## Loyola

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MATHS

## TERM - I, II \& III

This special guide is prepared on the basis of New Syllabus

## Loyola

## Publications

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## Loyola

Publications

## நாலினைள் பகுய்்்

1. 6ம் வகுப்பு கணிதம் மாணவ / மாணவியா் எளிதில் புரியும் வண்ணம் எழுதப்பட்டுள்ளது.
2. ஒவ்வொரு தலைப்புகளில் உள்ள கணக்குகள் அனைத்தும் எளிய முறையில் செய்து காட்டப்பட்டுள்ளது.
3. தேவைக்கேற்ப கூடுதல் வினாக்கள் கொடுக்கப்பட்டுள்ளன.
4. 6ம் வகுப்பு முதல் 9ம் வகுப்பு வரை அனைத்து நூல்களும் அரசுத் தோ்வை நோக்கியே எழுதப்பட்டுள்ளது.

குறி்ப: Loyola Ec புத்தகங்களை 10, 11 பற்றும் 12ம் வகுப்பு மாணவ மாணவிகள் வாங்க்ப் பயின்றால், அரசுத் தேர்வில் அதிக மதிப்பெண் பெற்று உச்சத்தைத் தொடலாம் என்பதை மகிழ்ச்சியுடன் தொிவித்துக் கொள்கறறோம்.

## அสण்படஎ் <br> Loyola Publication

## Contents



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## TERM-I

## UNIT

## NUMBERS

## SUMMARY

* Use of commas helps us in reading and writing large numbers.
* Use of commas differs in the Indian and the International Systems.


## Exercise 1.1

## 1. Fill in the blanks.

(i) The smallest 7 digit number is $\qquad$ .

Ans: 1000000
(ii) The largest 8 digit number is $\qquad$ .

Ans: 99999999
(iii) The place value of 5 in 7005380 is $\qquad$ .
$\qquad$ .

$$
\text { Ans: } 7000000+600000+70000+900+5
$$

2. Say True or False.
(i) Successor of a one digit number is always a one digit number

Ans: False
(ii) Predecessor of a 3-digit number is always a 3 or 4-digit number

Ans: False
(iii) In the Indian System of Numeration the number 67999037 is written as

$$
6,79,99,037
$$

Ans: True
(iv) $88,888=8 \times 10000+8 \times 100+8 \times 10+8 \times 1$

Ans: False
3. How many ten thousands are there in the smallest $\mathbf{6}$ digit number?

Ans: Smallest 6 digit number $=1,00,000$

$$
\frac{100000}{10000}=10
$$

1 Lakh = 10 Ten Thousands
4. Observe the commas and write down the place value of 7 .
(i) 56,74,56,345
(ii) $\mathbf{5 6 7 , 4 5 6 , 3 4 5}$

Ans: (i) 70,00,000 $\quad$ (ii) 7,000,000
5. Write the following numbers in the International System by using commas.
(i) 347056
(ii) 7345671
(iii) 634567105
(iv) $\mathbf{1 2 3 4 5 6 7 8 9 0}$
Ans: (i) 347,056 (ii) $7,345,671$ (iii) $634,567,105$ (iv) $1,234,567,890$
6. Write the largest six digit number and put commas in the Indian and the International Systems.
Ans: Largest 6 digit number $=9,99,999$
Indian System: 9,99,999 (Nine Lakh Ninety Nine Thousand Nine Hundred Ninety Nine)
International System: 999,999 (Nine Hundred Ninety Nine Thousand, Nine Hundred Ninety Nine)
7. Write the number names of the following numerals in the Indian System.
(i) $\mathbf{7 5 , 3 2}, 105$
(ii) 9,75,63,453

Ans: (i) Seventy five lakh thirty two thousand one hundred five
(ii) Nine crore seventy five lakh sixty three thousand four hundred fifty three
8. Write the number names in words using the International System.
(i) $\mathbf{3 4 5 , 6 7 8}$
(ii) $8,343,710$
(iii) 103,456,789

Ans: (i) Three hundred forty five thousand six hundred seventy eight
(ii) Eight million three hundred forty three thousand seven hundred ten
(iii) One hundred three million four hundred fifty six thousand seven hundred eighty nine
9. Write the number name in numerals.
(i) Two crore thirty lakh fifty one thousand nine hundred eighty.
(ii) Sixty six million three hundred forty five thousand twenty seven.
(iii) Seven hundred eighty nine million, two hundred thirteen thousand four hundred fifty six.

Ans:(i) 2,30,51,980 $\quad$ (ii) $66,345,027$ (iii) 789,213,456
10. Tamil Nadu has about twenty six thousand three hundred forty five square kilometre of Forest land. Write the number mentioned in the statement in Indian System and International system.

Ans: 26, 345
11. The number of employees in the Indian Railways is about ten lakhs. Write this in the International System of numeration.

Ans: 1,000,000(one million)

## Objective Type Questions

12. The successor of $\mathbf{1 0}$ million is
(a) 1000001
(b) 10000001
(c) 9999999
(d) 100001
Ans: (b) $\mathbf{1 0 0 0 0 0 0 1}$
13. The difference between the successor and the predecessor of $\mathbf{9 9 9 9 9}$ is
(a) 90000
(b) 1
(c) 2
(d) 99001
Ans: (c) 2
14. 1 billion is equal to
(a) 100 crore
(b) 100 million
(c) 100 lakh
(d) 10000 lakh
Ans: (a) $\mathbf{1 0 0}$ crore
15. The expanded form of the number $6,70,905$ is
a) $6 \times 10000+7 \times 1000+9 \times 100+5 \times 1$
b) $6 \times 10000+7 \times 1000+0 \times 100+9 \times 100+0 \times 10+5 \times 1$
c) $6 \times 1000000+7 \times 10000+0 \times 1000+9 \times 100+0 \times 10+5 \times 1$
d) $6 \times 100000+7 \times 10000+0 \times 1000+9 \times 100+0 \times 10+5 \times 1$

Ans:
d) $6 \times 100000+7 \times 10000+0 \times 1000+9 \times 100+0 \times 10+5 \times 1$

## SUMMARY

Comparing any two numbers, the one with more digits is larger.

* Comparing any two numbers, if the digits are the same, the number that has a greater left most digit is larger.


## Exercise 1.2

1. Fill in the blanks with $>$ or $<$ or $=$.
(i) 48792 $\qquad$ 48972
Ans: <
(ii) 1248654 $\qquad$ 1246854
Ans: >
(iii) 658794 $\qquad$ 658794 Ans: =
2. Say True or False
(i) The difference between the smallest number of seven digits and the largest number of six digits is 10 .

Ans: False
(ii) The largest 4-digit number formed by the digits $8,6,0,9$ using each digit only once is 9086 .

Ans: False
(iii) The total number of 4-digit numbers is 9000 .

Ans: True
3. Of the numbers $\mathbf{1 3 8 6 7 8 7 2 1 5}, \mathbf{1 3 7 6 9 8 8 9 0}, \mathbf{8 6 7 2 0 5 6 0}$, which one is the largest? Which one is the smallest?
Ans: Largest $=1386787215$

$$
\text { Smallest }=86720560
$$

4. Arrange the following numbers in the descending order:

128435, 10835, 21354, 6348, 25840

$$
\text { Ans: } 128435>25840>21354>10835>6348
$$

5. Write any eight digit number with 6 in ten lakhs place and 9 in ten thousandth place.

Ans: 7659423186493725
6. Rajan writes a 3-digit number, using the digits 4,7 and 9 . What are the possible numbers he can write?

Ans: 974, 947, 479, 497, 749, 794
7. The password to access my ATM card includes the digits $\mathbf{9 , 4 , 6}$ and $\mathbf{8}$. It is the smallest 4 digit even number. Find the password of my ATM card.

Ans: 4698
8. Postal Index Number consists of six digits. The first three digits are 6,3 , and 1 . Make the largest and the smallest Postal Index Number by using the digits $\mathbf{0 , 3}$ and 6, each only once.
Ans: Largest Postal Index Number - 631603
Smallest Postal Index Number - 631036
9. The heights(in metres) of the mountains in Tamil Nadu are as follows:

| SI.No | Mountains | Height(in metres) |
| :---: | :---: | :---: |
| 1 | Doddabetta | 2637 |
| 2 | Mahendragiri | 1647 |
| 3 | Anaimudi | 2695 |
| 4 | Velliangiri | 1778 |

(i) Which is the highest mountain listed above?
(ii) Order the mountains from the highest to the lowest.
(iii) What is the difference between the heights of the mountains Anaimudi and Mahendragiri?
Ans:
(i) Anaimudi( 2695 m )
(ii) Anaimudi, Doddabetta, Velliangiri, Mahendragiri
(iii) $2695 \mathrm{~m}-1647 \mathrm{~m}=1048 \mathrm{~m}$

## Objective Type Questions

10. Which list of numbers is in order from the smallest to the largest?
(a) $1468,1486,1484$
(b) $2345,2435,2235$
(c) $134205,134208,154203$
(d) $383553,383548,383642$

Ans: (c) 134205, 134208, 154203
11. The Arabian Sea has an area of 1491000 square miles. This area lies between which two numbers?
(a) 1489000 and 1492540
(b) 1489000 and 1490540
(c) 1490000 and 1490100
(d) 1480000 and 1490000

Ans: (a) 1489000 and 1492540
12. The chart below shows the number of newspapers sold as per Indian Readership Survey in 2018. Which could be the missing number in the table?

| Name of the newspaper | Ranking | Sold (in Lakh) |
| :---: | :---: | :---: |
| A | 1 | 70 |
| B | 2 | 50 |
| C | 3 | $?$ |
| D | 4 | 10 |

(a) 8
(b) 52
(c) 77
(d) 26
Ans: (d) 26

## SUMMARY

* Using BIDMAS, we can avoid the common arithmetic mistakes.
* Large numbers are needed for various situations in our daily life.


## Exercise 1.3

## 1. Fill in the Blanks.

(i) If Arulmozhi saves ₹ 12 per day, then she saves ₹ $\qquad$ in 30 days.

Ans: Rs. 360
(ii) If a person 'A' earns ₹ 1800 in 12 days, then he earns ₹ $\qquad$ in a day.

Ans: Rs 150
(iii) $45 \div(7+8)-2=$ $\qquad$ .
2. Say True or False.
(i) $3+9 \times 8=96$

Ans: False
(ii) $7 \times 20-4=136$

Ans: True
(iii) $40+(56-6) \div 2=45$ Ans: False
3. The number of people who visited the Public Library for the past 5 months were 1200 , 2000, 2450, 3060 and 3200 respectively. How many people visited the library in the last 5 months.
Ans: Total number of people who visited the public library for the past 5 months

$$
\begin{aligned}
& =1200+2000+2450+3060+3200 \\
& =11910
\end{aligned}
$$

4. Cheran had a bank savings of ₹ $\mathbf{7 , 5 0 , 2 5 0}$. He withdrew ₹ $5,34,500$ for educational purpose. Find the balance amount in his account.
Ans: Savings = Rs 7,50,250
Cash withdrawn = Rs 5,34,500
Balance amount $=$ Rs $7,50,250-$ Rs $5,34,500=$ Rs $2,15,750$
5. In a cycle factory, $\mathbf{1 5 6 0}$ bicycles were manufactured every day. Find the number of bicycles manufactured in $\mathbf{2 5}$ days.
Ans: Bicycles manufactured in one day $=1560$
Bicycles manufactured in 25 days $=1560 \times 25$

$$
=39,000 \text { bicycles }
$$

6. ₹. $\mathbf{6 2 5 0 0}$ was equally distributed as a New Year bonus for $\mathbf{2 5}$ employees of a company. How much did each receive?
Ans:
Total amount = Rs 62500
Total number of employees $=25$
Bonus amount received by each employee $=$ Rs $62500 \div 25$

$$
\begin{aligned}
& =\operatorname{Rs} \frac{62500}{25} \\
& =\operatorname{Rs} 2500
\end{aligned}
$$

7. Simplify the following numerical expressions:
(i) $(10+17) \div 3$
(ii) $12-[3-\{6-(5-1)\}]$
(iii) $100+8 \div 2+\{(3 \times 2)-6 \div 2\}$

Ans:
(i) $(10+17) \div 3$

$$
=27 \div 3
$$

(ii) $12-[3-\{6-(5-1)\}]$
(iii) $100+8 \div 2+\{(3 \times 2)-6 \div 2\}$

$$
=\frac{27}{3}
$$

$=12-[3-(6-4)]$

$$
=12-[3-2]
$$

$$
=9
$$

$$
=12-1
$$

$$
=11
$$

$$
\begin{aligned}
& =100+8 \div 2+\{6-3\} \\
& =100+8 \div 2+3 \\
& =100+4+3 \\
& =107
\end{aligned}
$$

## Objective Type Questions

8. The value of $3+5-7 \times 1$ is $\qquad$ .
(a) 5
(b) 7
(c) 8
(d) 1

Ans: d) 1
9. The value of $\mathbf{2 4} \div\{\mathbf{8 - ( 3 \times 2 )}\}$ is
(a) 0
(b) 12
(c) 3
(d) 4

Ans: b) $\mathbf{1 2}$
10. Use BIDMAS and put the correct operator in the box.

2 $\square$ $6-12 \div(4+2)=10$
(a) +
(b) -
(c) $\times$
(d) $\div$

Ans: $(c) \times$

## SUMMARY

* The situations where we do not need the exact quantity give rise to estimation or approx-1 imation.
* Estimation is approximating a quantity to a reasonable accuracy.
* Rounding of a number involves in getting a quick, desired and rough estimate of it.


## Exercise 1.4

1. Fill in the blanks.
(i) The nearest 100 of 843 is $\qquad$ .

Ans: 800
(ii) The nearest 1000 of 756 is $\qquad$ .

Ans: 1000
(iii) The nearest 10000 of 85654 is $\qquad$ Ans: 90000
2. Say True or False.
(i) 8567 is rounded off as 8600 to the nearest 10 .
(ii) 139 is rounded off as 100 to the nearest 100 .
(iii) $1,70,51,972$ is rounded off as $1,70,00,000$ to the nearest lakh.

Ans: False
Ans: True
Ans: False
3. Round off the following to the given nearest place.
(i) 4,065; hundred
(ii) 44,555 ; thousand
(iii) 86,943 ; ten thousand
(iv) $50,81,739$; lakh
(v) $33,75,98,482$; ten crore
Ans: (i) 4100
(ii) 45,000
(iii) 90,000
(iv) $51,00,000$
(v) $30,00,00,000$
4. Estimate the sum of $\mathbf{1 5 7 8 2 6}$ and $\mathbf{3 2 4 6 9}$ rounded off to the nearest ten thousand.

Ans:
157826 +
32469
190295
When rounded off to nearest ten thousand $=1,90,000$
5. Estimate by rounding off each number to the nearest hundred.
(i) $8074+4178$
(ii) $1768977+130589$

Ans: (i) $8074+4178=12,252$
When rounded off to nearest hundred 12,300
(ii) $1768977+130589=18,99,566$

When rounded off to nearest hundred $=18,99,600$
6. The population of a city was $43,43,645$ in the year 2001 and $46,81,087$ in the year 2011. Estimate the increase in population by rounding off to the nearest thousand.
Ans: Population in $2001=43,43,645$
Population in $2011=46,81,087$
Increase in population $=46,81,087-43,43,645=3,37,442$
When rounded off to the nearest thousand $=3,37,000$

## Objective Type Questions

7. The number which on rounding off to the nearest thousand gives $\mathbf{1 1 0 0 0}$ is
(a) 10345
(b) 10855
(c) 11799
(d) 10056
Ans: (b) 10855
8. The estimation to the nearest hundred of 76812 is
(a) 77000
(b) 76000
(c) 76800
(d) 76900
Ans: (c) 76800
9. The number $\mathbf{9 7 8 5 7 6 4}$ is rounded off to the nearest lakh as
(a) 9800000
(b) 9786000
(c) 9795600
(d) 9795000

Ans: (a) 9800000
10. The estimated difference of 167826 and 2765 rounded off to the nearest thousand is
(a) 180000
(b) 165000
(c) 140000
(d) 155000 Ans:
(b) 165000

## SUMMARY

* If zero is included in the collection of Natural numbers ( N ), we get the collection of Whole numbers (W), $\mathrm{W}=\{0,1,2, \ldots\}$.
* ' 0 ' is the smallest whole number.
* ' 0 ' and ' 1 ' are the additive and multiplicative identities of Whole numbers respectively.
* Whole numbers can be added or multiplied in any order and hence commutative.
* Multiplication of Whole numbers is both Commutative and Associative.
* Multiplication is Distributive over addition for Whole numbers.
* Division by ' 0 ' is not defined.


## Exercise 1.5

1. Fill in the blanks.
(i) The difference between the smallest natural number and the smallest whole number is $\qquad$ .

Ans: 1
(ii) $17 \times \quad=34 \times 17$
(iii) When $\qquad$ is added to a number, it remains the same.
(iv) Division by $\qquad$ is not defined.
(v) Multiplication by $\qquad$ leaves a number unchanged.

Ans: Zero
Ans:0
Ans: 1
2. Say True or False.
(i) 0 is the identity for multiplication of whole numbers.
(ii) Sum of two whole numbers is always less than their product.
(iii) Both addition and multiplication are associative for whole numbers.

Ans: False
Ans: False
Ans: True
(iv) Both addition and multiplication are commutative for whole numbers.

Ans: True
Ans: True
(v) Multiplication is distributive over addition for whole numbers.
3. Name the property being illustrated in each of the cases given below.
(i) $75+34=34+75$
(ii) $(12 \times 4) \times 8=12 \times(4 \times 8)$
(iii) $50+0=50$
(Ans:Commutativity for addition)
(iv) $50 \times 1=50$

Ans: Associativity for multiplication
Ans: Zero is the additive identity
(v) $50 \times 42=50 \times 40+50 \times 2$ Ans: Distributivity of multiplication over addition
4. Use the properties of whole numbers and simplify.
(i) $50 \times 102$
(ii) $500 \times 689-500 \times 89$
(iii) $4 \times 132 \times 25$
(iv) $196+34+104$

Ans:
(i) $50 \times 102=50 \times(100+2)=(50 \times 100)+(50 \times 2)$

$$
=5000+100=5100
$$

(ii) $500 \times 689-500 \times 89=500 \times(689-89)=344500-44500$

$$
=300000
$$

$$
500 \times(689-89)=500 \times 600=3,00000
$$

(iii) $(4 \times 132) \times 25=4 \times(132 \times 25)$
$(4 \times 132) \times 25$

$$
\begin{aligned}
& =528 \times 25 \\
& =13200 \\
& 4 \times(132 \times 25) \\
& =4 \times 3300 \\
& =13200
\end{aligned}
$$

(iv) $(196+34)+104=196+(34+104)$
$(196+34)+104=230+104=334$
$196+(34+104)=196+138=334$

## Objective Type Questions

5. $(53+49) \times 0$ is
a) 102
b) 0
c) 1
d) $53+49 \times 0$
Ans: b) 0
6. $\frac{59}{1}$ is
a) 1
b) 0
c) $\frac{1}{59}$
d) 59
Ans: d) 59
7. The product of a non-zero whole number and its successor is always
a) an even number
b) an odd number
c) zero
d) none of these
Ans: a) an even number
8. The whole number that does not have a predecessor is
a) 10
b) 0
c) 1
d) none of these
Ans: b) 0
9. Which of the following expressions is not zero?
a) $2 \times 0$
b) $0+0$
c) $2 / 0$
d) $0 / 2$
Ans: c) 2/0
10. Which of the following is not true?
a) $(4237+5498)+3439=4237+(5498+3439)$
b) $(4237 \times 5498) \times 3439=4237 \times(5498 \times 3439)$
c) $4237+5498 \times 3439=(4237+5498) \times 3439$
d) $4237 \times(5498+3439)=(4237 \times 5498)+(4237 \times 3439)$

Ans: (c) $4237+5498 \times 3439=(4237+5498) \times 3439$

## Exercise 1.6

## Miscellaneous Practice Problems

1. Try to open my locked suitcase which has the biggest 5 digit odd number as the password comprising the digits $\mathbf{7 , 5 , 4 , 3}$ and $\mathbf{8}$. Find the password.
Ans: 87543
2. As per the census of 2001, the population of four states are given below. Arrange the states in ascending and descending order of their population.

| State | Population |
| :--- | :--- |
| Tamil Nadu | 72147030 |
| Rajasthan | 68548437 |
| Madhya Pradesh | 72626809 |
| West Bengal | 91276115 |

Ans:
Ascending order: 6,85,48,437 $<7,21,47,030<7,26,26,809<9,12,76,115$
Descending Order: $9,12,76,115>7,26,26,809>7,21,47,030>6,85,48,437$
3. Study the following table and answer the questions.

| Year | No of Tigers |
| :---: | :---: |
| 1990 | 3500 |
| 2008 | 1400 |
| 2011 | 1706 |
| 2014 | 2226 |

(i) How many tigers were there in 2011?

Ans: 1706
(ii) How many tigers were less in 2008 than in 1990?

Ans: 2100
(iii) Did the number of tigers increase or decrease between 2011 and 2014? If yes, by how much?

Ans: Yes, 2226-1706 = 520 tigers increased from 2011 to 2014
4. Mullaikodi has 25 bags of apples. In each bag there are 9 apples. She shares them equally amongst her 6 friends. How many apples do each get? Are there any apples left over?
Ans:
No of apple bags $=25$
Apples in each bag $=9$
Total no of apples $=25 \times 9=225$
Apples shared among her 6 friends $=225 \div 6$
So, among her 6 friends, each of them get 37 apples and 3 apples are left over.
5. A poultry has produced 15472 eggs and fits 30 eggs in a tray. How many trays do they need?

## Ans:

No of eggs produced $=15472$
No of eggs fits in a tray $=30$
No of trays required $=15472 \div 30$
Trays required $=515+1$ (to fit the remaining 22 eggs) $=516$
Quotient $=515$
Remainder $=22$

## Challenging Problems

6. Read the table and answer the following questions.

| Name of the Star | Diameter(in miles) |
| :---: | :---: |
| Sun | 864730 |
| Sirius | 1556500 |
| Canopus | 25941900 |
| Alpha Centauri | 1037700 |
| Arcturus | 19888800 |
| Vega | 259400 |

(i) Write the Canopus star's diameter in words, in the Indian and the International System.
(ii) Write the sum of the place values of 5 in Sirius star's diameter in the Indian System.
(iii) Eight hundred sixty four million seven hundred thirty. Write in Indian System.
(iv) Write the diameter in words of Arcturus star in the International System
(v) Write the difference of the diameters of Canopus and Arcturus stars in the Indian and the International Systems.
Ans:
(i) $2,59,41,900 \quad 25,941,900$
(i) Indian System: Two crore fifty nine lakh forty one thousand nine hundred

International System: Twenty five million nine hundred forty one thousand nine hundred
(ii) $5,50,500$
(iii) $864,000,730(86,40,00,730)$
(iii) Eighty six crore forty lakh seven hundred thirty
(iv) Nineteen million eight hundred eighty eight thousand eight hundred- $(19,888,800)$
(v) Indian System: 60,53,100 - Sixty lakh fifty three thousand one hundred International System: 6,053,100 - Six million fifty three thousand one hundred
7. Anbu asks Arivu Selvi to guess a five digit odd number. He gives the following hints.
> The digit in the 1000s place is less than 5
> The digit in the 100s place is greater than 6
> The digit in the 10 s place is 8
What is Arivu Selvi answer? Does she give more than one answer?
Ans: 63785
53781
8. A Music concert is taking place in a stadium. A total of 7,689 chairs are to be put in rows of 90. (i) How many rows will there be? (ii) Will there be any chairs left over?
Ans:
Total no of chairs to be put $=7,689$
Chairs in each row $=90$
No of rows $=7689 \div 90$
Hence, $84+1=85$ rows are required to fill 7650 chairs
Chairs left over $=79$ (If the no of rows $=84$ )
9. Round off the seven digit number $29,75,842$ to the nearest lakhs and ten lakhs. Are they the same?
Ans: Yes. Both are same $(30,00,000)$
10. Find the 5 or $\mathbf{6}$ or 7 digit numbers from a newspaper or a magazine to get a rounded number to the nearest ten thousand.

## Ans:

(i) $14276 \simeq 10000$
(ii) $1,86945 \simeq 1,90000$

## UNIT <br> INTRODUCTION TO ALGEBRA

 2
## SUMMARY

* Variables are quantities that can take any value and they are denoted by small alphabets $\mathrm{a}, \mathrm{b}, \mathrm{c}, \ldots, \mathrm{x}, \mathrm{y}, \mathrm{z}$.
* A variable allows us to express relations easily in all practical situations..
* Variables are used to generalise and express many common rules of Geometry and Arithmetic.


## Exercise 2.1

## 1. Fill in the blanks.

(i) The letters $\mathrm{a}, \mathrm{b}, \mathrm{c} \ldots \mathrm{x}, \mathrm{y}, \mathrm{z}$ are used to represent $\qquad$ .
(ii) The algebraic statement of ' f ' decreased by 5 ' is $\qquad$

Ans: Variables

Ans: f-5
(iii) The algebraic statement of 's' divided by 5 ' is $\qquad$ Ans: $\frac{\mathrm{s}}{5}$
(iv) If A's age is ' $n$ ' years now, 7 years ago A's age was $\qquad$ Ans: $\mathbf{n - 7}$
(v) If 'p-5' gives 12 then ' p ' is

Ans: 17

## 2. Say True or False.

(i)


Ans: False
(ii) If the cost of an is ' $x$ ' and the cost of a $\qquad$ is ₹ 5 , then the total cost of fruits is $₹$. ' $x+5$ '.

Ans: True
(iii) 10 more to three times ' $\mathrm{c}^{\prime}$ is ' $10 \mathrm{c}^{+} 3$ '
(iv) If the cost of 10 rice bag is ₹ ' t ', then the cost of 1 rice bag is $₹ \frac{\mathrm{t} \mathrm{t} \text { ' }}{10}$
(v) The product of ' q ' and 20 is ' 20 q '

Ans: False
Ans: True
Ans: True

## 3. Draw the next two patterns and complete the table



| Shapes | $\mathbf{1}^{\text {st }}$ Pattern | $\mathbf{2}^{\text {nd }}$ Pattern | $3^{\text {rd }}$ Pattern | $4^{\text {th }}$ Pattern | $\mathbf{5}^{\text {th }}$ Pattern |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Squares | 1 | 2 | 3 |  |  |
| Circles | 1 | 2 | 3 |  |  |
| Triangles | 2 | 4 | 6 |  |  |

Ans:

| Shapes | $\mathbf{1}^{\text {st }}$ Pattern | $2^{\text {nd }}$ Pattern | $\mathbf{3}^{\text {rd }}$ Pattern | $\mathbf{4}^{\text {th }}$ Pattern | $\mathbf{5}^{\text {th }}$ Pattern |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Squares | 1 | 2 | 3 | 4 | 5 |
| Circles | 1 | 2 | 3 | 4 | 5 |
| Triangles | 2 | 4 | 6 | 8 | 10 |

4. Arivazhagan is $\mathbf{3 0}$ years younger to his father. Write Arivazhagan's age in terms of his father's age.
Ans: Let Arivazhagan's father's age be x years According to the problem,
Arivazhagan's age $=(x-30)$ years
5. If ' $u$ ' is an even number, how would you represent
(i) the next even number?
(ii) the previous even number?

Ans: (i) $\mathrm{u}+2$
(ii) $u-2$
6. Express the following verbal statement to algebraic statement.
(i) ' $t$ ' is added to 100 .
Ans: $\mathrm{t}+100$
(ii) 4 times ' $q$ '.
Ans: $4 q$
(iii) 4 less to 9 times of ' $y$ '.
Ans: $9 y-4$
7. Express the following algebraic statement to verbal statement.
(i) $x \div 3$
Ans: $x$ divided by 3
(ii) $11+10 x$
Ans: 11 added to 10 times $x$
(iii) 70 s
Ans: 70 times s
8. The teacher asked two students to write the algebraic statement for the verbal statement " 8 more than a number". Vetri wrote ' $8+x$ ' but Maran wrote ' $8 x$ '. Who gave the correct answer?
Ans: Vetri
9. Answer the following questions.
(i) If ' g ' is equal to 300 what is the value of ' $\mathrm{g}-1$ ' and ' $\mathrm{g}+1$ '?
(ii) What is the value of ' $s$ ', if ' $2 s-6$ ' gives 30 ?

Ans:
(i) $\mathrm{g}=300$
$\mathrm{g}-1=300-1=299$
$g+1=300+1=301$
(ii) $2 \mathrm{~s}-6=30$
$2 \mathrm{~s}=30+6$
$2 \mathrm{~s}=36$
$\mathrm{s}=36 / 2$
$\mathrm{s}=18$
10. Complete the table and find the value of ' $k$ ' for which ' $k / 3$ ' gives 5 .

| k | 3 | 6 | 9 | 12 | 15 | 18 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\frac{k}{3}$ | 1 | 2 |  |  |  |  |

Ans:

| K | 3 | 6 | 9 | 12 | 15 | 18 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\frac{k}{3}$ | 1 | 2 | 3 | 4 | 5 | 6 |

$$
\begin{aligned}
& \frac{k}{3}=5 \\
& k=15
\end{aligned}
$$

## Objective Type Questions

## 11. Variable means that it

a) can take only a few values
b) has a fixed value
c) can take different values
d) can take only 8 values

Ans: c) can take different values
12. The number of days in ' $w$ ' weeks is
a) $30+\mathrm{w}$
b) 30 w
c) $7+w$
d) 7 w
Ans: d) 7 w
13. The value of ' $x$ ' in the circle is

a) 6
b) 8
c) 21
d) 22
Ans: d) 22
14. The value of ' $y$ ' in $y+7=13$ is
a) $y=5$
b) $y=6$
c) $y=7$
d) $y=8$
Ans: b) $y=6$

15． 6 less to＇$n$＇gives 8 is represented as
a）$n-6=8$
b） $6-\mathrm{n}=8$
c） $8-\mathrm{n}=6$
d）$n-8=6$

Ans：a） $\mathbf{n - 6}=8$

## Exercise 2.2

## Miscellaneous Practice Problems

1．Complete the following pattern．

9－1＝
98－21＝
987－321＝
9876－4321＝
$98765-54321=$
What comes next？

Ans： $9-1=8$
Ans：98－21＝77
Ans：987－321＝666
Ans：9876－4321＝5555
Ans： $98765-54321=44444$
Ans：987654－654321＝ 333333

2．A piece of wire is＇ 12 s ＇ $\mathbf{c m}$ long．What will be the length of the side，if it is formed as
（i）an equilateral triangle
（ii）a square
Ans：（i）4s
（ii） 3 s

3．Identify the value of the shapes and figures in the table given below and verify their addition horizontally and vertically．

| 大 | $\because$ | （1） | ＊ | $=30$ |
| :---: | :---: | :---: | :---: | :---: |
| 大 | ＊ | $\wedge$ | $\wedge$ | $=36$ |
| 大 | $\wedge$ | （1） | （1） | ＝ |
| 大 | $\because$ | $\triangle$ | （1） | ＝ |
| $=32$ | $=$ | $=$ | ＝ | $=$ |

Ans：

| 8 | 7 | 7 | 8 | $=30$ |
| :---: | :---: | :---: | :---: | :---: |
| 8 | 8 | 10 | 10 | $=36$ |
| 8 | 10 | 7 | 7 | $=32$ |
| 8 | 7 | 10 | 7 | $=32$ |
| $=32$ | $=32$ | $=34$ | $=32$ | $=130$ |

4．The table given below shows the results of the matches played by 8 teams in a kabaddi championship tournament．

| Teams | A | B | C | $\mathbf{D}$ | $\mathbf{E}$ | F | G | H |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Total Matches played | 8 | 7 | n | a | 9 | 10 | 8 | y |


| Matches won | 5 | 6 | 4 | 7 | b | 6 | x | 3 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Matches lost | k | m | 6 | 2 | 3 | c | 4 | 6 |

Find the value of all the variables in the table given above.
Ans: $\mathrm{k}=3, \mathrm{~m}=1, \mathrm{n}=10, \mathrm{a}=9, \mathrm{~b}=6, \mathrm{c}=4, \mathrm{x}=4, \mathrm{y}=9$

## Challenging Problems

5. Gopal is 8 years younger to Karnan. If the sum of their ages is $\mathbf{3 0}$, how old is Karnan?

Ans: Let the age of Karnan be x years
Gopal's age $=x-8$
Acc to the problem,
$x+x-8=30$
$2 x-8=30$
$2 x=30+8$
$2 x=38$
$x=\frac{38}{2}$
$x=19$
Age of Karnan $=19$ years
6. The rectangles made of identical square blocks with varying lengths but having only two square blocks as width are given below


P


Q


R


S


T
(i) How many small size squares are there in each of the rectangles $\mathrm{P}, \mathrm{Q}, \mathrm{R}$ and S ?
(ii) Fill in the boxes.

| Rectangle | P | Q | R | S | T |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Number of small size squares along the breadth | 2 | 2 | $?$ | 2 | 2 |
| Number of squares along the length | 1 | 4 | 3 | $?$ | $x$ |
| Total number of squares in rectangle | $?$ | 8 | $?$ | 10 | $?$ |

Ans: (i) $P=2 ; Q=8 ; R=6 ; S=10$

| Rectangle | $\mathbf{P}$ | $\mathbf{Q}$ | $\mathbf{R}$ | $\mathbf{S}$ | $\mathbf{T}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Number of small size squares along the breadth | 2 | 2 | 2 | 2 | 2 |

EC $6^{\text {th }}$ Maths

| Number of squares along the length | 1 | 4 | 3 | 5 | $x$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Total number of squares in rectangle | 2 | 8 | 6 | 10 | $2 x$ |

7. Find the variables from the clues given below and solve the cross-word puzzle.


| Across | Down |
| :--- | :--- |
| $x+40$ gives 100 | $x$ is 1005 multiplied by 6 |
| 7 reduced from t gives 31 | $t \div 7=5$ |
| z is 5 added 5 times | $p$ is the predecessor of first 3 digit number |
| $v$ is the whole number zero plus number of <br> days in a Ordinary year | z is the number of weeks in a year (digits |
| reversed) |  |

Ans:

| ${ }^{x} 6$ | 0 |  | ${ }^{t}$ | 3 | 8 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 |  | $z^{2}$ | 2 |  | 5 |  |
| $p$ | 9 |  |  |  |  |  |
| ${ }^{v} 3$ |  | 6 |  | 5 |  | ${ }^{k}$ |$|$

## UNIT

## RATIO AND PROPORTION

## SUMMARY

* A ratio is a comparison of two quantities by division.
* Ratios are often expressed as fractions in the simplest form.
* A ratio has no unit.
* Two quantities of a ratio should be in the same unit.
* Order of the terms in a ratio cannot be reversed.

Exercise 3.1

1. Fill in the blanks.
(i) Ratio of ₹ 3 to ₹ $5=$ $\qquad$ .

Ans: 3 : 5
(ii) Ratio of 3 m to $200 \mathrm{~cm}=$ $\qquad$ .

Ans: 3 : 2
(iii) Ratio of 5 km 400 m to $6 \mathrm{~km}=$ $\qquad$ .
(iv) Ratio of 75 paise to $₹ 2=$ $\qquad$ .
2. Say whether the following statements are True or False.
(i) The ratio of 130 cm to 1 m is $13: 10$.

Ans: True
(ii) One of the terms in a ratio cannot be 1 Ans: False
3. Find the simplified form of the following ratios.
(i) $15: 20$
(ii) $32: 24$
(iii) $7: 15$
(iv) $12: 27$
(v) $75: 100$

Ans:
(i) $15: 20=\frac{15}{20}=\frac{3}{4}=3: 4$
(ii) $32: 24=\frac{32}{24}=\frac{4}{3}=4: 3$
(iii) $7: 15$
(iv) $12: 27=\frac{12}{27}=4: 9$
(v) $75: 100=\frac{75}{100}=3: 4$
4. Akilan walks 10 km in an hour while Selvi walks 6 km in an hour. Find the simplest ratio of the distance covered by Akilan to that of Selvi.
Ans: Ratio of the distance covered by Akilan to that of Selvi $=10 \mathrm{~km}: 6 \mathrm{~km}$

$$
=\frac{10}{6}=\frac{5}{3}=5: 3
$$

5. The cost of parking a bicycle is ₹ 5 and the cost of parking a scooter is ₹ 15 . Find the simplest ratio of the parking cost of a bicycle to that of a scooter.
Ans: Ratio of the parking cost of a bicycle to that of a scooter $=$ Rs $5:$ Rs 15

$$
=\frac{5}{15}=\frac{1}{3}=1: 3
$$

6. Out of $\mathbf{5 0}$ students in a class, $\mathbf{3 0}$ are boys. Find the ratio of
(i) number of boys to the number of girls.
(ii) number of girls to the total number of students.
(iii) number of boys to the total number of students.

Ans: Total no of students $=50$
No of boys $=30$
No of girls $=50-30=20$
(i) Ratio of boys to girls $=30: 20=\frac{30}{20}=\frac{3}{2}=3: 2$
(ii) Ratio of girls to the total no of students $=20: 50=\frac{20}{50}=\frac{2}{5}=2: 5$
(iii)Ratio of boys to the total no of students $=30: 50=\frac{30}{50}=\frac{3}{5}=3: 5$

## Objective Type Questions

7. The ratio of ₹ $\mathbf{1}$ to $\mathbf{2 0}$ paise is $\qquad$
a) $1: 5$
b) $1: 2$
c) $2: 1$
d) $5: 1$
Ans: d) $5: 1$
8. The ratio of $\mathbf{1} \mathbf{1}$ to 50 ml is $\qquad$
a) $1: 5$
b) $1: 20$
c) $20: 1$
d) $5: 1$
Ans: c) $20: 1$
9. The length and breadth of a window are in 1 m and 70 cm respectively. The ratio of the length to the breadth is $\qquad$
a) $1: 7$
b) $7: 1$
c) $7: 10$
d) $10: 7$
Ans: d) $10: 7$
10. The ratio of the number of sides of a triangle to the number of sides of a rectangle is
a) $4: 3$
b) $3: 4$
c) $3: 5$
d) $3: 2$
Ans: b) $3: 4$
11. If Azhagan is $\mathbf{5 0}$ years old and his son is $\mathbf{1 0}$ years old then the simplest ratio between the age of Azhagan to his son is
a) $10: 50$
b) $50: 10$
c) $5: 1$
d) $1: 5$
Ans: c) $5: 1$

## SUMMARY

To get an equivalent ratio, multiply or divide the numerator and denominator by the same number.

## Exercise 3.2

1. Fill in the blanks for the given equivalent ratios.
(i) $3: 5=9$ : $\qquad$ (ii) $4: 5=$ : 10 (iii) 6 : $\qquad$ $=1: 2$

Ans: (i) $\mathbf{3}: 5=9: x$
(ii) $4: 5=x: 10$

$$
\begin{array}{ll}
\frac{3}{5}=\frac{9}{x} & \frac{4}{5}=\frac{x}{10} \\
3 \times x=9 \times 5 & 5 \times x=4 \times 10 \\
\mathrm{x}=\frac{9 \times 5}{3} & \mathrm{x}=\frac{4 \times 10}{5} \\
\mathrm{x}=15 & \mathrm{x}=\frac{4 \times 10}{5} \\
3: 5=9: 15 & x=8
\end{array}
$$

(iii) $6: \ldots=1: 2$

$$
6: x=1: 2
$$

$$
\begin{aligned}
& \frac{6}{x}=\frac{1}{2} \\
& 1 \times x=6 \times 2 \\
& x=12
\end{aligned}
$$

$$
6: 12=1: 2
$$

2. Complete the table.
(i)

| Feet | 1 | 2 | 3 | $?$ |
| :---: | :---: | :---: | :---: | :---: |
| Inch | 12 | 24 | $?$ | 72 |

(ii)

| Days | 28 | 21 | $?$ | 63 |
| :---: | :---: | :---: | :---: | :---: |
| Weeks | 4 | 3 | 2 | $?$ |

Ans: (i) 1 feet $=12$ inches
3 feet $=3 \times 12$ inches $=36$ inches
72 inches $=6 \times 12$ inches $=6$ feet
(ii) 1 week $=7$ days

2 weeks $=2 \times 7$ days $=14$ days
63 days $=9 \times 7$ days $=9$ weeks

## 3. Say True or False.

(i) $5: 7$ is equivalent to $21: 15$.

Ans: False
(ii) If 40 is divided in the ratio $3: 2$, then the larger part is 24 .

Ans: True
4. Give two equivalent ratios for each of the following.
(i) $3: 2$
(ii) $1: 6$
(iii) $5: 4$
(i) $3: 2=\frac{3}{2}=\frac{3 \times 2}{2 \times 2}=\frac{3 \times 3}{2 \times 3}$

$$
\frac{3}{2}=\frac{6}{4}=\frac{9}{6}
$$

$$
3: 2=6: 4=9: 6
$$

(ii) $1: 6=\frac{1}{6}=\frac{1 \times 2}{6 \times 2}=\frac{1 \times 3}{6 \times 3}$
$\frac{1}{6}=\frac{2}{12}=\frac{3}{18}$
$1: 6=2: 12=3: 18$
(iii) $5: 4=\frac{5}{4}=\frac{5 \times 2}{4 \times 2}=\frac{5 \times 3}{4 \times 3}$

$$
\begin{aligned}
& \frac{5}{4}=\frac{10}{8}=\frac{15}{12} \\
& 5: 4=10: 8=15: 12
\end{aligned}
$$

5. Which of the two ratios is larger?
(i) $4: 5$ or $8: 15$
(ii) $3: 4$ or $7: 8$
(iii) $1: 2$ or $2: 1$
(i) $4: 5$ (or) $8: 15$
(ii) $3: 4$ (or) $7: 8$
(iii) $1: 2$ (or) $2: 1$
$3: 4=\frac{3}{4}$
$1: 2=\frac{1}{2}$
$4: 5=\frac{4}{5}$
$8: 15=\frac{8}{15}$
$\frac{4 \times 15}{5 \times 15}=\frac{60}{75}$
$\frac{8 \times 5}{15 \times 5}=\frac{40}{75}$
$7: 8=\frac{7}{8}$
$\frac{3 \times 8}{4 \times 8}=\frac{24}{32}$
$\frac{7 \times 4}{8 \times 4}=\frac{28}{32}$
$2: 1=\frac{2}{1}$
$\frac{60}{75}>\frac{40}{75}$
$\frac{28}{32}>\frac{24}{32}$
$\frac{4}{5}>\frac{8}{15} \quad 4: 5>8: 15$
$\frac{7}{8}>\frac{3}{4}$
$7: 8>3: 4$
6. Divide the numbers given below in the required ratio.
(i) 20 in the ratio $3: 2$
(ii) 27 in the ratio $4: 5$
(iii) 40 in the ratio $6: 14$
(i) Ratio $=3: 2$

Sum of the ratio $=3+2=5$
5 parts $=20$

1 part $=\frac{20}{5}=4$
3 parts $=3 \times 4=12$
2 parts $=2 \times 4=8$
20 can be divided in the form as 12,8
(ii) Ratio $=4: 5$

Sum of the ratio $=4+5=9$
9 parts $=27$
1 part $=\frac{27}{9}=3$
4 parts $=4 \times 3=12$
5 parts $=5 \times 3=15$
27 can be divided in the form as 12,15
(iii) 40 in the ratio $6: 14$

Ratio $=6: 14$
Sum of the ratio $=6+14=20$
20 parts $=40$
1 part $=\frac{40}{20}=2$
6 parts $=2 \times 6=12$
14 parts $=2 \times 14=28$
40 can be divided in the form as 12,28
7. In a family, the amount spent in a month for buying Provisions and Vegetables are in the ratio $3: 2$. If the allotted amount is $₹ 4000$, then what will be the amount spent for (i) Provisions and (ii) Vegetables?

Ans: Allotted amount $=$ Rs 4000
Ratio $=3: 2$
Sum of the ratio $=3+2=5$
5 parts $=$ Rs 4000
1 part $=$ Rs $\frac{4000}{5}=$ Rs 800
Provisions: Vegetables $=3: 2$

3 parts $=3 \times$ Rs $800=$ Rs 2400
2 parts $=2 \times$ Rs $800=$ Rs 1600
Amount spent for provisions = Rs 2400
Amount spent for vegetables $=$ Rs 1600
8. A line segment 63 cm long is to be divided into two parts in the ratio $3: 4$. Find the length of each part.
Ans: Total length $=63 \mathrm{~cm}$
Ratio $=3: 4$
Sum of the ratio $=3+4=7$
7 parts $=63 \mathrm{~cm}$
1 part $=\frac{63}{7}=9 \mathrm{~cm}$
3 parts $=3 \times 9 \mathrm{~cm}=27 \mathrm{~cm}$
4 parts $=4 \times 9 \mathrm{~cm}=36 \mathrm{~cm}$
$\therefore 63 \mathrm{~cm}$ can be divided into the parts as 27 cm and 36 cm .

## Objective Type Questions

9. If 2:3 and 4:--- are equivalent ratios, then the missing term is
a) 6
b) 2
c) 4
d) 3

Ans: a) 6
10. An equivalent ratio of $4: 7$ is
a) $1: 3$
b) $8: 15$
c) $14: 8$
d) $12: 21$
Ans: d) 12 : 21
11. Which is not an equivalent ratio of $\frac{16}{24}$ ?
a) $\frac{6}{9}$
b) $\frac{12}{18}$
c) $\frac{10}{15}$
d) $\frac{20}{28}$
Ans: d) $\frac{20}{28}$
12. If $₹ 1600$ is divided among $A$ and $B$ in the ratio $3: 5$ then, $B$ 's share is $\qquad$ .
a) ₹480
b) ₹ 800
c) $₹ 1000$
d) ₹200
Ans: c) ₹ 1000

## SUMMARY

* When two ratios are equal, they are said to be in proportion.
* The proportionality law states that the product of the extremes is equal to the product of the means.


## Exercise 3.3

1. Fill in the boxes.
(i) $3: 5:$ : $\square$ : 20

Ans: 12
(ii) $\square: 24:: 3: 8$

Ans: 9
(iii) 5 : $\square$ : $: 10: 8:: 15:$ $\square$
(iv) $12: \square=\square: 4=8: 16$

Ans: 24, 2
2. Say True or False.
(i) 7 Persons is to 49 Persons as 11 kg is to 88 kg

Ans: False
(ii) 10 books is to 15 books as 3 books is to 15 books
(iii) If the weight of 40 books is 8 kg , then the weight of 15 books is 3 kg .

Ans: False
Ans: True
(iv) A car travels 90 km in 3 hours with constant speed. It will travel 140 km in 5 hours at the same speed.

Ans: False
3. Fill in the blanks.
(i) If the cost of 3 pens is $₹ 18$, then the cost of 5 pens is $\qquad$ .

Ans: ₹. 30
(ii) If Karkuzhali earns ₹ 1800 in 15 days, then she earns ₹ 3000 in __days.

Ans: 25
4. Find whether 12, 24, 18, 36 are in order that can be expressed as two ratios that are in proportion.
Ans: Yes, they are in proportion

$$
\begin{aligned}
& 12: 24=18: 36 \\
& \frac{12}{24}=\frac{1}{2} \quad \text { Product of means }=24 \times 18=432 \\
& \frac{18}{36}=\frac{1}{2} \quad \text { Product of extremes }=12 \times 36=432
\end{aligned}
$$

Hence $a \times d=\mathrm{b} \times \mathrm{c}$
5. Write the mean and extreme terms in the following ratios and check whether they are in proportion.
(i) 78 litre is to 130 litre and 12 bottles is to 20 bottles
(ii) 400 gm is to 50 gm and 25 rupees is to 625 rupees

Ans: (i) $78: \mathbf{1 3 0}, 12: 20$
Product of the means $=78 \times 20=1560$
Product of the extremes $=130 \times 12=1560$
$a \times d=\mathrm{b} \times \mathrm{c} \therefore$ They are in proportion
(ii) $400: 50,25: 625$

Product of the extremes $=400 \times 625=250000$
Product of the means $=50 \times 25=1250$
$a \times d \neq \mathrm{b} \times \mathrm{c} \therefore$ They are not in proportion
6. The America's famous Golden Gate bridge is $\mathbf{6 4 8 0}$ ft long with 756 ft tall towers. A model of this bridge exhibited in a fair is 60 ft long with 7 ft tall towers. Is the model in proportion to the original bridge?
Ans:
6480:756, $60: 7$


Product of the means $=756 \times 60=45360$
Product of the extremes $=6480 \times 7=45360$
$\mathrm{ad}=\mathrm{bc}$
$\therefore$ They are in proportion
7. If a person reads $\mathbf{2 0}$ pages of a book in $\mathbf{2}$ hours, how many pages will he read in $\mathbf{8}$ hours at the same speed?
Ans: In 2 hours, pages read $=20$
In 1 hour, pages read $=\frac{20}{2}=10$
In 8 hours, pages read $=10 \times 8=80$ pages
8. Cholan walks $\mathbf{6} \mathbf{~ k m}$ in $\mathbf{1}$ hour at constant speed. Find the distance covered by him in 20 minutes at the same speed.
Ans: In 1 hour ( 60 minutes), distance covered $=6 \mathrm{~km}$
In 1 minute, distance covered $=\frac{6 \mathrm{~km}}{60 \mathrm{~min}}=\frac{6000 \mathrm{~m}}{60}=100 \mathrm{~m}$
In 20 minutes, distance covered $=20 \times 100 \mathrm{~m}=2000 \mathrm{~m}=2 \mathrm{~km}$
9. The number of correct answers given by Kaarmugilan and Kavitha in a quiz competition are in the ratio $10: 11$. If they had scored a total of 84 points in the competition, then how many points did Kavitha get?
Ans: Total points scored $=84$
Ratio $=10: 11$
Sum of the ratio $=10+11=21$
21 parts $=84$ points
1 part $=\frac{84}{21}=4$ points

Kavitha $=11$ parts
Kaarmugilan $=10$ parts
Points scored by Kavitha $=11$ parts $=11 \times 4$ points $=44$ points
10. Karmegan made 54 runs in 9 overs and Asif made 77 runs in 11 overs. Whose run rate is better? (run rate $=$ ratio of runs to overs)
Ans: Karmegam
Runs made in 9 overs $=54$
Runs made in 1 over $=\frac{54}{9}=6$ runs
Asif
Runs made in 11 overs $=77$
Runs made in 1 over $=\frac{77}{11}=7$ runs
$\therefore$ Asif's run rate is better than Karmegam
11. You purchase 6 apples for $₹ 90$ and your friend purchases 5 apples for $₹ 70$. Whose purchase is better?
Ans: Myself
Cost of 6 apples $=$ Rs 90
Cost of 1 apple $=\frac{R s 90}{6}=$ Rs 15
Friend's purchase
Cost of 5 apples $=$ Rs 70
Cost of 1 apple $=\frac{70}{5}=$ Rs 14
$\therefore$ Friend's purchase is better than myself

## Objective Type Questions

12. Which of the following ratios are in proportion?
a) $3: 5,6: 11$
b) $2: 3,9: 6$
c) $2: 5,10: 25$
d) $3: 1,1: 3$
Ans: c) 2:5, $10: 25$
13. If the ratios formed using the numbers $2,5, x, 20$ in the same order are in proportion, then ' $x$ ' is
a) 50
b) 4
c) 10
d) 8
Ans: d) 8
14. If $7: \mathbf{5}$ is in proportion to $x: 25$, then ' $x$ ' is
a) 27
b) 49
c) 35
d) 14
Ans: c) 35
15. If a Barbie doll costs ₹ 90 , then the cost of $\mathbf{3}$ such dolls is ₹ $\qquad$ .
a) 260
b) 270
c) 30
d) 93
Ans: b) 270
16. If a man walks $\mathbf{2} \mathbf{k m}$ in $\mathbf{1 5}$ minutes, then he will walk $\qquad$ km in 45 minutes.
a) 10
b) 8
c) 6
d) 12
Ans: c) 6

## Exercise 3.4

## Miscellaneous Practice Problems

1. The maximum speed of some of the animals are given below:
the Elephant $=20 \mathrm{~km} / \mathrm{h}$; the Lion $=80 \mathrm{~km} / \mathrm{h}$; the Cheetah $=100 \mathrm{~km} / \mathrm{h}$
Find the following ratios of their speeds in simplified form and find which ratio is the least?
(i) the Elephant and the Lion
(ii) the Lion and the Cheetah
(iii) the Elephant and the Cheetah

Ans: (i) The Elephant : the Lion
$=20: 80=\frac{20}{80}=\frac{1}{4}=1: 4$
(ii) the Lion : the Cheetah

$$
=80: 100=\frac{80}{100}=\frac{4}{5}=4: 5
$$

(iii) the Elephant : the Cheetah
$=20: 100=\frac{20}{100}=\frac{1}{5}=1: 5$
The ratio of Elephant to Cheetah is the least
2. A particular high school has $\mathbf{1 5 0 0}$ students $\mathbf{5 0}$ teachers and $\mathbf{5}$ administrators. If the school grows to 1800 students and the ratios are maintained, then find the number of teachers and administrators.
Ans:
Administrators: teachers: students

$$
=5: 50: 1500=1: 10: 300
$$

If the school grows to 1800 students then 10 parts = teachers
1 part $=$ administrators
300 parts $=1800$
1 part $=\frac{1800}{300}=6$
10 parts $=6 \times 10=60$

So, if the school grows to 1800 students the new ratio is administrators : teachers : students 6:60:1800
3. I have a box which has $\mathbf{3}$ green, $\mathbf{9}$ blue, $\mathbf{4}$ yellow, $\mathbf{8}$ orange coloured cubes in it.
(a) What is the ratio of orange to yellow cubes?
(b) What is the ratio of green to blue cubes?
(c) How many different ratios can be formed, when you compare each colour to anyone of the other colours?
Ans:
(i) orange : Yellow $=8: 4=2: 1$
(ii) green: blue $=3: 9=1: 3$
(iii) green : orange $=3: 8$
blue : orange $=9: 8$
green : yellow $=3: 4$
blue : yellow $=9: 4$
green : blue $=3: 9=1: 3$
yellow : orange $=4: 8=1: 2$

$$
\begin{aligned}
& \text { orange }: \text { green }=8: 3 \\
& \text { orange }: \text { blue }=8: 9 \\
& \text { yellow }: \text { green }=4: 3 \\
& \text { yellow }: \text { blue }=4: 9 \\
& \text { blue }: \text { green }=9: 3=3: 1 \\
& \text { orange }: \text { yellow }=8: 4=2: 1
\end{aligned}
$$

4. A gets double of what $B$ gets and $B$ gets double of what $C$ gets. Find $A: B$ and $B: C$ and verify whether the result is in proportion or not.
Ans:
A: B $=2: 1$
B: C $=2: 1$
They are in proportion
5. The ingredients required for the preparation of Ragi Kali, a healthy dish of Tamilnadu is given below.

| Ingredients | Quantity |
| :---: | :---: |
| Ragi flour | 4 cups |
| Raw rice broken | 1 cup |
| Water | 8 cups |
| Sesame oil | 15 ml |
| Salt | 10 mg |

(a) If one cup of ragi flour is used then, what would be the amount of raw rice required?
(b) If 16 cups of water is used, then how much of ragi flour should be used?
(c) Which of these ingredients cannot be expressed as a ratio? Why?

Ans: (i) $\frac{1}{4}$ cup
(ii) 8 cups
(iii) Ragi flour, Raw rice and water are in one unit. Sesame oil and salt are in different units. These different units cannot be compared and cannot be expressed as a ratio because the two quantities of a ratio should be in the same unit.

## Challenging Problems

6. Antony brushes his teeth in the morning and night on all days in a week. Shabeen brushes her teeth only in the morning. What is the ratio of the number of times they brush their teeth in a week?
Ans: Number of times $=14: 7=2: 1$
7. Thirumagal's mother wears a bracelet made of 35 red beads and 30 blue beads. Thirumagal wants to make smaller bracelets using the same two coloured beads in the same ratio. In how
 many different ways can she make the bracelets?
Ans: Red : blue $=35: 30=7: 6$
Different ways (i) $7: 6$
(ii) $14: 12$; (iii) $21: 18$; (iv) $28: 24$
8. Team A wins 26 matches out of 52 matches. Team $B$ wins three-fourth of 52 matches played. Which team has a better winning record?
Ans:
Team $\mathrm{A}=\frac{26}{52}=\frac{1}{2}$
Team $B=\frac{3}{4} \times 52=\frac{3}{4} \times 52=39$
Team B has a better winning record
9. In a school excursion, 6 teachers and 12 students from 6th standard and 9 teachers and 27 students from 7th standard, 4 teachers and 16 students from 8th standard took part. Which class has the least teacher to student ratio?
Ans: Std VI - teachers : students $=6: 12=1: 2$
Std VII - teachers : students $=9: 27=1: 3$
Std VIII - teachers : students $=4: 16=1: 4$
Std VIII has the least ratio
10. Fill the boxes using any set of suitable numbers 6 : $\square$ : : $\square$ : 15.
Ans:
6 : $\qquad$ $=$ $\qquad$ : 15
Product of the extremes $=6 \times 15=90$
Set of suitable numbers
1 and 90, 2 and 45, 3 and 30, 5 and 18, 6 and 15
11. From your school diary, write the ratio of the number of holidays to the number of working days in the current academic year.
Ans: $\quad$ Number of holidays $=145$
Number of working days $=220$
Holidays $:$ working days $=145: 220=\frac{145}{220}=\frac{29}{44}=29: 44$
12. If the ratio of Green, Yellow and Black balls in a bag is $4: 3: 5$, then
(a) Which is the most likely ball that you can choose from the bag?
(b) How many balls in total are there in the bag if you have 40 black balls in it?
(c) Find the number of green and yellow balls in the bag.

Ans: Green : Yellow : Black $=4: 3: 5$
(i) Black balls;
(ii) 96 balls $(32+24+40)$;
(iii) green balls $=32$
yellow balls $=24$


