

**QUARTERLY SEPTEMBER 2023**  
**10<sup>TH</sup> MATHS KEY ANSWER ( CHENNAI )**

**I CHOOSE THE CORRECT ANSWER**

1. c            3
2. a            ( 8, 6 )
3. d            Quadratic
4. b            2
5. a            1
6. b             $k^2$
7. b             $(y + \frac{1}{y})^2$
8. c            - 1, 2
9. d             $5\sqrt{2}$
10. a           1.4 cm
11. b           Parallel to Y – axis
12. d            $-\frac{a}{b}$
13. b            $x + y = 3, 3x + y = 7$
14. d            $\cot \theta$

**II ANSWER ANY 10 ONLY**

15. Domain       = { 0, 1, 2, 3, 4, 5 }  
Range            = { 3, 4, 5, 6, 7, 8 }
16.  $\Rightarrow f(x^2) = (f(x))^2$   
 $\Rightarrow 3 - 2x^2 = (3 - 2x)^2$   
 $\Rightarrow x^2 - 2x + 1 = 0$   
 $\Rightarrow (x - 1)(x - 1) = 0 \quad \therefore x = 1$
17. image of 1 = 5 & image of 2 = 8  
Preimage of 29 is 9 & Preimage of 53 is 17
18.  $2^a \times 3^b = 13824$   
 $2^a \times 3^b = 2^9 \times 3^3$   
 $\therefore a = 9 \text{ and } b = 3$
19.  $a_8 = \frac{63}{11}$  &  $a_{15} = \frac{225}{31}$
20. Here  $a = 3$  and  $r = \frac{t_2}{t_1} = \frac{1}{3}$   
 $\Rightarrow S_\infty = \frac{a}{1-r} = \frac{3}{1-\frac{1}{3}}$   
 $\Rightarrow S_\infty = \frac{3}{1} \times \frac{3}{2} = \frac{9}{2}$
21.  $x(x + 3)(x - 2) = 0$   
Therefore excluded values are  $x = 0, 2 \text{ \& } -3$
22.  $x^2 - (SOR)x + POR = 0$   
 $x^2 + 9x + 20 = 0$
23.  $\frac{\text{Area}(\Delta ABC)}{\text{Area}(\Delta DEF)} = \frac{BC^2}{EF^2} \Rightarrow \frac{54}{\text{Area}(\Delta DEF)} = \frac{3^2}{4^2}$   
 $\text{Area}(\Delta DEF) = \frac{16 \times 54}{9} = 96\text{cm}^2$

$$24. \frac{AD}{AB} = \frac{AE}{AC} = \frac{3}{4} = \frac{x}{15-x}$$

$$3(15-x) = 4x \Rightarrow x = \frac{45}{7} = 6.43\text{cm.}$$

$$25. \frac{3-a}{9+2} = \frac{-1}{2} \quad a = \frac{17}{2}$$

$$26. x\text{-intercept} = -9$$

$$Y\text{-intercept} = 4$$

$$27. \sqrt{\frac{1+\cos\theta}{1-\cos\theta}} = \sqrt{\frac{1+\cos\theta}{1-\cos\theta} \times \frac{1+\cos\theta}{1+\cos\theta}}$$

$$= \sqrt{\frac{(1+\cos\theta)^2}{1-\cos^2\theta}} = \sqrt{\left(\frac{1+\cos\theta}{\sin\theta}\right)^2}$$

$$= \frac{1+\cos\theta}{\sin\theta} = \frac{1}{\sin\theta} + \frac{\cos\theta}{\sin\theta}$$

$$= \text{cosec}\theta + \cot\theta = \text{RHS}$$

$$28. \Rightarrow \frac{1}{2} \begin{pmatrix} p^2 & 0 & 1 & p^2 \\ 0 & q^2 & 1 & 0 \end{pmatrix} = 0$$

$$\Rightarrow \frac{1}{2} [(p^2q^2 + 0 + 0) - (0 + q^2 + p^2)] = 0$$

$$\Rightarrow \frac{1}{p^2} + \frac{1}{q^2} = 1$$

**III ANSWER ANY 10 ONLY**

29.  $(B \cup C) = \{2, 3, 4\} \cup \{3, 5\} = \{2, 3, 4, 5\}$   
 $A \times (B \cup C) = \{0, 1\} \times \{2, 3, 4, 5\}$   
 $= \{(0,2), (0,3), (0,4), (0,5), (1,2), (1,3), (1,4), (1,5)\}$   
 $(A \times B) = \{(0,2), (0,3), (0,4), (1,2), (1,3), (1,4)\}$   
 $(A \times C) = \{(0,3), (0,5), (1,3), (1,5)\}$   
 $(A \times B) \cup (A \times C)$   
 $= \{(0,2), (0,3), (0,4), (0,5), (1,2), (1,3), (1,4), (1,5)\}$
30. (i)  $f(4) = 3x - 2 = 3(4) - 2 = 10$   
(ii)  $f(-2) = x^2 - 2 = (-2)^2 - 2 = 2$   
(iii)  $f(4) + 2f(1)$   
 $2f(1) = x^2 - 1 = 2[(1)^2 - 2] = -2$   
 $f(4) + 2f(1) = 10 - 2 = 8$   
(iv)  $\frac{f(1) - 3f(4)}{f(-3)} = \frac{-1 - 3(10)}{1} = \frac{-1 - 30}{1} = -31$
31.  $\text{fog} = (x - 1) \circ (3x + 1) \Rightarrow (3x + 1) - 1 = 3x$   
 $(\text{fog})\text{oh} = (3x) \circ (x^2) \Rightarrow 3x^2$   
 $\text{goh} = (3x + 1) \circ (x^2) = 3x^2 + 1$   
 $\text{fo(goh)} = (x - 1) \circ (3x^2 + 1) \Rightarrow 3x^2$
32.  $a = 7, d = \pm 2, \therefore$  Numbers are 1, 5, 9, 13
33.  $3 + 33 + 333 + \dots + n$   
 $S_n = \frac{3}{9} (9 + 99 + 999 + \dots + n \text{ terms})$   
 $S_n = \frac{3}{9} \left( \frac{10(10^n - 1)}{9} - n \right)$   
 $S_n = \frac{10(10^n - 1)}{27} - \frac{n}{3}$

34.  $\Sigma 24^2 - \Sigma 9^2 = 4900 - 285 = 4615$

35.  $x = 2, y = -1, z = 4$

36.  $m = 30$  and  $n = 9$

37.  $\Delta = b^2 - 4ac$

$$= [2(pr + qs)]^2 - 4(p^2 + q^2)(r^2 + s^2)$$

$$= -1[(ps - qr)^2] < 0 \therefore \text{the roots are not real}$$

If  $ps = qr$  then  $\Delta = -4(ps - qr)^2 =$

$$= -4(qr - qr)^2 \therefore \Delta = 0 \text{ and so the roots will be the real and equal.}$$

38. Angle Bisector Theorem.

39. Area of quadrilateral

$$= \frac{1}{2} \begin{vmatrix} 8 & 5 & -5 & -4 & 8 \\ 6 & 11 & 12 & 3 & 6 \end{vmatrix} = \frac{1}{2}(109 + 49)$$

$$= \frac{1}{2}(158) = 79 \text{ Sq. Units.}$$

40. Mid point of AB =  $\left(\frac{6-4}{2}, \frac{-4+2}{2}\right) = (1, -1)$

$$\text{Slope of AB } (m_1) = \frac{-4-2}{6+4} = \frac{-3}{5}$$

Therefore the slope of perpendicular to AB is

$$(m_2) = \frac{5}{3}$$

$\Rightarrow$  Equation of the line perpendicular to AB is

$$\Rightarrow (y + 1) = \frac{5}{3}(x - 1) \Rightarrow 5x - 3y - 8 = 0$$

41.  $\Rightarrow a = \frac{1 + \sin\theta}{\cos\theta}$

$$\Rightarrow a^2 = \frac{1 + \sin^2\theta + 2\sin\theta}{\cos^2\theta}$$

$$= \frac{a^2 - 1}{a^2 + 1} = \frac{\frac{1 + \sin^2\theta + 2\sin\theta}{\cos^2\theta} - 1}{\frac{1 + \sin^2\theta + 2\sin\theta}{\cos^2\theta} + 1}$$

$$= \frac{1 + \sin^2\theta + 2\sin\theta - \cos^2\theta}{1 + \sin^2\theta + 2\sin\theta + \cos^2\theta}$$

$$= \frac{2\sin\theta(1 + \sin\theta)}{2(1 + \sin\theta)} = \sin\theta$$

42.  $\frac{1}{x+2} + \frac{1}{x-2} = 6\left(\frac{1}{4x+7}\right)$

$$\frac{x-2+x+2}{(x+2)(x-2)} = \frac{6}{4x+7}$$

$$\Rightarrow x^2 + 7x + 12 = 0$$

$$\Rightarrow (x + 3)(x + 4) = 0$$

$$\therefore x = -3 \text{ \& } -4$$

## GEOMETRY & GRAPH

43. (a)

Time taken (hr) - x	1	2	3	4	5	6
Distance (km) - y	50	100	150	200	250	300

Equation:

$$\Rightarrow y = kx \Rightarrow k = \frac{y}{x}$$

(i) Constant of variation  $\Rightarrow k = \frac{5}{6}$

(ii) The distance travelled for  $1\frac{1}{2}$  hours (90 minutes) = **75 km**

(iii) The time taken to cover 300 km = **6 hours = 360 minutes.**

(b)

X	1	2	3	4	6	8	12	24
y	24	12	8	6	4	3	2	1

**Variation : Indirect Variation**

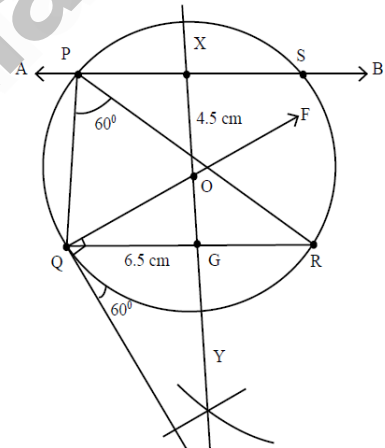
**Equation :**  $xy = k$

**Solution:** From the graph

(i) If  $x = 3$  then,  $y = 8$

(ii) If  $y = 6$  then,  $x = 4$

44. (a)



(b)

