

KALAIMAGAL MATRIC HIGHER SECONDARY SCHOOL, MOHANUR.

STD : XI

MATHEMATICS

MARKS: 50

DATE: 15.02.2023

ONE MARKS TEST-I (BB FULLY)

TIME: 30 min

Choose the correct answer:

50 x 1 = 50

1. If $A = \{(x, y) : y = e^x, x \in R\}$ and $B = \{(x, y) : y = e^{-x}, x \in R\}$ then $n(A \cap B)$ is
 1) Infinity 2) 0 3) 1 4) 2
2. If $A = \{(x, y) : y = \sin x, x \in R\}$ and $B = \{(x, y) : y = \cos x, x \in R\}$ then $A \cap B$ contains
 1) no element 2) infinitely many elements 3) only one element 4) cannot be determined
3. The relation R defined on a set $A = \{0, -1, 1, 2\}$ by xRy if $|x^2 + y^2| \leq 2$, then which one of the following is true?
 1) $R = \{(0,0), (0,-1), (0,1), (-1,0), (-1,1), (1,2), (1,0)\}$ 2) $R^{-1} = \{(0,0), (0,-1), (0,1), (-1,0), (1,0)\}$
 3) Domain of R is $\{0, -1, 1, 2\}$ 4) Range of R is $\{0, -1, 1\}$
4. If $f(x) = |x-2| + |x+2|, x \in R$, then

$1) f(x) = \begin{cases} -2x & \text{if } x \in (-\infty, -2] \\ 4 & \text{if } x \in (-2, 2] \\ 2x & \text{if } x \in (2, \infty) \end{cases}$	$2) f(x) = \begin{cases} 2x & \text{if } x \in (-\infty, -2] \\ 4x & \text{if } x \in (-2, 2] \\ -2x & \text{if } x \in (2, \infty) \end{cases}$
$3) f(x) = \begin{cases} -2x & \text{if } x \in (-\infty, -2] \\ -4x & \text{if } x \in (-2, 2] \\ 2x & \text{if } x \in (2, \infty) \end{cases}$	$4) f(x) = \begin{cases} -2x & \text{if } x \in (-\infty, -2] \\ 2x & \text{if } x \in (-2, 2] \\ 2x & \text{if } x \in (2, \infty) \end{cases}$
5. If $|x+2| \leq 9$, then x belongs to
 1) $(-\infty, -7)$ 2) $[-11, 7]$ 3) $(-\infty, -7) \cup [11, \infty)$ 4) $(-11, 7)$
6. Given that x, y and b are real numbers $x < y, b > 0$, then
 1) $xb < yb$ 2) $xb > yb$ 3) $xb \leq yb$ 4) $\frac{x}{b} \geq \frac{y}{b}$
7. If $\frac{|x-2|}{x-2} \geq 0$, then x belongs to
 1) $[2, \infty)$ 2) $(2, \infty)$ 3) $(-\infty, 2)$ 4) $(-2, \infty)$
8. $\frac{1}{\cos 80^\circ} - \frac{\sqrt{3}}{\sin 80^\circ} =$
 1) $\sqrt{2}$ 2) $\sqrt{3}$ 3) 2 4) 4
9. If $\cos 28^\circ + \sin 28^\circ = k^3$, then $\cos 17^\circ$ is equal to
 1) $\frac{k^3}{\sqrt{2}}$ 2) $-\frac{k^3}{\sqrt{2}}$ 3) $\pm \frac{k^3}{\sqrt{2}}$ 4) $-\frac{k^3}{\sqrt{3}}$
10. The maximum value of $4 \sin^2 x + 3 \cos^2 x + \sin \frac{x}{2} + \cos \frac{x}{2}$ is
 1) $4 + \sqrt{2}$ 2) $3 + \sqrt{2}$ 3) 9 4) 4
11. The sum of the digits at the 10th place of all numbers formed with the help of 2, 4, 5, 7 taken all at a time is
 1) 432 2) 108 3) 36 4) 18
12. In an examination there are three multiple choice questions and each question has 5 choices. Number of ways in which a student can fail to get all answer correct is
 1) 125 2) 124 3) 64 4) 63
13. The number of ways in which the following prize be given to a class of 30 boys first and second in mathematics, first and second in physics, first in chemistry and first in English is
 1) $30^4 \times 29^2$ 2) $30^3 \times 29^3$ 3) $30^2 \times 29^4$ 4) 30×29^5

14. The number of 5 digit numbers all digits of which are odd is
 1) 25 2) 5^5 3) 5^6 4) 625

15. The value of $2+4+6+\dots+2n$ is
 1) $\frac{n(n-1)}{2}$ 2) $\frac{n(n+1)}{2}$ 3) $\frac{2n(2n+1)}{2}$ 4) $n(n+1)$

16. The coefficient of x^6 in $(2+2x)^{10}$ is
 1) ${}^{10}C_6$ 2) 2^6 3) ${}^{10}C_6 \cdot 2^6$ 4) ${}^{10}C_6 \cdot 2^{10}$

17. The coefficient of $x^8 y^{12}$ in the expansion of $(2x+3y)^{20}$ is
 1) 0 2) $2^8 3^{12}$ 3) $2^8 3^{12} + 2^{12} 3^8$ 4) ${}^{20}C_8 \cdot 2^8 3^{12}$

18. The equation of the locus of the point whose distance from y -axis is half the distance from origin is
 1) $x^2 + 3y^2 = 0$ 2) $x^2 - 3y^2 = 0$ 3) $3x^2 + y^2 = 0$ 4) $3x^2 - y^2 = 0$

19. Which of the following equation is the locus of $(at^2, 2at)$?
 1) $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$ 2) $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ 3) $x^2 + y^2 = a^2$ 4) $y^2 = 4ax$

20. Which of the following points lie on the locus of $3x^2 + 3y^2 - 8x - 12y + 17 = 0$
 1) (0,0) 2) (-2,3) 3) (1,2) 4) (0, -1)

21. If the point (8, -5) lies on the locus $\frac{x^2}{16} - \frac{y^2}{25} = k$, then the value of k is
 1) 0 2) 1 3) 2 4) 3

22. If $a_{ij} = \frac{1}{2}(3i - 2j)$ and $A = [a_{ij}]_{2 \times 2}$ is
 1) $\begin{bmatrix} \frac{1}{2} & 2 \\ -\frac{1}{2} & 1 \end{bmatrix}$ 2) $\begin{bmatrix} \frac{1}{2} & -\frac{1}{2} \\ 2 & 1 \end{bmatrix}$ 3) $\begin{bmatrix} 2 & \frac{1}{2} \\ \frac{1}{2} & -\frac{1}{2} \end{bmatrix}$ 4) $\begin{bmatrix} -\frac{1}{2} & \frac{1}{2} \\ 1 & 2 \end{bmatrix}$

23. What must be the matrix X , if $2X + \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} = \begin{bmatrix} 3 & 8 \\ 7 & 2 \end{bmatrix}$?
 1) $\begin{bmatrix} 1 & 3 \\ 2 & -1 \end{bmatrix}$ 2) $\begin{bmatrix} 1 & -3 \\ 2 & -1 \end{bmatrix}$ 3) $\begin{bmatrix} 2 & 6 \\ 4 & -2 \end{bmatrix}$ 4) $\begin{bmatrix} 2 & -6 \\ 4 & -2 \end{bmatrix}$

24. Which one of the following is not true about the matrix $\begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 5 \end{bmatrix}$?
 1) a scalar matrix 2) a diagonal matrix
 3) an upper triangular matrix 4) a lower triangular matrix

25. If A and B are two matrices such that $A+B$ and AB are both defined, then
 1) A and B are two matrices not necessarily of same order
 2) A and B are square matrices of same order
 3) Number of columns of A is equal to the number of rows of B
 4) $A=B$

26. The value of $\overrightarrow{AB} + \overrightarrow{BC} + \overrightarrow{DA} + \overrightarrow{CD}$ is
 1) \overrightarrow{AD} 2) \overrightarrow{CA} 3) \overrightarrow{O} 4) $-\overrightarrow{AD}$

27. If $\vec{a} + 2\vec{b}$ and $3\vec{a} + m\vec{b}$ are parallel, then the value of m is
 1) 3 2) $\frac{1}{3}$ 3) 6 4) $\frac{1}{6}$

28. The unit vector parallel to the resultant of the vectors $\hat{i} + \hat{j} - \hat{k}$ and $\hat{i} - 2\hat{j} + \hat{k}$ is

1) $\frac{\hat{i} - \hat{j} + \hat{k}}{\sqrt{5}}$ 2) $\frac{2\hat{i} + \hat{j}}{\sqrt{5}}$ 3) $\frac{2\hat{i} - \hat{j} + \hat{k}}{\sqrt{5}}$ 4) $\frac{2\hat{i} - \hat{j}}{\sqrt{5}}$

29. A vector \overrightarrow{OP} makes 60° and 45° with the positive direction of the x and y axes respectively. Then the angle between \overrightarrow{OP} and the z -axis is

- 1) 45° 2) 60° 3) 90° 4) 30°

30. $\lim_{x \rightarrow \infty} \frac{\sin x}{x}$

- 1) 1 2) 0 3) ∞ 4) $-\infty$

31. $\lim_{x \rightarrow \frac{\pi}{2}} \frac{2x - \pi}{\cos x} =$

- 1) 2 2) 1 3) -2 4) 0

32. $\lim_{x \rightarrow 0} \frac{\sqrt{1 - \cos 2x}}{x}$

- 1) 0 2) 1 3) $\sqrt{2}$ 4) does not exist

33. $\lim_{\theta \rightarrow 0} \frac{\sin \sqrt{\theta}}{\sqrt{\sin \theta}}$

- 1) 1 2) -1 3) 0 4) 2

34. $\frac{d}{dx} \left(\frac{2}{\pi} \sin x^\circ \right)$ is

- 1) $\frac{\pi}{180} \cos x^\circ$ 2) $\frac{1}{90} \cos x^\circ$ 3) $\frac{\pi}{90} \cos x^\circ$ 4) $\frac{2}{\pi} \cos x^\circ$

35. If $y = f(x^2 + 2)$ and $f'(3) = 5$, then $\frac{dy}{dx}$ at $x=1$ is

- 1) 5 2) 25 3) 15 4) 10

36. If $y = \frac{1}{4}u^4$, $u = \frac{2}{3}x^3 + 5$, then $\frac{dy}{dx}$ is

- 1) $\frac{1}{27}x^2(2x^3 + 15)^3$ 2) $\frac{1}{27}x(2x^3 + 5)^3$
 3) $\frac{2}{27}x^2(2x^3 + 15)^3$ 4) $-\frac{2}{27}x(2x^3 + 5)^3$

37. If $f(x) = x^2 - 3x$, then the points at which $f(x) = f'(x)$ are

- 1) both positive integers 2) both negative integers
 3) both irrational 4) one rational and another irrational

38. If $\int f(x)dx = g(x) + c$, then $\int f(x)g'(x)dx$

- 1) $\int (\mathbf{f}(x))^2 dx$ 2) $\int f(x)g(x) dx$ 3) $\int f'(x)g(x) dx$ 4) $\int (g(x))^2 dx$

39. If $\int \frac{3^{\frac{1}{x}}}{x^2} dx = k(3^{\frac{1}{x}}) + c$, then the value of k is

- 1) $\log 3$ 2) $-\log 3$ 3) $-\frac{1}{\log 3}$ 4) $\frac{1}{\log 3}$

40. If $\int f'(x)e^{x^2} dx = (x-1)e^{x^2} + c$, then $f(x)$ is

- 1) $2x^3 - \frac{x^2}{2} + x + c$ 2) $\frac{x^3}{2} + 3x^2 + 4x + c$ 3) $x^3 + 4x^2 + 6x + c$ 4) $\frac{2x^3}{3} - x^2 + x + c$

41. The gradient (slope) of a curve at any point (x, y) is $\frac{x^2 - 4}{x^2}$. If the curve passes through the point $(2, 7)$, then the equation of the curve is

- 1) $y = x + \frac{4}{x} + 3$ 2) $y = x + \frac{4}{x} + 4$ 3) $y = x^2 + 3x + 4$ 4) $y = x^2 - 3x + 6$

42. Four persons are selected at random from a group of 3 men, 2 women and 4 children. The probability that exactly two of them are children is

- 1) $\frac{3}{4}$ 2) $\frac{10}{23}$ 3) $\frac{1}{2}$ 4) $\frac{10}{21}$

43. A number is selected from the set $\{1, 2, 3, \dots, 20\}$. The probability that the selected number is divisible by 3 or 4 is

- 1) $\frac{2}{5}$ 2) $\frac{1}{8}$ 3) $\frac{1}{2}$ 4) $\frac{2}{3}$

44. A, B and C try to hit a target simultaneously but independently. Their respective probabilities of hitting the target are $\frac{3}{4}, \frac{1}{2}, \frac{5}{8}$. The probability that the target is hit by A or B but not by C is

- 1) $\frac{21}{64}$ 2) $\frac{7}{32}$ 3) $\frac{9}{64}$ 4) $\frac{7}{8}$

45. If A and B are any two events, then the probability that exactly one of them occur is

- 1) $P(A \cup \bar{B}) + P(\bar{A} \cup B)$ 2) $P(A \cap \bar{B}) + P(\bar{A} \cap B)$
 3) $P(A) + P(B) - P(A \cap B)$ 4) $P(A) + P(B) + 2P(A \cap B)$

46. Let R be the set of all real numbers. Consider the following subsets of the plane

$R \times R : S = \{(x, y) : y = x+1 \text{ and } 0 < x < 2\}$ and $T = \{(x, y) : x - y \text{ is an integer}\}$. Then which of the following is true?

- 1) T is an equivalence relation but S is not an equivalence relation.
 2) Neither S nor T is an equivalence relation
 3) Both S and T are equivalence relation
 4) S is an equivalence relation but T is not an equivalence relation

47. In 3 fingers, the number of ways four rings can be worn is ways.

- 1) $4^3 - 1$ 2) 3^4 3) 68 4) 64

48. Straight line joining the points $(2, 3)$ and $(-1, 4)$ passes through the point (α, β) if

- 1) $\alpha + 2\beta = 7$ 2) $3\alpha + \beta = 9$ 3) $\alpha + 3\beta = 11$ 4) $3\alpha + \beta = 11$

49. If $A = \begin{bmatrix} \lambda & 1 \\ -1 & -\lambda \end{bmatrix}$, then for what value of λ , $A^2 = O$?

- 1) 0 2) ± 1 3) -1 4) 1

50. If $\overline{BA} = 3\hat{i} + 2\hat{j} + \hat{k}$ and the position vector of B is $\hat{i} + 3\hat{j} - \hat{k}$, then the position vector A is

- 1) $4\hat{i} + 2\hat{j} + \hat{k}$ 2) $4\hat{i} + 5\hat{j}$ 3) $4\hat{i}$ 4) $-4\hat{i}$