

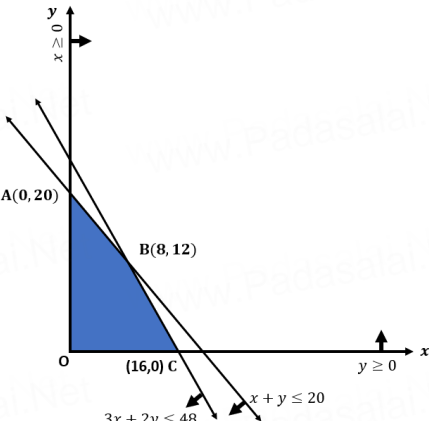
Sample Question Paper CLASS: XII Session: 2022-23 Applied Mathematics (Code-241) Marking Scheme	
Section – A Each question carries 1-mark weightage	
1.	$x \equiv 27 \pmod{4}$ $\Rightarrow x - 27 = 4k$, for some integer k $\Rightarrow x = 31$ as $27 < x \leq 36$ (C) option
2.	(D) option
3.	$n = 26 \Rightarrow t = 3.07 > t_{25}(0.05) = 2.06$ (B) option
4.	$n = 34 \Rightarrow v = 34 - 1 = 33$ (B) option
5.	Speed of boat downstream = $u = 10$ km/h And, speed of boat upstream = $v = 6$ km/h \Rightarrow Speed of stream = $\frac{1}{2}(u - v) = 2$ km/h (B) option
6.	(C) option
7.	Truck A carries water = $100 - \left(\frac{20 \times 1500}{1000}\right) = 70$ l Truck B carries water = $80 - \left(\frac{20 \times 1000}{1000}\right) = 60$ l (C) option
8.	Let the face value of the bond = x Then, $\frac{10}{200}x = 1800 \Rightarrow x = 36000$ (D) option
9.	(C) option
10.	(D) option
11.	$D = \frac{C - S}{n} = \frac{480000 - 25000}{10} = 45500$ (B) option
12.	(A) option
13.	$\int \frac{dy}{y \log y} = \int \frac{dx}{x}$ $\Rightarrow \log(\log y) = \log x + \log C $ $\Rightarrow \log(\log y) = \log Cx $ $\Rightarrow y = e^{ Cx }$

	Subject to constraints: $x + y \leq 960$ $5x + y \leq 2400$ $x, y \geq 0$	1
24.	Speed of boat in still waters = x km/h Speed of stream = y km/h Distance travelled = d km Time taken to travel downstream = $\frac{d}{x+y}$ Time taken to travel upstream = $\frac{d}{x-y}$	1
	Then, $\frac{2d}{x+y} = \frac{d}{x-y} \Rightarrow x : y = 3 : 1$	1
	OR	1
	Param runs 5 m in 3 seconds \Rightarrow time taken to run 200 m = $\frac{3}{5} \times 200 = 120$ seconds	
	Anuj 's time = $120 - 3 = 117$ seconds	1
25.	$V_f = 437500, V_i = 350000$ Nominal rate = $\frac{V_f - V_i}{V_i} \times 100$	1
	$= \frac{437500 - 350000}{350000} \times 100 = 25\%$	1
Section – C		
Each question carries 3-mark weightage		
26.	$f'(x) = x^3 - 6x^2 + 11x - 6 = (x - 1)(x - 2)(x - 3)$ $\Rightarrow x = 1, 2, 3$	1
	Strictly increasing in $(1, 2) \cup (3, \infty)$	1
	Strictly decreasing in $(-\infty, 1) \cup (2, 3)$	1
27.	Daily diet of team A = $[2 \ 3 \ 1] \begin{bmatrix} 2500 & 65 \\ 1900 & 50 \\ 2000 & 54 \end{bmatrix} = \begin{bmatrix} 12700 \\ 334 \end{bmatrix}$ Team A consumes 12700 calories and 334 g vitamin	1.5
	Daily diet of team B = $[1 \ 2 \ 2] \begin{bmatrix} 2500 & 65 \\ 1900 & 50 \\ 2000 & 54 \end{bmatrix} = \begin{bmatrix} 10300 \\ 273 \end{bmatrix}$ Team B consumes 10300 calories and 273 g vitamin	1.5
28.	$\int \frac{dx}{(1 + e^x)(1 + e^{-x})}$ $= \int \frac{e^x dx}{(1 + e^x)^2}$	3

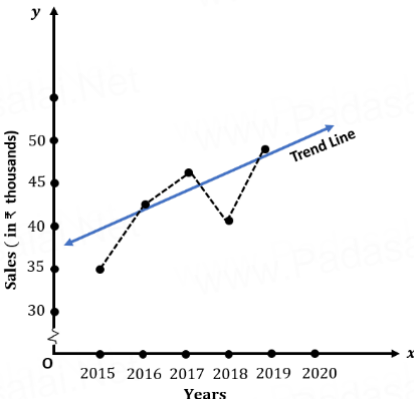
	$= \int \frac{dt}{t^2}, \text{ where } t = e^x + 1 \text{ and } dt = e^x dx$ $= \frac{-1}{t} + C$ $= \frac{-1}{1+e^x} + C$ <p style="text-align: center;">OR</p> $\int \frac{x \log(1+x^2) dx}{I}$ <p style="text-align: center;">, Integration by parts</p> $= \log(1+x^2) \cdot \int x dx - \int \left[\frac{d}{dx} \log(1+x^2) \cdot \int x dx \right] dx$ $= \frac{x^2}{2} \log(1+x^2) - \int \left[\frac{2x}{1+x^2} \cdot \frac{x^2}{2} \right] dx$ $= \frac{x^2}{2} \log(1+x^2) - \int \frac{x^3}{1+x^2} dx$ $= \frac{x^2}{2} \log(1+x^2) - \int \left[x - \frac{x}{1+x^2} \right] dx$ $= \frac{x^2}{2} \log(1+x^2) - \frac{x^2}{2} + \frac{1}{2} \log(1+x^2) + C$ $= \frac{1}{2} [(1+x^2) \log(1+x^2) - x^2] + C$	
29.	<p>Under pure competition, $p_d = p_s$</p> $\Rightarrow \frac{8}{x+1} - 2 = \frac{x+3}{2}$ $\Rightarrow x^2 + 8x - 9 = 0$ $\Rightarrow x = -9, 1$ $\therefore x = 1$	1.5
	<p>When $x_0 = 1 \Rightarrow p_0 = 2$</p> $\therefore \text{Produce surplus} = 2 - \int_0^1 \frac{x+3}{2} dx = 2 - \left[\frac{x^2}{4} + \frac{3x}{2} \right]_0^1 = \frac{1}{4}$	1.5
	<p style="text-align: center;">OR</p> $p = 274 - x^2$ $\Rightarrow R = px = 274x - x^3$ $\frac{dR}{dx} = 274 - 3x^2$ <p>Given $MR = 4 + 3x$</p> <p>In profit monopolist market,</p> $MR = \frac{dR}{dx} \Rightarrow 4 + 3x = 274 - 3x^2$ $\Rightarrow x^2 + x - 90 = 0$	1.5

	$\Rightarrow x = -10, 9$ $\therefore x = 9$	
	When $x_0 = 9 \Rightarrow p_0 = 193$ \therefore Consumer surplus $= \int_0^9 (274 - x^2) dx - 193 \times 9$ $= [274x - \frac{x^3}{3}]_0^9$ $= 486$	1.5
30.	Purchase = ₹ 40,00,000 Down payment = x Balance = $40,00,000 - x$ $i = \frac{9}{1200} = 0.0075, n = 25 \times 12 = 300$ $E = ₹ 30,000$	1
	$\Rightarrow 30000 = \frac{(4000000 - x) \times 0.0075}{1 - (1.0075)^{-300}}$ $\Rightarrow 30000 = \frac{(4000000 - x) \times 0.0075}{1 - 0.1062}$ $\Rightarrow x = 424800$ Down payment = ₹ 4,24,800	2
31.	$n = 10 \times 2 = 20, S = 10,21,760, i = \frac{5}{200} = 0.025, R = ?$ $S = R \left[\frac{(1+i)^n - 1}{i} \right]$	1.5
	$\Rightarrow 1021760 = R \left[\frac{(1+0.025)^{20} - 1}{0.025} \right]$ $\Rightarrow 1021760 = R \left[\frac{1.6386 - 1}{0.025} \right]$ $\Rightarrow R = \left[\frac{1021760 \times 0.025}{0.6386} \right]$ $\Rightarrow R = ₹ 40,000$ Mr Mehra set aside an amount of ₹ 40,000 at the end of every six months	1.5
Section – D		
Each question carries 5-mark weightage		
32.	Probability of defective bucket = 0.03 $n = 100$ $m = np = 100 \times 0.03 = 3$ Let $X =$ number of defective buckets in a sample of 100 $P(X = r) = \frac{m^r e^{-m}}{r!}, r = 0, 1, 2, 3, \dots$	1
	(i) $P(\text{no defective bucket}) = P(r = 0) = \frac{3^0 e^{-3}}{0!} = 0.049$	2
	(ii) $P(\text{at most one defective bucket}) = P(r = 0, 1)$ $= \frac{3^0 e^{-3}}{0!} + \frac{3^1 e^{-3}}{1!}$	2

	$= 0.049 + 0.147$ $= 0.196$	
	OR	
	$X = \text{scores of students, } \mu = 45, \sigma = 5$ $\therefore Z = \frac{X - \mu}{\sigma} = \frac{X - 45}{5}$	1
	(i) When $X = 45, Z = 0$ $P(X > 45) = P(Z > 0) = 0.5$ $\Rightarrow 50\%$ students scored more than the mean score	2
	(ii) When $X = 30, Z = -3$ and when $X = 50, Z = 1$ $P(30 < X < 50) = P(-3 < Z < 1) = P(-3 < Z \leq 1)$ $= P(-3 < Z \leq 0) + P(0 \leq Z < 1)$ $= P(0 \leq Z < 3) + P(0 \leq Z < 1)$ $= 0.4987 + 0.3413 = 0.84$ $\Rightarrow 84\%$ students scored between 30 and 50 marks	2
33.	Let x be the number of guests for the booking Clearly, $x > 100$ to avail discount $\therefore \text{Profit, } P = [4800 - \frac{200}{10}(x - 100)]x = 6800x - 20x^2$	2
	$\Rightarrow \frac{dP}{dx} = 6800 - 40x \Rightarrow x = 170$	1
	As $\frac{d^2P}{dx^2} = -40 < 0, \forall x$	1
	A booking for 170 guests will maximise the profit of the company And, Profit = ₹ 5,78,000	1
	OR	
	$P(x) = R(x) - C(x)$ $= 5x - (100 + 0.025x^2)$	2
	$\Rightarrow P'(x) = 5 - 0.05x \Rightarrow x = 100$	1
	As $P''(x) = -0.05 < 0, \forall x$	1
	\therefore Manufacturing 100 dolls will maximise the profit of the company And, Profit = ₹ 1,50,000	1
34.	Let the number of tables and chairs be x and y respectively (Max profit) $Z = 22x + 18y$ Subject to constraints: $x + y \leq 20$ $3x + 2y \leq 48$ $x, y \geq 0$	1.5

		2										
	<p>The feasible region OABCA is closed (bounded)</p> <table border="1" data-bbox="576 701 1045 909"> <thead> <tr> <th>Corner points</th> <th>$Z = 22x + 18y$</th> </tr> </thead> <tbody> <tr> <td>O (0,0)</td> <td>0</td> </tr> <tr> <td>A (0,20)</td> <td>360</td> </tr> <tr> <td>B (8,12)</td> <td>392</td> </tr> <tr> <td>C (16,0)</td> <td>352</td> </tr> </tbody> </table> <p>Buying 8 tables and 12 chairs will maximise the profit</p>	Corner points	$Z = 22x + 18y$	O (0,0)	0	A (0,20)	360	B (8,12)	392	C (16,0)	352	1.5
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35.	$A = \begin{bmatrix} 1 & 2 & 3 \\ 3 & 2 & 2 \\ 2 & 3 & 2 \end{bmatrix}$ $\Rightarrow A = 9 \Rightarrow A^{-1} \text{ exists}$ $\text{And } A^{-1} = \frac{1}{9} \begin{bmatrix} -2 & 5 & -2 \\ -2 & -4 & 7 \\ 5 & 1 & -4 \end{bmatrix}$	2										
	$AX = B \Rightarrow X = A^{-1}B$ $\Rightarrow X = \frac{1}{9} \begin{bmatrix} -2 & 5 & -2 \\ -2 & -4 & 7 \\ 5 & 1 & -4 \end{bmatrix} \begin{bmatrix} 85 \\ 105 \\ 110 \end{bmatrix} = \begin{bmatrix} 15 \\ 20 \\ 10 \end{bmatrix}$ $\Rightarrow p_1 = 15, p_2 = 20, p_3 = 10$	3										
Section – E Each Case study carries 4-mark weightage												
36.	CASE STUDY - I											
a)	Pipe C empties 1 tank in 20 h $\Rightarrow \frac{2}{5}$ th tank in $\frac{2}{5} \times 20 = 8$ hours	1										
b)	Part of tank filled in 1 hour = $\frac{1}{15} + \frac{1}{12} - \frac{1}{20} = \frac{1}{10}$ th \Rightarrow time taken to fill tank completely = 10 hours	1										
c)	At 5 am,	2										

	<p>Let the tank be completely filled in 't' hours \Rightarrow pipe A is opened for 't' hours pipe B is opened for 't-3' hours And, pipe C is opened for 't-4' hours</p> <p>\Rightarrow In one hour, part of tank filled by pipe A = $\frac{t}{15}$ th part of tank filled by pipe B = $\frac{t-3}{15}$ th and, part of tank emptied by pipe C = $\frac{t-4}{15}$ th</p> <p>Therefore $\frac{t}{15} + \frac{t-3}{12} - \frac{t-4}{20} = 1$ $\Rightarrow t = 10.5$ Total time to fill the tank = 10 hours 30 minutes</p>																																				
	<p>OR</p> <p>6 am, pipe C is opened to empty $\frac{1}{2}$ filled tank Time to empty = 10 hours Time for cleaning = 1 hour</p> <p>Part of tank filled by pipes A and B in 1 hour = $\frac{1}{15} + \frac{1}{12} = \frac{3}{20}$ th tank \Rightarrow time taken to fill the tank completely = $\frac{20}{3}$ hours Total time taken in the process = $10 + 1 + \frac{20}{3} = 17$ hour 40 minutes</p>																																				
37.	CASE STUDY - II																																				
a)	<table border="1" data-bbox="397 1193 1034 1478"> <thead> <tr> <th>Year</th> <th>Y</th> <th>X</th> <th>X²</th> <th>XY</th> </tr> </thead> <tbody> <tr> <td>2015</td> <td>35</td> <td>-2</td> <td>4</td> <td>-70</td> </tr> <tr> <td>2016</td> <td>42</td> <td>-1</td> <td>1</td> <td>-42</td> </tr> <tr> <td>2017</td> <td>46</td> <td>0</td> <td>0</td> <td>0</td> </tr> <tr> <td>2018</td> <td>41</td> <td>1</td> <td>1</td> <td>41</td> </tr> <tr> <td>2019</td> <td>48</td> <td>2</td> <td>4</td> <td>96</td> </tr> <tr> <td></td> <td>212</td> <td></td> <td>10</td> <td>25</td> </tr> </tbody> </table> <p>$a = \frac{\sum Y}{n} = \frac{212}{5} = 42.4$ and $b = \frac{\sum XY}{\sum X^2} = \frac{25}{10} = 2.5$</p> <p>$Y_C = 42.4 + 2.5X$</p>	Year	Y	X	X ²	XY	2015	35	-2	4	-70	2016	42	-1	1	-42	2017	46	0	0	0	2018	41	1	1	41	2019	48	2	4	96		212		10	25	2
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b)	<p>For year 2022,</p> $Y_{2022} = 42.4 + 2.5(2022 - 2017) = 54.9$ <p>⇒ the estimated sales for year 2022 = ₹ 54,900</p>	1																									
c)	$Y_C = 42.4 + 2.5X$ $\Rightarrow 67.4 = 42.4 + 2.5X$ $\Rightarrow X = 10$ <p>Sales will be ₹ 67,400 in year (2017+ 10) = year 2027</p>	1																									
38.	CASE STUDY - III																										
a)	$\frac{k}{6} + \frac{2k}{6} + \frac{3(1-k)}{6} + \frac{4k}{2} = 1 \Rightarrow k = \frac{1}{4}$	1																									
b)	<p>P (getting admission on applying at least 2 weeks ahead of application deadline)</p> $= P(X = 2, 3, 4)$ $= \frac{1}{12} + \frac{3}{8} + \frac{1}{2} = \frac{23}{24}$ <p>[alternate method: $1 - P(X = 1) = 1 - \frac{1}{24} = \frac{23}{24}$]</p>	1																									
c)	<p style="text-align: center;">X = week applied ahead of application deadline</p> <table border="1" style="margin-left: auto; margin-right: auto;"> <tbody> <tr> <td>X</td> <td>1</td> <td>2</td> <td>3</td> <td>4</td> </tr> <tr> <td>P(X)</td> <td>$\frac{1}{24}$</td> <td>$\frac{1}{12}$</td> <td>$\frac{3}{8}$</td> <td>$\frac{1}{2}$</td> </tr> <tr> <td>XP(X)</td> <td>$\frac{1}{24}$</td> <td>$\frac{1}{6}$</td> <td>$\frac{9}{8}$</td> <td>2</td> </tr> </tbody> </table> <p style="text-align: center;">$\therefore E(X) = \frac{80}{24} = 3\frac{1}{3}$ weeks</p> <p style="text-align: center;">OR</p> <p>X = Scholarship money awarded for the week applied in, before the deadline</p> <table border="1" style="margin-left: auto; margin-right: auto;"> <tbody> <tr> <td>Week applied in</td> <td>1</td> <td>2</td> <td>3</td> <td>4</td> </tr> <tr> <td>X</td> <td>9600</td> <td>12000</td> <td>20000</td> <td>50000</td> </tr> </tbody> </table>	X	1	2	3	4	P(X)	$\frac{1}{24}$	$\frac{1}{12}$	$\frac{3}{8}$	$\frac{1}{2}$	XP(X)	$\frac{1}{24}$	$\frac{1}{6}$	$\frac{9}{8}$	2	Week applied in	1	2	3	4	X	9600	12000	20000	50000	2
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XP(X)	$\frac{9600}{24}$	$\frac{12000}{12}$	$\frac{60000}{8}$	$\frac{50000}{2}$		
$\therefore E(X) = ₹ 33,900$						

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