (2i+3j+4k)=0,$	then the
	value of $\lambda$ is			WWW.Padasa	
	(a) $-\frac{13}{4}$	(b) −13	(c) -4	(d) $-\frac{1}{4}$	ishMet
10	Distance from the o	rigin to the plane	3x - 6y + 2z + 7 = 0 is	TANKIN Padasa	



- (a) has no horizontal tangent
- (b) is concave up

(c) is concave down

(d) has no points of inflection

12. The function 
$$f(x) = \sqrt[3]{4-x^2}$$
 has a vertical tangent at

(a) x = 0

- (b) x = 2 and x = -2
- (c) x = 0, x = 2 and x = -2
- (d) x = 1 and x = -1

- (a) 0.4 cu.cm
- (b) 0.45 cu.cm
- (c) 2 cu.cm
- (d) 0.8 cu.cm

(d) 3

14. 
$$\int_{0}^{\infty} e^{-3x} x^2 dx =$$

- (a)  $\frac{7}{27}$
- (b)  $\frac{5}{27}$
- (c)  $\frac{4}{27}$

(d)  $\frac{2}{27}$ 

15. The value of 
$$\int_{0}^{\pi} (\sin x + \cos x) dx$$

- (a) 1 ·
- (b) 2

(c) 0

(d)4

16. 
$$P$$
 is the amount of certain substance left in after time t. If the rate of evaporation of the substance is proportional to the amount remaining, then (where  $k > 0$ )

- (a)  $P = ce^{kt}$
- (b)  $P = ce^{-kt}$
- (c) P = ckt
- Pt = c(d)

17. The solution of the differential equation 
$$\frac{dy}{dx} = \frac{y}{x} + \frac{\phi\left(\frac{y}{x}\right)}{\phi'\left(\frac{y}{x}\right)}$$
 is

(a) 
$$x\phi\left(\frac{y}{x}\right) = k$$

(b) 
$$\phi\left(\frac{y}{x}\right) = kx$$

(a) 
$$x\phi\left(\frac{y}{x}\right) = k$$
 (b)  $\phi\left(\frac{y}{x}\right) = kx$  (c)  $y\phi\left(\frac{y}{x}\right) = k$ 

(d) 
$$\phi\left(\frac{y}{x}\right) = ky$$

18. A rod of length 21 is broken into two pieces at random. The probability density function of the shorter of the two pieces is

$$f(x) = \begin{cases} \frac{1}{l} & 0 < x < l \\ 0 & l \le x < 2l \end{cases}$$

The mean and variance of the shorter of the two pieces are respectively

- (a)  $\frac{l}{2}$ ,  $\frac{l^2}{2}$
- (b)  $\frac{l}{2}$ ,  $\frac{l^2}{6}$  (c) l,  $\frac{l^2}{12}$
- (d)  $\frac{l}{2}$ ,  $\frac{l^2}{12}$
- 19. If X is a binomial random variable with expected value 6 and variance 2.4, Then  $P\{X=5\}$  is
- (a)  $\binom{10}{5} \left(\frac{3}{5}\right)^6 \left(\frac{2}{5}\right)^4$  (b)  $\binom{10}{5} \left(\frac{3}{5}\right)^5$  (c)  $\binom{10}{5} \left(\frac{3}{5}\right)^4 \left(\frac{2}{5}\right)^6$  (d)  $\binom{10}{5} \left(\frac{3}{5}\right)^5 \left(\frac{2}{5}\right)^5$
- 20. The operation \* is defined by  $a*b = \frac{ab}{7}$ . It is it not a binary operation on
  - (a)  $\mathbb{Q}^+$

(d) C

## PART - II

Note: (i) Answer any SEVEN questions.

 $7\times2=14$ 

- (ii) Question number 30 is compulsory.
- 21. Prove that  $\begin{bmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{bmatrix}$  is orthogonal.
- 22. Find the modulus of  $\frac{1-i}{3+i} + \frac{4i}{5}$ .
- 23. Find the value of  $\tan^{-1} \left( \tan \left( -\frac{\pi}{6} \right) \right)$
- 24. Find the centre and radius of the circle  $3x^2 + 3y^2 12x + 6y 9 = 0$ .
- 25. Verify whether the line  $\frac{x-3}{-4} = \frac{y-4}{-7} = \frac{z+3}{12}$  lies in the plane 5x-y+z=8.
- 26. Evaluate:  $\int_{0}^{\log 2} e^{-|x|} dx$
- 27. Determine the order and degree (if exists) of the differential equation

$$\left(\frac{d^2y}{dx^2}\right)^2 + \left(\frac{dy}{dx}\right)^2 = x\sin\left(\frac{d^2y}{dx^2}\right).$$

28. Suppose a discrete random variable can only take the values 0, 1, and 2 The probability mass function is defined by 
$$f(x) = \begin{cases} \frac{x^2+1}{k}, & \text{for } x=0,1,2\\ 0, & \text{otherwise} \end{cases}$$
. Find the value of  $k$ .

29. Verify the associative property under the binary operation 
$$*$$
 defined by  $a*b=a^b, \forall a,b \in \mathbb{N}$ 

30. Evaluate 
$$\lim_{x\to 0} \frac{xe^x - \sin x}{x}$$

#### **PART-III**

Note:

(i) Answer any SEVEN questions.

 $7\times3=21$ 

- (ii) Question number 40 is compulsory.
- 31. Find the rank of the matrix by row reduction method:  $\begin{bmatrix} 1 & 1 & 1 & 3 \\ 2 & -1 & 3 & 4 \\ 5 & -1 & 7 & 11 \end{bmatrix}$
- 32. Show that the equation  $z^3 + 2\overline{z} = 0$  has five solutions.
- 33. Solve the equation  $x^3 5x^2 4x + 20 = 0$ .
- 34. If the equation  $3x^2 + (3-p)xy + qy^2 2px = 8pq$  represents a circle, find p and q. Also determine the centre and radius of the circle.
- 35. Find the points on the curve  $y = x^3 6x^2 + x + 3$  where the normal is parallel to the line x + y = 1729..

36. If 
$$u(x,y) = \frac{x^2 + y^2}{\sqrt{x + y}}$$
, prove that  $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} = \frac{3}{2}u$ .

- 37. Evaluate:  $\int_{0}^{1} \frac{2x}{1+x^2} dx$
- 38. Solve:  $\cos x \cos y \, dy \sin x \sin y \, dx = 0$
- 39. If  $\mu$  and  $\sigma^2$  are the mean and variance of the discrete random variable X, and E(X+3)=10 and  $E(X+3)^2=116$ , find  $\mu$  and  $\sigma^2$ .
- 40. If  $\vec{a}, \vec{b}, \vec{c}$  are three vectors prove that  $\left[\vec{a} + \vec{b}, \vec{b} + \vec{c}, \vec{c} + \vec{a}\right] = 2\left[\vec{a}, \vec{b}, \vec{c}\right]$

Note: Answer all the questions.

 $7 \times 5 = 35$ 

41. (a) Examine the consistency of the system of equations 4x+3y+6z=25, x+5y+7z=13, 2x+9y+z=1. If it is consistent then solve.

(OR)

(b) If z = x + iy and  $\arg\left(\frac{z - i}{z + 2}\right) = \frac{\pi}{4}$ , then show that  $x^2 + y^2 + 3x - 3y + 2 = 0$ .

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- (b) At a water fountain, water attains a maximum height of 4m at horizontal distance of 0.5 m from its origin. The flow is from the origin and the path of water is a parabola open upwards, find the height of water at a horizontal distance of 0.75m from the point of origin.
- 43. (a) If  $\vec{a} = \hat{i} \hat{j}$ ,  $\vec{b} = \hat{i} \hat{j} 4\hat{k}$ ,  $\vec{c} = 3\hat{j} \hat{k}$  and  $\vec{d} = 2\hat{i} + 5\hat{j} + \hat{k}$ , verify that  $(\vec{a} \times \vec{b}) \times (\vec{c} \times \vec{d}) = [\vec{a}, \vec{b}, \vec{d}]\vec{c} [\vec{a}, \vec{b}, \vec{c}]\vec{d}$

(OR)

- (b) Find the vector and Cartesian equations of the plane  $\vec{r} = (6\hat{i} \hat{j} + \hat{k}) + s(-\hat{i} + 2\hat{j} + \hat{k}) + t(-5\hat{i} 4\hat{j} 5\hat{k}).$
- 44. (a) A hollow cone with base radius a cm and height b cm is placed on a table. Show that the volume of the largest cylinder that can be hidden underneath is  $\frac{4}{9}$  times volume of the cone.

(OR)

- (b) Expand  $\log(1+x)$  as a Maclaurin's series upto 4 non-zero terms for  $-1 < x \le 1$ .
- 45. (a) If u = xyz,  $x = e^{-t}$ ,  $y = e^{-t} \sin t$ ,  $z = \sin t$  find  $\frac{du}{dt}$

(OR)

- (b) Solve:  $\left(y e^{\sin^{-1}x}\right) \frac{dx}{dy} + \sqrt{1 x^2} = 0$ .
- 46. (a) A multiple choice examination has ten questions, each question has four distractors with exactly one correct answer. Suppose a student answers by guessing and if X denotes the number of correct answers, find (i) binomial distribution (ii) probability that the student will get seven correct answers (iii) at least one correct answer.

(OR)

- (b) Show that  $p \leftrightarrow q \equiv (p \land q) \lor (\neg p \land \neg q)$ .
- 47. (a) Find the area enclosed by the curve  $y = -x^2$  and the straight line x + y + 2 = 0.

(OR)

(b) If  $\cos^{-1} x + \cos^{-1} y + \cos^{-1} z = \pi$  and 0 < x, y, z < 1, then show that  $x^2 + y^2 + z^2 + 2xyz = 1$ .

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### **MATHEMATICS**

## **MODEL QUESTION PAPER - 2**

Time Allowed: 15 Min + 3.00 Hours

[Maximum Marks:90

**Instructions:** 

- Check the question paper for fairness of printing. If there is any (a) lack of fairness, inform the Hall Supervisor immediately.
- Use Blue or Black ink to write and underline and pencil to draw (b) diagrams.

## <u>PART – I</u>

Note: (i) All questions are compulsory.  $20 \times 1 = 20$ 

1. If 
$$A = \begin{bmatrix} 7 & 3 \\ 4 & 2 \end{bmatrix}$$
, then  $9I - A = \begin{bmatrix} 7 & 3 \\ 4 & 2 \end{bmatrix}$ 

- (a)  $A^{-1}$
- (b)  $\frac{A^{-1}}{2}$
- (c)  $3A^{-1}$
- (d)  $2A^{-1}$

2. If 
$$A = \begin{bmatrix} 3 & -3 & 4 \\ 2 & -3 & 4 \\ 0 & -1 & 1 \end{bmatrix}$$
, then adj(adj A) is

(a) 
$$\begin{bmatrix} 3 & -3 & 4 \\ 2 & -3 & 4 \\ 0 & -1 & 1 \end{bmatrix}$$

(b) 
$$\begin{bmatrix} 6 & -6 & 8 \\ 4 & -6 & 8 \\ 0 & -2 & 2 \end{bmatrix}$$

(a) 
$$\begin{bmatrix} 3 & -3 & 4 \\ 2 & -3 & 4 \\ 0 & -1 & 1 \end{bmatrix}$$
 (b)  $\begin{bmatrix} 6 & -6 & 8 \\ 4 & -6 & 8 \\ 0 & -2 & 2 \end{bmatrix}$  (c)  $\begin{bmatrix} -3 & 3 & -4 \\ -2 & 3 & -4 \\ 0 & 1 & -1 \end{bmatrix}$  (d)  $\begin{bmatrix} 3 & -3 & 4 \\ 0 & -1 & 1 \\ 2 & -3 & 4 \end{bmatrix}$ 

3. The area of the triangle formed by the complex numbers z, iz and z+iz in the Argand's diagram is

- (a)  $\frac{1}{2}|z|^2$
- (b)  $|z|^2$
- (c)  $\frac{3}{2}|z|^2$

4. All complex numbers z which satisfy the equation  $\left| \frac{z-6i}{z+6i} \right| = 1$  lie on the

- (a) real axis
- (b) imginary axis
- (c) circle
- (d) ellipse

5. If  $\cot^{-1} 2$  and  $\cot^{-1} 3$  are two angles of a triangle, then the third angle is

- (b)  $\frac{3\pi}{4}$
- (c)  $\frac{\pi}{6}$
- (d)  $\frac{\pi}{2}$

6. The range of  $\sec^{-1} x$  is

- (a)  $[0,\pi] \setminus \left\{ \frac{\pi}{2} \right\}$  (b)  $[0,\pi]$
- (c)  $\left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$  (d)  $\left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$

7. P(x, y) be any point on  $16x^2 + 25y^2 = 400$  with foci  $F_1(3, 0)$  and  $F_2(-3, 0)$  then  $PF_1 + PF_2$ is

(a) 8

(b) 6

(c) 10

(d) 12

	locus of P is	eigents drawn from a point $P$ (b) $x = -1$		$= 4x \text{ are at } \text{ right}_{\text{max}}$ $(d) x = 1$	m:Net
	(a) $2x + 1 =$	$= 0 \qquad (0) \ x = -1$	(c) $2x = 1 = 0$	(a) x = 1	
	9. The locus of	the point whose distance fi	rom $(-2,0)$ is $-\frac{1}{3}$	imes its distance from the l	ine
	$x = -\frac{9}{2}$ is			· WWW.Padasaid	
	(a) a parabola				Met
10	0. The angle bet	ween the line $\vec{r} = (\hat{i} + 2\hat{j} - 3\hat{i})$	$(\hat{k}) + t(2\hat{i} + \hat{j} - 2\hat{k})$	and the plane $\vec{r} \cdot (\hat{i} + \hat{j}) + 4$	=0
	is (a) 0°	(b) 30°	(c) 45°	(d) 90°	
11		increase of the radius of a cirus is 20 cm, will be	rcle is 5 cm/sec, the	en the rate of increase of its	area
	(a) $10\pi$	(b) $20\pi$	(c) $200\pi$	(d) $400\pi$	
12	2Angle betwee	en $y^2 = x$ and $x^2 = y$ at the o	rigin is		
	(a) $\tan^{-1} \frac{3}{4}$	(b) $\tan^{-1}\left(\frac{4}{3}\right)$	(c) $\frac{\pi}{2}$	(d) $\frac{\pi}{4}$	
13	3. If $w(x, y) = x^3$	$\frac{\partial w}{\partial x}$ , $x > 0$ , then $\frac{\partial w}{\partial x}$ is equal to	Jassala	, Net	
	(a) $x^y \log x$	(b) $y \log x$	(c) $yx^{y-1}$	(d) $x \log y$	
14	$\int_{0}^{a} \frac{1}{4+x^2} dx = \frac{2}{8}$	$\frac{\tau}{8}$ then a is	i. NNN Pädasala	i.Nêt' 	Net
	(a) 4	(b) 1			
15.	. The area bour quadrant is	nded by the curve $y^2 = 4x$	and the lines $x =$	1, x = 4 and $x - axis$ in the	e first
	_	(b) $\frac{17}{3}$	(2) 28	$(d) \frac{31}{}$	Lake
	$(a) \frac{1}{3}$	$(6) \frac{1}{3}$	$\frac{(c)}{3}$	$\frac{(a)}{3}$	Ver
16.	. If the solution	of the differential equation	$\frac{dy}{dx} = \frac{ax+3}{2y+f} \text{ repres}$	sents a circle, then the value	of a is
	(a) 2	(b) −2	(c) 1	(d) -1	
17.	A random variof $X$ is	iable X has binomial distribu	ution with $n = 25$ a	p = 0.8 then standard de	viation
.P°	(a) 6	(b) 4	(c) 3	(d) 2	
18.	. Suppose that $\lambda$	takes on one of the values (	), 1, and 2. If for so	ome constant c,	kakt.
	P(X=i)=kI	P(X=i-1) for $i=1,2$ and $F$	$P(X=0) = \frac{1}{7}$ . Then	n the value of $k$ is	Mor
	(a) 1	(b) 2	(c) 3	(d) 4	Net
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- 19. Which one is the inverse of the statement  $(p \lor q) \to (p \land q)$ ?
  - (a)  $(p \land q) \rightarrow (p \lor q)$

(b)  $\neg (p \lor q) \rightarrow (p \land q)$ 

(c)  $(\neg p \lor \neg q) \rightarrow (\neg p \land \neg q)$ 

- (d)  $(\neg p \land \neg q) \rightarrow (\neg p \lor \neg q)$
- 20. Which one of the following statements has the truth value T?
  - (a)  $\sin x$  is an even function.
  - (b) Every square matrix is non-singular
  - (c) The product of complex number and its conjugate is purely imaginary
  - (d)  $\sqrt{5}$  is an irrational number

#### PART - II

Note: (i) Answer any SEVEN questions.

 $7\times2=14$ 

- (ii) Question number 30 is compulsory.
- 21. Find  $z^{-1}$ , if z = (2+3i)(1-i)
- 22. Find the square root of -6+8i
- 23. Find the principal value of  $\csc^{-1}(-\sqrt{2})$
- 24. Find the equation of the parabola whose end points of the latus rectum are (4,-8) and (4,8), centre is (0,0) and open rightward.
- 25. A particle is fired straight up from the ground to reach a height of s feet in t seconds, when  $s = 128t 16t^2$ . Compute the maximum height of the particle reached?
- 26. If  $f(x,y) = x^3 3x^2 + y^2 + 5x + 6$ , then find  $f_x$  at (1,-2)
- 27. Find the differential equation of the curve represented by  $xy = ae^x + be^{-x} + x^2$ .
- 28. Establish the equivalence property:  $p \rightarrow q \equiv \neg p \lor q$
- 29. Let \* be defined on  $\mathbb{R}$  by a\*b=a+b+ab-7. Is \*binary on  $\mathbb{R}$ .
- 30. Evaluate:  $\int_{0}^{\frac{\pi}{2}} \frac{\sin x}{1 + \cos^2 x} dx$

#### PART-III

Note:

- (i) Answer any SEVEN questions.
- (ii) Question number 40 is compulsory.
- 31. Find the value of  $\sum_{k=1}^{8} \left( \cos \frac{2k\pi}{9} + i \sin \frac{2k\pi}{9} \right).$

 $7 \times 3 = 21$ 

32. Show that the equation  $x^9 - 5x^5 + 4x^4 + 2x^2 + 1 = 0$  has at least 6 imaginary solutions.

33. Prove that the length of the latus rectum of the hyperbola  $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$  is  $\frac{2b^2 vww.Padasalai.Net}{a}$ .

34. Find the altitude of a parallelepiped determined by the vectors  $\vec{a} = -2i + 5j + 3k$ ,  $\vec{b} = i + 3j - 2k$  and  $\vec{c} = -3i + j + 4k$  if the base is taken as the parallelogram determined by  $\vec{b}$  and  $\vec{c}$ .

35. Examine the concavity for the function  $f(x) = x^4 - 4x^3$ .

36. Show that the value in the conclusion of the mean value theorem for  $f(x) = Ax^2 + Bx + C$  on any interval [a,b] is  $\frac{a+b}{2}$ .

37. Evaluate:  $\int_{0}^{\frac{\pi}{2}} (\sin^2 x + \cos^4 x) dx$ .

38. Assume that a spherical rain drop evaporates at a rate proportional to its surface area. Form a differential equation involving the rate of change of the radius of the rain drop.

39. The probability distribution of a random variable is given below

X = x	0	Lasalai	2	3	4	5	6	7
P(X=x)	0	k	2k	2k	3k	$k^2$	2 k <sup>2</sup>	$7k^2+k$

Then find P(0 < X < 4).

40. If  $A = \begin{bmatrix} 3 & -2 \\ \lambda & -2 \end{bmatrix}$ , find the value of  $\lambda$  so that  $A^2 = \lambda A - 2I$ .

### PART - IV

Note: Answer all the questions.

 $7\times5=35$ 

41. (a) Investigate for what values of  $\lambda$  and  $\mu$  the system of linear equations x+2y+z=7,  $x+y+\lambda z=\mu$ , x+3y-5z=5 has (i) no solution (ii) a unique solution

Approximate the second section of the second

(OR)

(b) Find the sum of squares of the roots of the equation  $2x^4 - 8x^3 + 6x^2 - 3 = 0$ .

42. (a) Evaluate: 
$$\sin\left(\sin^{-1}\left(\frac{3}{5}\right) + \sec^{-1}\left(\frac{5}{4}\right)\right)$$

(OR)

(b) Find the foci and vertices of the hyperbola  $4x^2 - 24x - 25y^2 + 250y - 489 = 0$ .

43. (a) Find the vector and cartesian equations of the plane passing through the point (1,-2,4) and

perpendicular to the plane x+2y-3z=11 and parallel to the line  $\frac{x+7}{3}=\frac{y+3}{-1}=\frac{z}{1}$ .

- (b) Find the foot of the perpendicular drawn from the point (5,4,2) to the line  $\frac{x+1}{2} = \frac{y-3}{3} = \frac{z-1}{-1}$ . Also, find the equation of the perpendicular.
- 44. (a) Find intervals of concavity and points of inflexion for the function

$$f(x) = \frac{1}{2}(e^x - e^{-x})$$

(OR)

- (b) Evaluate:  $\int_{0}^{2a} x^2 \sqrt{2ax x^2} dx$
- 45. (a) Find the area of the region bounded between the parabola  $x^2 = y$  and the curve y = |x|. (OR)
  - (b) The equation of electromotive force for an electric circuit containing resistance and self-inductance is  $E = Ri + L\frac{di}{dt}$ , where E is the electromotive force given to the circuit, R the resistance and L, the coefficient of induction. Find the current i at time t when E = 0.
- 46. (a) The probability density function of X is given by  $f(x) = \begin{cases} ke^{-\frac{x}{3}} & \text{for } x > 0 \\ 0 & \text{for } x \le 0 \end{cases}$

Find (i) the value of k (ii) P(X < 3).

(OR)

- (b) Verify whether the compound proposition  $(p \rightarrow q) \leftrightarrow (\neg p \rightarrow q)$  is a tautology or contradiction or contingency
- 47. (a) Solve  $z^4 = 1 \sqrt{3}i$

(OR)

(b) If 
$$f(x,y) = \log \sqrt{x^2 + y^2}$$
, show that  $\frac{\partial^2 f}{\partial x^2} + \frac{\partial^2 f}{\partial y^2} = 0$ 

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## **MATHEMATICS**

HIGHER SECONDARY SECOND YEAR

## **MODEL QUESTION PAPER - 3**

Time Allowed: 15 Min + 3.00 Hours

[Maximum Marks:90

Instructions:

- Check the question paper for fairness of printing. If there is any (a) lack of fairness, inform the Hall Supervisor immediately.
- (b) Use Blue or Black ink to write and underline and pencil to draw diagrams.

### PART – I

Note:

(i) All questions are compulsory.

 $20 \times 1 = 20$ 

- (ii) Choose the correct or most suitable answer from the given four alternatives. Write the option code and the corresponding answer.
- 1. If  $A = \begin{vmatrix} 1 & \tan \frac{\theta}{2} \\ -\tan \frac{\theta}{2} & 1 \end{vmatrix}$  and AB = I, then B = I
  - (a)  $\left(\cos^2\frac{\theta}{2}\right)A$  (b)  $\left(\cos^2\frac{\theta}{2}\right)A^T$  (c)  $(\cos^2\theta)I$  (d)  $\left(\sin^2\frac{\theta}{2}\right)A$

- 2. If  $x^a y^b = e^m, x^c y^d = e^n, \Delta_1 = \begin{vmatrix} m & b \\ n & d \end{vmatrix}, \Delta_2 = \begin{vmatrix} a & m \\ c & n \end{vmatrix}, \Delta_3 = \begin{vmatrix} a & b \\ c & d \end{vmatrix}$ , then the values of x and y are respectively,

  - (a)  $e^{(\Delta_2/\Delta_1)}$ ,  $e^{(\Delta_3/\Delta_1)}$  (b)  $\log(\Delta_1/\Delta_3)$ ,  $\log(\Delta_2/\Delta_3)$
  - (c)  $\log(\Delta_2/\Delta_1), \log(\Delta_2/\Delta_1)$
- (d))  $e^{(\Delta_1/\Delta_3)}$ ,  $e^{(\Delta_2/\Delta_3)}$
- 3. If z = x + iy is a complex number such that |z + 2| = |z 2| then the locus of z is
  - (a) real axis
    - (b) imaginary axis
- (c) ellipse
- (d) circle
- 4. The principal argument of the complex number  $\frac{\left(1+i\sqrt{3}\right)^2}{4i\left(1-i\sqrt{3}\right)}$  is
  - (a)  $\frac{2\pi}{2}$

 $(c)\frac{5\pi}{6}$ 

- 5. The polynomial equation  $x^3 + 2x + 3 = 0$  has
  - (a) one negative and two real roots
- (b) one positive and two imaginary roots

(c) three real roots

(d) no solution

-1(1)	_1(2) .		www.Padasalai.Net	
6. $\tan^{-1}\left(\frac{-4}{4}\right) + \tan^{-1}\left(\frac{-4}{4}\right)$	$n^{-1}\left(\frac{2}{9}\right)$ is equal to	mum Padasalai Net	mum Padasalai Net	
(a) $\frac{1}{2}\cos^{-1}\left(\frac{3}{5}\right)$	$\text{(b) } \frac{1}{2}\sin^{-1}\left(\frac{3}{5}\right)$	(c) $\frac{1}{2} \tan^{-1} \left( \frac{3}{5} \right)$	(d) $\tan^{-1}\left(\frac{1}{2}\right)$	
7. The vertex of	the parabola $x^2 = 8y -$	1 is	AWWW.Padasaran.	W
(a) $\left(-\frac{1}{8},0\right)$	(b) $\left(\frac{1}{8},0\right)$	(c) $\left(-6, \frac{9}{2}\right)$	$(d)\left(\frac{9}{2},-6\right)$	VOOK
8. Area of the gre	eatest rectangle inscribe	d in the ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$	lis	
(a) 2 <i>ab</i>	(b) <i>ab</i>	(c) $\sqrt{ab}$	(d) $\frac{a}{b}$	
9. If $\vec{a} = \hat{i} + \hat{j} + \hat{k}$	$(\hat{k}, \vec{b} = \hat{i} + \hat{j}, \vec{c} = \hat{i})$ and	$(\vec{a} \times \vec{b}) \times \vec{c} = \lambda \vec{a} + \mu \vec{b}$ , then	the value of $\lambda + \mu$ is	
	(b) 1 of the point $(1,1,1)$ nen the values of $k$ are		(d) 3 of its distance from the pla	ine
(a) $\pm 3$	(b) $\pm 6$	(c) - 3, 9	(d) 3, -9	
11. If $x + y = k$ is	a normal to the parabol	a $y^2 = 16x$ , then the value	of $k$ is	
(a) 3	(b) 6	(c) 12	(d) 15	
12. The number giv		heorem for the function $\frac{1}{r}$ ,		
(a) 2	(b) 2.5	(c) 3	(d) 3.5	
13. If $f(x) = \frac{x-1}{x+1}$	, then its differential is	given by	www.	
$(a) \frac{2}{\left(x+1\right)^2} dx$	$(b) -\frac{2}{\left(x+1\right)^2} dx$	$(c) \frac{x}{\left(x+1\right)^2} dx$	$(d) \frac{-x}{\left(x+1\right)^2} dx$	
14. If $\int_{0}^{x} f(t)dt = x$	$t + \int_{x}^{1} tf(t)dt$ , then the	value of $f(1)$ is	WWW.Padasalal.Net	
(a) $\frac{1}{2}$	(b) 2	(c) 1	(d) $\frac{3}{4}$	

(c) 4

(d) 5

14.

(a) 0

15. The value of  $\int_{0}^{1} \log \left( \frac{x}{1-x} \right) dx$ 

(b) 2

(a) $\left(\frac{1}{5}\right)$	,25)	(b) $\left(25, \frac{1}{5}\right)$	(c) $\left(25,\right)$	$\left(\frac{4}{5}\right)$	(d) $\left(\frac{4}{5}, 25\right)$	
1.1	obability fundaria	etion of a random $\frac{1}{0}$	1001	2	www.Padasa	lal Net
Posaasa ar	(x) $k$	2k $3k$	4 <i>k</i>	5 <i>k</i>	www.padasa	lal Net
(a) $\frac{1}{15}$		(b) $\frac{1}{10}$	(c) $\frac{1}{3}$	<sub>Jasalal</sub> Net	(d) $\frac{2}{3}$	
20. Which	one is the inv	erse of the stateme				
(a) $(p)$	$\wedge q) \rightarrow (p \vee q)$	) aaaalai.Net	• • •	$\vee q) \rightarrow (p \wedge q)$	· 0444688	
(c) (¬p	$p \lor \neg q) \rightarrow (\neg p)$	$p \wedge \neg q)$		$\wedge \neg q) \rightarrow (\neg p \vee \neg q)$	¬q)	
			*	· · · · · · · · · · · · · · · · · · ·		70 14
Note: (i) An	swer any SEV	EN questions.	Par		www.Padasa	$7\times2=14$
(ii) Que	estion numbe	r 30 is compulsor	<b>y</b> .			. Nakt
21. Show the	$\cot\left(2+i\sqrt{3}\right)$	$+(2-i\sqrt{3})^{10}$ is	real	Jasalai.Nei	www.Padasa	lativer w
22. Find the	e value of sin	$n^{-1}\left(\sin\left(\frac{5\pi}{4}\right)\right)$	www.Pad	jasalai:Net r	www.Padasa	ial Met
		of the circle for wh				
24. Find the	intercepts cu	it off by the plane	$\vec{r} \cdot (6\hat{i} + 4\hat{j} -$	$3\hat{k}$ )=12 on the	coordinate axes.	
25. For the	function $f(x)$	$(x) = x^4 - 2x^2$ , find	all the values	s of $c$ in $(-2, 1)$	2) such that $f'($	(c)=0
26. Evaluate	$e: \int_{0}^{\frac{\pi}{2}} \sin^{10} x dt$	x Jadasalai Net	www.Pac	jasalsi.Net	www.padasa	lalatek :
	det •	Padasalal Net		jasalai.Net		lal Net

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16. The degree of the differential equation  $y(x) = 1 + \frac{dy}{dx} + \frac{1}{1 \cdot 2} \left(\frac{dy}{dx}\right)^2 + \frac{1}{1 \cdot 2 \cdot 3} \left(\frac{dy}{dx}\right)^2 + \frac{1}{1 \cdot$ 

3

(b)  $P = ce^{-kt}$ 

(b)

to the population. Then (k > 0)

(a) 2

(a)  $P = ce^{kt}$ 

(c) 1

(c) P = ckt

17. The population P in any year t is such that the rate of increase in the population is proportional

18. If the mean of a binomial distribution is 5 and its variance is 4, then the value of n and p are

(d) 4

(d) P = c

- 27 Show that the differential equation for the function  $y = e^{-x} + mx + n$ , where m and n are arbitrary constants is  $e^{x} \left( \frac{d^{2}y}{dx^{2}} \right) 1 = 0$ .
- 28. Find the mean of the distribution  $f(x) = \begin{cases} 3e^{-3x}, & 0 < x < \infty \\ 0, & elsewhere \end{cases}$
- 29. On  $\mathbb{Z}$ , define  $\otimes$  by  $(m \otimes n) = m^n + n^m : \forall m, n \in \mathbb{Z}$ . Is  $\otimes$  binary on  $\mathbb{Z}$ ?
- 30. If  $A = \begin{bmatrix} 2 & 3 \\ 1 & 2 \end{bmatrix}$ ,  $B = \begin{bmatrix} 4 & 0 \\ 2 & 5 \end{bmatrix}$ , find adj(AB).

#### **PART-III**

 $7 \times 3 = 21$ 

Note:

- (i) Answer any SEVEN questions.
- (ii) Question number 40 is compulsory.
- 31. Solve the following system of linear equations by matrix inversion method 2x-y=8; 3x+2y=-2
- 32. Find the value of  $\frac{\cos\frac{\pi}{6} + i\sin\frac{\pi}{6}}{\cos\frac{\pi}{3} i\sin\frac{\pi}{3}}.$
- 33. Find the equation of the hyperbola with foci  $(\pm 3,5)$  and eccentricity e=2.
- 34. Find the cartesian equation of the plane passing through the line of intersection of the planes  $\vec{r} \cdot (2\hat{i} 7\hat{j} + 4\hat{k}) = 3$  and 3x 5y + 4z + 11 = 0, and the point (-2,1,3).
- 35. Prove that the function  $f(x) = x \sin x$  is increasing but not strictly on the real line. Also discuss for the existence of local extrema.
- 36. If  $U = \log(x^3 + y^3 + z^3)$ , find  $\frac{\partial U}{\partial x} + \frac{\partial U}{\partial y} + \frac{\partial U}{\partial z}$ .
- 37. Evaluate:  $\int_{0}^{\pi} x^{2} \cos nx dx$ , where *n* is a positive integer.
- 38. Solve:  $\frac{dy}{dx} = e^{x+y} + x^2 e^{x^3+y}$
- 39. The mean and variance of a binomial variate X are respectively 2 and 1.5. Find P(X=0).
- 40. Find the magnitude and direction cosines of the moment about the point (0,-2,3) of a force  $\hat{i}+\hat{j}+\hat{k}$  whose line of action passes through the origin.

Note: Answer all the questions.

- 41. (a) If  $ax^2 + bx + c$  is divided by x+3, x-5 and x-1, the remainders are 21,61 and 9 respectively. Find a, b and c. (OR)
  - (b) Simplify:  $\left(-\sqrt{3}+3i\right)^{31}$
- 42. (a) Solve the equation  $x^4 10x^3 + 26x^2 10x + 1 = 0$ . (OR)
  - (b) Solve for  $x : \tan^{-1} x + 2 \cot^{-1} x = \frac{2\pi}{3}$
- 43. (a) For the ellipse  $4x^2 + y^2 + 24x 2y + 21 = 0$ , find the centre, vertices, foci and the length of latus rectum. (OR)
  - (b) By vector method, prove that  $\cos(\alpha + \beta) = \cos \alpha \cos \beta \sin \alpha \sin \beta$ .
- 44 (a) Find the absolute extrema of the function  $f(x) = 3x^4 4x^3$  on the interval [-1,2].

(OR)

- (b) For the function  $f(x, y) = \frac{3x}{y + \sin x}$ , find  $f_x, f_y$ , and show that  $f_{xy} = f_{yx}$ .
- 45 (a) Using integration find the area of the region bounded by triangle ABC, whose vertices A, B, and C are (-1,1), (3, 2), and (0,5) respectively.

(OR)

- (b) Solve:  $y^2 x^2 \frac{dy}{dx} = xy \frac{dy}{dx}$
- 46. (a) The cumulative distribution function of a discrete random variable is given by

$$F(x) = \begin{cases} 0 & -\infty < x < -1 \\ 0.15 & -1 \le x < 0 \\ 0.35 & 0 \le x < 1 \\ 0.60 & 1 \le x < 2 \\ 0.85 & 2 \le x < 3 \\ 1 & 3 \le x < \infty \end{cases}$$

Find (i) the probability mass function (ii) P(X < 1) and (iii)  $P(X \ge 2)$  (OR)

- (b) Using truth table check whether the statements  $\neg (p \lor q) \lor (\neg p \land q)$  and  $\neg p$  are logically equivalent.
- 47. (a) Find the shortest distance between the straight lines  $\frac{x-6}{1} = \frac{2-y}{2} = \frac{z-2}{2}$  and  $\frac{x+4}{3} = \frac{y}{2} = \frac{1-z}{2}$ . (OR)
  - (b) Prove that among all the rectangles of the given area square has the least perimeter.

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## **MATHEMATICS**

## **MODEL QUESTION PAPER - 4**

Time Allowed: 15 Min + 3.00 Hours]

[Maximum Marks:90

**Instructions:** 

- Check the question paper for fairness of printing. If there is any (a) lack of fairness, inform the Hall Supervisor immediately.
- Use Blue or Black ink to write and underline and pencil to draw (b) diagrams.

## PART - I

Note:

(i) All questions are compulsory.

 $20 \times 1 = 20$ 

- (ii) Choose the correct or most suitable answer from the given four alternatives. Write the option code and the corresponding answer.
- 1. The adjoint of  $3\times 3$  matrix P is  $\begin{vmatrix} -1 & 2 & 2 \\ 1 & 1 & 2 \\ 2 & 2 & 1 \end{vmatrix}$ , then the possible value(s) of the determinant P is

(are)

(a) 3

(b) -3 (c)  $\pm 3$  (d)  $\pm \sqrt{3}$ 2. If  $x = \frac{-1 + i\sqrt{3}}{2}$  then the value of  $x^2 + x + 1$ 

(b)  $\frac{1}{2}$  (c) 0 (d) 1

3. The value of  $\left(\frac{1+\sqrt{3}i}{1-\sqrt{3}i}\right)^{10}$  is

(a)  $cis \frac{2\pi}{3}$  (b)  $cis \frac{4\pi}{3}$  (c)  $-cis \frac{2\pi}{3}$ 

(d)  $-cis\frac{4\pi}{3}$ 

- 4. A polynomial equation in x of degree n always has
  - (a) *n* distinct roots
- (b) *n* real roots (c) *n* imaginary roots
- (d) atmost one root

5.  $\sin^{-1}(\cos x) = \frac{\pi}{2} - x$  is valid for

(a)  $-\pi \le x \le 0$  (b)  $0 \le x \le \pi$  (c)  $-\frac{\pi}{2} \le x \le \frac{\pi}{2}$  (d)  $-\frac{\pi}{4} \le x \le \frac{3\pi}{4}$ 

6. If  $\cot^{-1}(\sqrt{\sin \alpha}) + \tan^{-1}(\sqrt{\sin \alpha}) = u$ , then  $\cos 2u$  is equal to

(a)  $\tan^2 \alpha$ 

(d)  $\tan 2\alpha$ 

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7. The locus of a	point whose distance from	$(-2,0)$ is $\frac{2}{}$ times i	www.Padasalai.Net
$x = -\frac{9}{2}$ is	WWW.Padacalal.Net	3asalal	WWW.Padasalai.Ne.
(a) a parabola 8. If $P(x, y)$ be	(b) a hyperbola any point on $4x^2 + 9y^2 =$		(d) a circle he distances of P from the points
$(\sqrt{5},0)$ and $(-$			
(a) 4 9. If the plane x-	(b) 8 + $\alpha y + z - 8 = 0$ has equal	(c) 6 intercepts on the coor	(d) 18 rdinate axes, the value of $\alpha$ is
(a) 1	(b) 2	(c) 8	(d) $\frac{1}{8}$
10. If the planes $\vec{r}$	$\cdot (2\hat{i} - \lambda \hat{j} + \hat{k}) = 3$ and $\vec{r} \cdot ($	$(4\hat{i}+\hat{j}-\mu\hat{k})=5$ are	parallel, then the value of $\lambda$ and
$\mu \text{ are}$ (a) $\frac{1}{2}$ , -2	(b) $-\frac{1}{2}$ ,2	(c) $-\frac{1}{2}$ , $-2$	(d) $\frac{1}{2}$ ,2
	of a particle moving ale-8. For what values of $t$		ne of any time $t$ is given by ving?
(a) 0	(b) $\frac{1}{3}$	(c) 1	(d) 3
12. The minimum v	value of the function $ 3-3 $	x  + 9 is	Net : Padasalal Net
(a) 0	(b) 3	(c) 6	(d) 9
13. The abscissa of	the point on the curve	$f(x) = \sqrt{8 - 2x} \text{ at y}$	(d) 9 which the slope of the tangent is
-0.25 ? (a) $-8$	(b) -4	(c) -2	(d) 0
4. If $f(x) = \frac{x}{x+1}$ ,	then its differential is give	en by	Mind Area and Met
$(a) \frac{-1}{(x+1)^2} dx$	(b) $\frac{1}{(x+1)^2} dx$	(c) $\frac{1}{x+1} dx$	$(d) \frac{-1}{x+1} dx$
5. The solution of	the differential equation	$\frac{dy}{dx} + \frac{1}{\sqrt{1 - x^2}} = 0 \text{ is}$	Nev WWW.Padasalal.Nev
	a1 -		

(a)  $y + \sin^{-1} x = c$  (b)  $x + \sin^{-1} y = 0$  (c)  $y^2 + 2\sin^{-1} x = c$  (d)  $x^2 + 2\sin^{-1} y = 0$ 

16. The differential equation of the family of curves  $y = Ae^x + Be^{-x}$ , where A and B are arbitrary constants is

(a)  $\frac{d^2y}{dx^2} + y = 0$  (b)  $\frac{d^2y}{dx^2} - y = 0$  (c)  $\frac{dy}{dx} + y = 0$  (d)  $\frac{dy}{dx} - y = 0$ 

17. The solution of the differential equation  $\frac{dy}{dx} = e^x + 2$  is

12.

13.

14.

(a)  $y = e^x + C$  (b)  $y = 2x + e^x + C$  (c)  $y = 2xe^x + C$  (d)  $y = e^x + 2Cx$ 

18. The random variable X has the probability density function

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The random variable X has the proof 
$$f(x) = \begin{cases} ax + b & 0 < x < 1 \\ 0 & \text{otherwise} \end{cases}$$
 and  $E(X) = \frac{7}{12}$ , then a and b are respectively

- (a) 1 and  $\frac{1}{2}$
- (b)  $\frac{1}{2}$  and 1
- (c) 2 and 1
- (d) 1 and 2
- 19. In the set  $\mathbb{R}$  of real numbers '\*' is defined as follows. Which one of the following is not a binary operation on  $\mathbb{R}$ ?
  - (a)  $a*b = \min(a,b)$

(b)  $a*b = \max(a,b)$ 

(c) a\*b=a

- (d)  $a*b=a^b$
- 20. If  $a*b = \sqrt{a^2 + b^2}$  on the real numbers then \* is
  - (a) commutative but not associative
- (b) associative but not commutative
- (c) both commutative and associative
- (d) neither commutative nor associative

#### PART - II

Note: (i) Answer any SEVEN questions.

 $7 \times 2 = 14$ 

- (ii) Question number 30 is compulsory.
- 21. If A is a non-singular matrix of odd order, prove that |adj(A)| is positive.
- 22. Write the principal value of  $\tan^{-1} \left[ \sin \left( -\frac{\pi}{2} \right) \right]$
- 23. Identify the type of the conic  $y^2 + 4x + 3y + 4 = 0$
- 24. Find the foci of  $9x^2 16y^2 = 144$ .
- 25. Find the angle between the lines 2x = 3y = -z and 6x = -y = -4z.
- 26. Find the intervals of monotonicity for the function  $f(x) = x^2 4x + 4$ .
- 27. Evaluate:  $\int_{0}^{1} \frac{\left(\sin^{-1} x\right)^{2}}{\sqrt{1-x^{2}}} dx$
- 28. Find the order and degree (if exists) of the differential equation  $y\left(\frac{dy}{dx}\right) = \frac{x}{\left(\frac{dy}{dx}\right) + \left(\frac{dy}{dx}\right)}$ .
- 29. If X is the random variable with distribution function F(x) given by,

$$F(x) = \begin{cases} 0, & x < 0 \\ \frac{1}{2}(x^2 + x) & 0 \le x < 1 \text{ then find the probability density function } f(x) \\ 1, & x \ge 1 \end{cases}$$

30. If  $\omega \neq 1$  is a cubic root of unity and  $(1+\omega)^7 = A + B\omega$ , then find A and B.

#### PART-III

Note:

- (i) Answer any SEVEN questions.
- (ii) Question number 40 is compulsory.
- 31. Find the rank of the matrix  $\begin{bmatrix} 4 & -2 & 6 & 8 \\ 1 & 1 & -3 & -1 \\ 15 & -3 & 9 & 21 \end{bmatrix}$ .
- 32. If  $\alpha$  and  $\beta$  are the roots of the quadratic equation  $2x^2 7x + 13 = 0$ , construct a quadratic equation whose roots are  $\alpha^2$  and  $\beta^2$ .
- 33. The line 3x+4y-12=0 meets the coordinate axes at A and B. Find the equation of the circle drawn on AB as diameter
- 34. Find the magnitude and direction cosines of the torque of a force represented by 3i+4j-5k about the point with position vector 2i-3j+4k acting through a point whose position vector is 4i+2j-3k.
- 35. Find the local extrema for the function  $f(x) = x^2 e^{-2x}$  using second derivative test.
- 36. A circular plate expands uniformly under the influence of heat. If it's radius increases from 10.5 cm to 10.75 cm, then find an approximate change in the area and the approximate percentage change in the area.
- 37. If  $u = e^{2(x-y)}$ , prove that  $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} = u \log u$ .
- 38. Evaluate  $\int_{0}^{2\pi} x \log \left( \frac{3 + \cos x}{3 \cos x} \right) dx$  using properties of integration.
- 39. Show that (i)  $p \lor (\neg p)$  is a tautology (ii)  $p \land (\neg p)$  is a contradiction.
- 40. The population of a city grows at the rate of 5 % per year. Calculate the time taken for the population doubles. [ Given  $\log 2 = 0.6912$  ]

## PART - IV

Note: Answer all the questions.

 $7 \times 5 = 35$ 

- 41. (a) Determine the values of  $\lambda$  for which the following system of equations  $x+y+3z=0; 4x+3y+\lambda z=0; 2x+y+2z=0$  has
  - (i) a unique solution (ii) a non-trivial solution.

(OR)

- (b) If  $\cos\alpha + \cos\beta + \cos\gamma = \sin\alpha + \sin\beta + \sin\gamma = 0$  then show that
  - (i)  $\cos 3\alpha + \cos 3\beta + \cos 3\gamma = 3\cos(\alpha + \beta + \gamma)$  and
  - (ii)  $\sin 3\alpha + \sin 3\beta + \sin 3\gamma = 3\sin(\alpha + \beta + \gamma)$
- 42. (a) Solve the equation  $z^3 + 8i = 0$ , where  $z \in \mathbb{C}$ . (OR)
- (b) Draw the curve  $\sin x$  in the domain  $\left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$  and  $\sin^{-1} x$  in [-1,1].

43. (a) The eccentricity of an ellipse with its centre at the origin is  $\frac{1}{2}$ . If one of the directrix is x = 4, then find the equation of the ellipse.

(OR)

- (b) If the straight lines  $\frac{x-1}{2} = \frac{y+1}{\lambda} = \frac{z}{2}$  and  $\frac{x+1}{5} = \frac{y+1}{2} = \frac{z}{\lambda}$  are coplanar, find  $\lambda$  and cartesian equations of the planes containing these two lines.
- 44. (a) Find the angle between  $y = x^2$  and  $y = (x-3)^2$ .

(OR)

- (b) Let  $w(x, y, z) = \frac{1}{\sqrt{x^2 + y^2 + z^2}}$ ,  $(x, y, z) \neq (0, 0, 0)$ . Show that  $\frac{\partial^2 w}{\partial x^2} + \frac{\partial^2 w}{\partial y^2} + \frac{\partial^2 w}{\partial z^2} = 0$ .
- 45. (a) Using integration, find the area of the region bounded by the triangle whose vertices are (-1,2),(1,5) and (3,4).

(OR)

- (b) Solve:  $(1+2e^{x/y})dx + 2e^{x/y}\left(1-\frac{x}{y}\right)dy = 0$ .
- 46. (a) The probability density function of X is given by  $f(x) = \begin{cases} 16xe^{-4x} & \text{for } x > 0 \\ 0 & \text{for } x \le 0 \end{cases}$  Find the mean and variance of X.

(b) Verify (i) closure property (ii) associative property (iii) existence of identity

(iv) existence of inverse and (v) commutative property for the operation  $+_5$  on  $\mathbb{Z}_5$  using table corresponding to addition modulo 5.

47. (a) If 
$$\vec{a} = \hat{i} + \hat{j} - \hat{k}$$
,  $\vec{b} = 2\hat{i} + 3\hat{j}$  and  $\vec{c} = \hat{j} - \hat{k}$ , verify that  $\vec{a} \times (\vec{b} \times \vec{c}) = (\vec{a} \cdot \vec{c})\vec{b} - (\vec{a} \cdot \vec{b})\vec{c}$ 

(OR)

(b) Evaluate: 
$$\int_{0}^{\frac{\pi}{2}} \frac{dx}{4\sin^2 x + 5\cos^2 x}.$$

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## **MATHEMATICS**

## **MODEL QUESTION PAPER - 5**

Time Allowed: 1	[5 Min + 3.00 Hours]	·	[Max	imum Marks:90
Instructions:	(a) Check the questi	on paper for fair	ness of printing. If ther	e is any
	lack of fairness,	inform the Hall S	Supervisor immediately	7.
	(b) Use Blue or Blac	ck ink to write ar	nd underline and penci	to draw
	diagrams.		AMMA.	4
	. Nebt	PART – I		
Note: (i) All q	uestions are compulsory.	www.Padas	salar.Nor.	$20\times1=20$
	ose the correct or most suita		the given four alter	natives. Write the
optio	n code and the corresponding	g answer.	salai Net .	padasalai Net
	WWW.	PART – I	1	
1. If $A$ is a	$3\times3$ matrix such that $ 3adjA $	=3 then $ A $ is	equal to	· nuNdet
adasalalin	www.Padasalah	www.hadas	(1)	
(a) $\frac{1}{3}$	(b) $-\frac{1}{3}$	(c) $\pm \frac{1}{3}$	(d) $\pm 3$	
Г3	$\begin{bmatrix} a_{11} & a_{12} \end{bmatrix}$	$a_{13}$	salai Net .	sariasalal Net
2. If $A = 2$	$-2   0   and   A^{-1} =  a_{21}   a_{22}$	$a_{23}$ then the	value of $a_{23}$ is	
_1	$\begin{bmatrix} 1 & -1 \\ -2 & 0 \\ 2 & -1 \end{bmatrix} \text{ and } A^{-1} = \begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \\ a_{31} & a_{32} \end{bmatrix}$	$a_{33}$	operation of the second se	- i Naht
(a) 0	(b) $-2$	. (c) -3	(d) −1	Sadasalal.Ne
3. $z_1, z_2$ and	$z_3$ be complex numbers	such that $z_1$	$-z_2 + z_3 = 0$ and $ z_1 $	$= z_2 = z_3 =1$ ther
$z_1^2 + z_2^2 +$	-2 in managedal Net	Pada		adasalal.Net
	(b) 2		(d) 0	
(a) 3		77 70 18 1500		- Jaan Net
4. The value	of $i^{201} + i^{202} + i^{203}$ is	WWW.Padas	salari	
(a) 1	(b) <i>i</i>		(d) -1	
5. If $\frac{z-1}{z-1}$ is	s purely imaginary, then $ z $	is	ald Net	adasalai Net
z+1	, parer,g,  -		•	
(1)	<b>(L)</b> 1	(a) 2 (b) 2	(d) 3	- In LINGE
(a) $\frac{1}{2}$	(b) 1	(c) 2	(u) 3	padasalah
6. If $f$ and $g$	g are polynomials of degre	es <i>m</i> and <i>n</i> resi	pectively, and if $h(x)$	$=(f \circ g)(x)$ the
the decree		n=da8	salal:Net	, ( 3)(), 410

7. If $\sin^{-1}\frac{x}{5} + \csc \theta$	$e^{-1}\frac{5}{4} = \frac{\pi}{2}$ , then the va	alue of $x$ is	www.Padasalai.Net
(a) 4	(b) 5	(c) 2	(d) 3
* * \\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\	parabola $y^2 - 2y + 8$	UVILLAMA ET OGGE	
		(c) $x = 3$	(d) $y=1$
	of the hyperbola who	ose latus rectum is 8 and co	onjugate axis is equal to half
(a) $\frac{4}{3}$	(b) $\frac{4}{\sqrt{3}}$	(c) $\frac{2}{\sqrt{3}}$	(d) $\frac{3}{2}$
10. If the volume of	the parallelepiped v	with $\vec{a} \times \vec{b}, \vec{b} \times \vec{c}, \vec{c} \times \vec{a}$ as	coterminous edges is 8 cubic
units, then the	volume of the par	allelepiped with $(\vec{a} \times \vec{b})$	$\langle (\vec{b}  imes \vec{c}), (\vec{b}  imes \vec{c})  imes (\vec{c}  imes \vec{a}) $ and
$(\vec{c} imes \vec{a}) imes \left( \vec{a} imes ec{b} ight)$ a	as coterminous edges	s is,	WWW.Harasa
(a) 8 cubic units	(b) 512 cubic units	s (c) 64 cubic units	(d) 24 cubic units
11. The angle betwee	en the lines $\frac{x-2}{x-1} = \frac{1}{x-1}$	$\frac{y+1}{-2}$ , $z=2$ and $\frac{x-1}{1} = \frac{2}{3}$	$\frac{2y+3}{z} = \frac{z+5}{z+3}$ is
·	3		
(a) $\frac{\pi}{6}$	(b) $\frac{\pi}{4}$	$(c)\frac{n}{3}$	$(d)\frac{\pi}{2}$
12. The slope of the c	curve $y^3 - xy^2 = 4$	at the point where $y = 2$ i	S
(a) $-2$	(b) $-\frac{1}{2}$	(c) $\frac{1}{2}$	(d) $\frac{1}{2}$
WWW.	2	(c) $\frac{1}{4}$	2
13. The point of infle	ction of the curve $y$	$=(x-1)^3$ is	
(a) (0,0)	(b) (0,1)	(c) (1,0)	(d) (1,1)
14. If $f(x, y) = e^{xy}$ , then	$nen \frac{\partial^2 f}{\partial x \partial y} \text{ is equal to}$		· · · · · · · · · · · · · · · · · · ·
(a) $xye^{xy}$	(b) $(1+xy)e^{xy}$	(c) $(1+y)e^{xy}$	(d) $(1+x)e^{xy}$
15. If $u(x, y) = e^{x^2 + y^2}$	, then $\frac{\partial u}{\partial r}$ is equal	to :	in the second of
(a) $e^{x^2+y^2}$	(b) 2ru	(c) $r^2 u$	(d) w²
(4)	(0) 2.14	(1.)	$(\mathbf{u}) y u$
6. The general solution	on of the differentia	(c) $(1+y)e^{xy}$ to (c) $x^2u$ I equation $\log\left(\frac{dy}{dx}\right) = x +$	y is
$(a) e^x + e^y = c$	(b) $e^x + e^{-y} = c$	(c) $e^{-x} + e^y = c$	(d) $e^{-x} + e^{-y} = c$
		he general solutions of or	
_	(b) $n, n+1$	(c) $n+1, n+2$	(d) $n+1, n$

15.

16.

17.

18. If the function  $f(x) = \frac{1}{12}$  for a < x < b, represents a probability density function of a

continuous random variable X, then which of the following cannot be the value of a and b

19.	On a multiple-che	oice exam with 3	possible destructives	(d) 16 and 24 www.s for each of the 5 c	Padasalai.Net questions, the
adas			more correct answer		dasajani
	4TJ	7	(c) $\frac{1}{243}$		
20.	In the last column	of the truth table f	for $\neg(p \lor \neg q)$ the nu	imber of final outcom	es of the truth
	value 'F' are				
	(a) 1	(b) 2	(c)) 3	(d) 4	uu Mabt
	alaruse.	, padasalal. No	PART – II	al.No.	
ote: (	i) Answer any SE	VEN questions.			$7\times2=14$
(i	i) Question numbe	er 30 is compulsory	· ppadasal		dasalai.Net
21.	Find the rank of th	ne matrix : $\begin{bmatrix} 1 & -2 \\ 3 & -6 \end{bmatrix}$	$\begin{bmatrix} -1 & 0 \\ -3 & 1 \end{bmatrix}$	al Net	a asalai Net
22.	If $z_1 = 2 - i$ and $z_1 = 2 - i$	$z_2 = -4 + 3i$ , find the	he inverse of $\frac{z_1}{z_2}$		
23.	State the reason fo	or $\cos^{-1} \left[ \cos \left( -\frac{\pi}{6} \right) \right]^{\frac{\pi}{2}}$	$\neq \frac{\pi}{6}$ .	al.Net	dasalai Net
24.	Find the length of	the latus rectum of	the hyperbola $16y^2$	$-9x^2 = 144$	
25.	Evaluate : $\lim_{x\to 0} \left(\sin \left(\frac{\sin \left(\frac{\cos \left(\frac{\cos \left(\frac{\cos \left(\frac{\sin \left(\frac{\cos \left(\frac{\sin \left(\frac{\cos (\cos \left(\frac{\cos (\cos \left(\frac{\cos (\cos \left(\frac{\cos (\cos \left(\frac{\cos (\cos (\cos$	$\left(\frac{\ln x}{x^2}\right)$ .	Padasal	alines. NimwiPâ	dasalal.No
26.	Find the area of th	he region bounded	by the line $6x + 5y$	=30, x axis and the	lines $x = -1$ and

28. Find the mean and variance of X, for the probability mass functions of X given below:

$$f(x) = \begin{cases} 2(x-1) & 1 < x << 2 \\ 0 & \text{otherwise} \end{cases}$$

x=3.

27. Solve:  $\frac{dy}{dx} + y = e^{-x}$ 

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29. Let  $A = \{a + \sqrt{5}b : a, b \in \mathbb{Z}\}$ . Check whether the usual multiplication is a binary operation on A.

30. Find the vector equation of the plane passing through the point (2,2,3) having 3,4,3 as direction ratios of the normal to the plane

## **PART-III**

Note: (i) Answer any SEVEN questions.

 $7 \times 3 = 21$ 

(ii) Question number 40 is compulsory.

31. Solve by matrix inversion method: 5x+2y=4, 7x+3y=5

32. Solve the equation  $2x^3 + 11x^2 - 9x - 18 = 0$ 

- 33. The maximum and minimum distances of the Earth from the Sun respectively are  $152 \times 10^6 km$  and  $94.5 \times 10^6 km$ . The Sun is at one focus of the elliptical orbit. Find the distance from the Sun to the other focus.
- 34. If  $\vec{a} = \hat{i} + 2\hat{j} + 3\hat{k}$ ,  $\vec{b} = 2\hat{i} \hat{j} + \hat{k}$ ,  $\vec{c} = 3\hat{i} + 2\hat{j} + \hat{k}$  and  $\vec{a} \times (\vec{b} \times \vec{c}) = l\vec{a} + m\vec{b} + n\vec{c}$ , find the values of l, m, n.
- 35. Find two positive numbers whose product is 20 and their sum is minimum.
- 36. Find the approximate value of  $\sqrt[5]{31}$ .
- 37. Find the area of the region bounded by 2x-y+1=0, y=-1, y=3 and y-axis.
- 38. Find the differential equation for the function  $y = 2(x^2 1) + ce^{-x^2}$  where c is an arbitrary constant.
- 39. If  $X \sim B(n, p)$  such that 4P(X = 4) = P(x = 2) and n = 6. Find the distribution, mean standard deviation.

40. If 
$$x + iy = \sqrt{\frac{a+ib}{c+id}}$$
, prove that  $x^2 + y^2 = \sqrt{\frac{a^2 + b^2}{c^2 + d^2}}$ 

#### PART - IV

Note: Answer all the questions.

 $7 \times 5 = 35$ 

- 41. (a) Test for consistency and if possible, solve the system of equations 2x-y+z=2, 6x-3y+3z=6, 4x-2y+2z=4. (OR)
  - (b) Find the all cube roots of  $\sqrt{3} + i$
- 42. (a) Find a polynomial equation of minimum degree with rational coefficients, having  $\sqrt{5} \sqrt{3}$  as a root. (OR)
  - (b) If D is the midpoint of the side BC of a triangle ABC, then show by vector method the  $\left|\overrightarrow{AB}\right|^2 + \left|\overrightarrow{AC}\right|^2 = 2\left(\left|\overrightarrow{AD}\right|^2 + \left|\overrightarrow{BD}\right|^2\right)$ .
- 43. (a) Show that the straight lines  $\vec{r} = \left(5\hat{i} + 7\hat{j} 3\hat{k}\right) + s\left(4\hat{i} + 4\hat{j} 5\hat{k}\right)$  and  $\vec{r} = \left(8\hat{i} + 4\hat{j} + 5\hat{k}\right) + t\left(7\hat{i} + \hat{j} + 3\hat{k}\right)$  are coplanar. Find the vector equation of the plane in which they lie. (OR)
  - (b) The volume of a cylinder equals V cubic cm, where V is a constant. Find the condition that minimize the total surface area of the cylinder.

44. (a) If the curves  $ax^2 + by^2 = 1$  and  $cx^2 + dy^2 = 1$  intersect each other orthogonally then,  $\frac{1}{a} - \frac{1}{b} = \frac{1}{c} - \frac{1}{d}.$  (OR)

(b) Let 
$$z(x, y) = xe^y + ye^{-x}, x = e^{-t}, y = st^2, s, t \in \mathbb{R}$$
. Find  $\frac{\partial z}{\partial s}$  and  $\frac{\partial z}{\partial t}$ .

- 45. (a) Prove that  $\int_{0}^{\frac{\pi}{4}} \log(1 + \tan x) dx = \frac{\pi}{8} \log 2$ . (OR)
  - (b) Solve:  $\frac{dy}{dx} = \frac{x y + 5}{2(x y) + 7}$ .
- 46. (a) The sum of mean and variance of a binomial distribution for five trails is 1.8. Find the distribution. (OR)
  - (b) Establish the equivalence property  $p \leftrightarrow q \equiv (p \rightarrow q) \land (q \rightarrow p)$
- 47. (a) Solve  $\cos(\tan^{-1} x) = \sin(\cot^{-1} \frac{3}{4})$ 
  - (b) Find the equation of the circle through the points (1,0), (-1,0), and (0,1).

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## HIGHER SECONDARY SECOND YEAR

### **MATHEMATICS**

## **MODEL QUESTION PAPER - 6**

Time Allowed:	15	Min	+3.00	Hours]	
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[Maximum Marks:90

Instructions:

- Check the question paper for fairness of printing. If there is any (a) lack of fairness, inform the Hall Supervisor immediately.
- Use Blue or Black ink to write and underline and pencil to draw (b) diagrams.

#### PART - I

Note:

(i) All questions are compulsory.

- $20 \times 1 = 20$
- (ii) Choose the correct or most suitable answer from the given four alternatives. Write the option code and the corresponding answer.
- 1. If  $\rho(A) = \rho([A \mid B])$ , then the system of linear equations AX = B is
  - (a) consistent and has a unique solution (b) consistent
  - (c) consistent and has infinitely many solution (d) inconsistent
- 2. Let A be a non-singular matrix then which one of the following is false

  - (a)  $\left(\operatorname{adj} A\right)^{-1} = \frac{A}{|A|}$  (b) I is an orthogonal matrix

  - (c)  $adj(adjA) = |A|^n A$  (d) If A is symmetric then adjA is symmetric
- 3. If  $z = \frac{(\sqrt{3} + i)^3 (3i + 4)^2}{(8 + 6i)^2}$ , then |z| is
  - (a) 0
- (b) 1

(c)2

- (d) 3
- 4. The continued product of the four values of  $\left(\cos\frac{\pi}{3} + i\sin\frac{\pi}{3}\right)^{\frac{7}{4}}$  is
  - (a) 1

- (d) -2
- 5. The value of  $\sin^{-1}(2\cos^2 x 1) + \cos^{-1}(1 2\sin^2 x)$  is
  - (a)  $\frac{\pi}{2}$
- (b)  $\frac{\pi}{2}$
- (c)  $\frac{\pi}{4}$
- (d)  $\frac{\pi}{\epsilon}$
- 6. The area of quadrilateral formed with foci of the hyperbolas  $\frac{x^2}{a^2} \frac{y^2}{h^2} = 1$  and  $\frac{x^2}{a^2} \frac{y^2}{h^2} = -1$ is

	(a) $4(a^2+b^2)$	(b) $2(a^2+b^2)$	(c) $a^2 + b^2$	$(d) \frac{1}{2} (a^2 + b^2) w. Padasalai. Net$			
7	. An ellipse has <i>OB</i> as set Then the eccentricity of	mi minor axes, F	and $F'$ its foci and the	e angle $FBF'$ is a right angle.			
	(a) $\frac{1}{\sqrt{2}}$	(b) $\frac{1}{2}$	EDWAM PRODUCT	(d) $\frac{1}{\sqrt{3}}$			
8	If $\vec{a}, \vec{b}, \vec{c}$ are three non-c	coplanar unit vecto	rs such that $\vec{a} \times (\vec{b} \times \vec{c})$	$=\frac{\left(\vec{b}+\vec{c}\right)}{\sqrt{2}}$ , then the angle			
	between $\vec{a}$ and $\vec{b}$ is		WWW.Pauss	www.Pause			
	(a) $\frac{\pi}{2}$	(b) $\frac{3\pi}{4}$	$(c)\frac{\pi}{4}$	(d) $\pi$			
9.	The equation of the plan x+2y-2z-9=0 is	sassalai Net	nadassalal.)	detaaaaalal.Net			
	24			x = 1 (d) $x + 2y - 2z = 5$			
10.	If $\left[\vec{a}, \vec{b}, \vec{c}\right] = 1$ , then the	value of $\frac{a \cdot (b \times c)}{(\vec{c} \times \vec{a}) \cdot \vec{b}}$	$\frac{\vec{b} \cdot (c \times a)}{\vec{b} \cdot \vec{c}} + \frac{c \cdot (a \times b)}{(\vec{c} \times \vec{b}) \cdot \vec{c}} + \frac{c \cdot (a \times b)}{(\vec{c} \times \vec{b})}$	$\frac{\partial}{\partial a}$ is			
	(a) 1	(b) $-1$	(c) 2	$\pi$ (d) 3			
11. The slope of the line normal to the curve $f(x) = 2\cos 4x$ at $x = \frac{\pi}{12}$ is							
	(i) $-4\sqrt{3}$	(ii) -4	1.2	(iv) $4\sqrt{3}$			
12.	The number given by th	ne Rolle's theorem	n for the function $x^3$	$3x^2, x \in [0,3]$ is			
	(a) 1	(b) $\sqrt{2}$	(c) $\frac{3}{2}$	(d) 2			
13.	If $f(x, y, z) = xy + yz +$	$zx$ , then $f_x - f_z$	is equal to				
	(a) $z-x$	(b) $y-z$	(c) $x-z$	(d) $y-x$			
14.	If $f(x) = \int_0^x t \cos t  dt$ , the	hen $\frac{df}{dx}$ =	. ₩şk, ağadasalal.l	vet			
	(a) $\cos x - x \sin x$	(b) $\sin x + x \cos x$	$(c) x \cos x$	(d) $x \sin x$			
15.	The value of $\int_{-\pi}^{\frac{\pi}{2}} \frac{\sin x}{2 + \cos x}$	$\frac{d}{dx}$ is	www.Padasalai.l	Vet			
ada	The value of $\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \frac{\sin x}{2 + \cos x}$ (a) 0	(b) 2	(c) log 2	(d) log 4			
	smar Net		i.	det i de de la compandation de la c			
	Salow			" . " . Pagaasala"			

16	The order and degree 0	the differential equati	on $\frac{d^2y}{dx^2} + \left(\frac{dy}{dx}\right)^{1/2} +$	$x^{1/4} = 0$ are respectively
ada 10.	The order and degree of		$\frac{dx^{2}}{(c)} = \frac{(dx)^{2}}{2}$	(d) 2 4
٠	(a) 2, 3			
17.	The solution of the diffe	erential equation $2x\frac{dy}{dx}$	$\frac{y}{c} - y = 3$ represents	
	(-) studialit lines	(b) circles	(c) parabola	(d) ellipse
18.	A random variable X ha	as binomial distribution	n with $n = 25$ and $p$	= 0.8 then standard deviation
	of $X$ is (a) 6	(b) 4	(c) 3	(d) 2
19.		a is a probability d	ensity function of a	random variable, the value
	then of a is			*
	(a) 1	(b) 2	(c) 3	(d) 4
20.	Subtraction is not a bination (a) $\mathbb{R}$	ary operation on (b) $\mathbb{Z}$	(c) N	(d) Q
	(a) 12	PART -	(c) ℕ - <b>II</b>	Carrassalal Net
auo-	CO A CEVEN		7-3000	$7\times2=1$
	(i) Answer any SEVEN	1977		; · · <sub>p</sub>
(i	i) Question number 30 i	is compulsory.	padasalai.Net	Padasalal Net
	$\begin{bmatrix} 0 & -2 \end{bmatrix}$	0		e en la company de la comp La company de la company d
21.	If $adj(A) = \begin{bmatrix} 0 & -2 \\ 6 & 2 \\ -3 & 0 \end{bmatrix}$	$\begin{bmatrix} -6 \\ 6 \end{bmatrix}$ , find $A^{-1}$ .		
22.	Express $-1+i\sqrt{3}$ in po	olar form.	r carakta Metile k	uri Mandiri Alidis u arti
23.	Find centre and radius	of the circle $2x^2 + 2y$	$x^2 - 6x + 4y + 2 = 0$	
	WWW.Pauc	· · · · · · · · · · · · · · · · · · ·	(2) 2 (2) 14(3)	$(\hat{i} + \hat{k})$ and the plane
24.	Find the angle between	the straight line $r = 0$	(2i+3j+k)+i(i-	The plane
	2x-y+z=5.	isalai Nerri	Padasalaline	Www.Padasalal.Net
25	Explain why Lagrange	mean value theorem i	s not applicable to	the function
	anNet.	isalai.Net	a a a salai Net	w cassalal Net
	$f(x) = \left  \frac{1}{x} \right , x \in [-1,1].$	WWWW.	t telefolial et	www.Pada
26.	Evaluate: $\int_{0}^{1} \frac{ x }{x} dx$	isalal Net	Padasalai Net	onggan Padasalal Nets Su , , , ot woler, x23 (d)
27.	Form the differential e	quation of the famil	y of parabolas $y^2$	= 4ax, where a is an arbi

constant.

29. Write the statements in words corresponding to  $\neg p$ ,  $q \lor \neg p$ , where p is 'It is cold' and q is 'It is raining.'.

30. Find the value of 
$$\cos^{-1}\left(\frac{1}{2}\right) - 2\sin^{-1}\left(-\frac{1}{2}\right)$$

PART-III

Note:

(i) Answer any SEVEN questions.

 $7\times3=21$ 

(ii) Question number 40 is compulsory.

31. Find the adjoint of the matrix  $A = \begin{bmatrix} 1 & 3 \\ 2 & -5 \end{bmatrix}$  and verify that A(adjA) = (adjA)A = |A|I.

32. Show that the points 1,  $-\frac{1}{2} + \frac{i\sqrt{3}}{2}$  and  $-\frac{1}{2} - \frac{i\sqrt{3}}{2}$  are the vertices of the equilateral triangle.

33. Find the equation of the hyperbola with vertices  $(0,\pm 4)$  and foci  $(0,\pm 6)$ .

34. If the two lines  $\frac{x-1}{2} = \frac{y+1}{3} = \frac{z-1}{4}$  and  $\frac{x-3}{1} = \frac{y-m}{2} = z$  intersect at a point, find the value of m.

35. If  $w(x, y) = xy + \sin(xy)$ , then prove that  $\frac{\partial^2 w}{\partial y \partial x} = \frac{\partial^2 w}{\partial x \partial y}$ 

36. Evaluate :  $\int_{0}^{\frac{\pi}{3}} \frac{\sec x \tan x}{1 + \sec^2 x} dx$ .

37. Solve:  $\frac{dy}{dx} = \sqrt{\frac{1 - y^2}{1 - x^2}}$ .

38. Form the differential equation of  $y = e^{3x} (C\cos 2x + D\sin 2x)$ , where C and D are arbitrary constants.

39. Solve:  $y^2 + x^2 \frac{dy}{dx} = xy \frac{dy}{dx}$ 

40. Find the equation of the tangent to the curve  $x^2y - x = y^3 - 8$  at x = 0

## PART - IV

Note: Answer all the questions.

 $7 \times 5 = 35$ 

41. (a) Find the inverse of the non-singular matrix  $A = \begin{bmatrix} 2 & 1 & 1 \\ 3 & 2 & 1 \\ 2 & 1 & 2 \end{bmatrix}$ , by elimentary transformations. (OR)

(b) If 
$$z = x + iy$$
 and  $\arg\left(\frac{z-1}{z+1}\right) = \frac{\pi}{2}$ , then show that  $x^2 + y^2 = 1$ 

- 42. (a) Solve the equation  $6x^4 5x^3 38x^2 5x + 6 = 0$  if it is known that  $\frac{1}{3}$  is a solution.(OR)
  - (b) Solve  $\tan^{-1} 2x + \tan^{-1} 3x = \frac{\pi}{4}$ , if  $6x^2 < 1$ .
- 43. (a) An elliptical whispering room has height 5m and width 26m. Where should two persons stand if they would like to whisper back and forth and be heard. (OR)
  - (b) Show that the four points (6,-7,0), (16,-19,-4), (0,3,-6), (2,-5,10) lie on a same plane.
- 44. (a) Show that the straight lines x+1=2y=-12z and x=y+2=6z-6 are skew and hence find the shortest distance between them. (OR)
  - (b) If we blow air into a balloon of spherical shape at a rate of 1000cm<sup>3</sup> per second. At what rate the radius of the baloon changes when the radius is 7cm? Also compute the rate at which the surface area changes.
- 45. (a) If an initial amount  $A_0$  of money is invested at an interest rate r compounded n times a year, the value of the investment after t years is  $A = A_0 \left( 1 + \frac{r}{n} \right)^{n \cdot t}$ . If the interest is compounded continuously, (that is  $n \to \infty$ ) show that the amount after t years is  $A = A_0 e^{rt}$ . (OR)
  - (b) If  $u = \sec^{-1}\left(\frac{x^3 y^3}{x + y}\right)$ , show that  $x\frac{\partial u}{\partial x} + y\frac{\partial u}{\partial y} = 2\cot u$
- 46. (a) The curve  $y = (x-2)^2 + 1$  has a minimum point at P. A point Q on the curve is such that the slope of PQ is 2. Find the area bounded by the curve and the chord PQ. (OR)
  - (b) Prove that  $p \rightarrow (\neg q \lor r) \equiv \neg p \lor (\neg q \lor r)$  using truth table.
- 47. (a) An equation relating to the stability of an aircraft is given by  $\frac{dv}{dt} = g \cos \alpha kv$ , where g,  $\alpha$ , k are constants and v is the velocity. Obtain an expression in terms of v if v = w when t = 0. (OR)
  - (b) Four fair coins are tossed once. Find the probability mass function, mean and variance for number of heads occurred.

## \*\*\*\*All The Best\*\*\*\*