

RAMA STUDY CENTRE WHATSAPP-8754834604

MINIMUM STUDY MATERIAL FOR QUARTERLY EXAM

## 12th STANDARD - MATHS

## CHAPTER - 1

- 1) Prove and state reverse law for inverse
- 2) If  $\text{adj } A = \begin{bmatrix} -1 & 2 & 2 \\ 1 & 1 & 2 \\ 2 & 2 & 1 \end{bmatrix}$  find  $A^{-1}$
- 3)  $A = \begin{bmatrix} 4 & 3 \\ 2 & 5 \end{bmatrix}$  find  $x$  and  $y$  such that  $A^2 + xA + yI_2 = O_2$ ,  $A^{-1} = ?$
- 4) Prove that  $\begin{bmatrix} \cos\theta & -\sin\theta \\ \sin\theta & \cos\theta \end{bmatrix}$  is orthogonal
- 5) Find the matrix  $A$  for which  $A \times \begin{bmatrix} 5 & 3 \\ -1 & -2 \end{bmatrix} = \begin{bmatrix} 14 & 7 \\ 7 & 7 \end{bmatrix}$
- 6) Find the rank of matrix  $\begin{bmatrix} 4 & 3 & 1 & -2 \\ -3 & -1 & -2 & 4 \\ 6 & -1 & -1 & 2 \end{bmatrix}$
- 7) Find the inverse of  $A = \begin{bmatrix} 2 & 1 & 1 \\ 3 & 2 & 1 \\ 2 & 1 & 2 \end{bmatrix}$  by Gauss Jordan method
- 8) Solve the following system of linear equation by matrix inversion method  $2x + 5y = -2$ ,  $x + 2y = 3$
- 9) A chemist has one solution which is 50% acid and another solution 25% acid. How much each should be mixed to make 10 litres of 40% acid solution?
- 10) If  $ax^2 + bx + c$  is divided by  $x+3$ ,  $x-5$  and  $x-1$ , the remainders are 21, 61 and 9 respectively find a, b, c
- 11) Test the consistency of system of linear equation  
 $4x - 2y + 6z = 8$ ,  $x + y - 3z = -1$  and  $15x - 3y + 9z = 21$
- 12) Find the value of  $k$ ,  $kx - 2y + z = 1$ ,  $x - 2y + k + z = -2$ ,  $x - 2y + kz = 1$   
 i) no solution ii) unique solution iii) infinitely many soln
- 13) By using Gaussian elimination method balance the chemical reaction equation  $C_5H_8 + O_2 \rightarrow CO_2 + H_2O$

G. Rajesh M.Sc., B.Ed., MBA, MSC  
 (Psych), MA(Eco), MA(Yoga), MA(Tam)  
 Dept of mathematics.

RAMA STUDY CENTRE WHATSAPP -87154834604  
MINIMUM STUDY MATERIAL FOR QUARTERLY EXAM

12th STANDARD - MATHS

- 1) Simplify the following  $\sum_{n=1}^{102} i^n$
- 2) Find the values of real numbers  $x$  and  $y$  if the complex number  $(3-i)x - (2-i)y + 2i + 5$  and  $2x + (-1+2i)y + 3+2i$  are equal
- 3) If  $z_1 = 2+5i$ ,  $z_2 = -3-4i$  and  $z_3 = 1+i$ , find the additive and multiplicative inverse of  $z_1$ ,  $z_2$  and  $z_3$
- 4) A complex number  $z$  is purely imaginary if and only if  $z = -\bar{z}$
- 5) Simplify  $\left(\frac{1+i}{1-i}\right)^3 - \left(\frac{1-i}{1+i}\right)^3$  into rectangular form
- 6) If  $\frac{z+3}{z-5i} = \frac{1+4i}{2}$  find  $z$  in rectangular form
- 7) Find  $z^{-1}$  if  $z = (2+3i)(1-i)$
- 8) Show i)  $(2+i\sqrt{3})^{10} + (2-i\sqrt{3})^{10}$  is real ii)  $\left(\frac{19+9i}{5-3i}\right)^{15} - \left(\frac{8+i}{1+2i}\right)^{15}$  is purely imaginary
- 9) Which one of following points  $i$ ,  $-2+i$  and  $3$  is farthest from the origin?
- 10) If  $|z| = 2$ , show that  $3 \leq |z + 3i + 4i| \leq 7$
- 11) Let  $z_1, z_2, z_3$  be complex numbers such that  $|z_1| = |z_2| = |z_3| = r > 0$  and  $z_1 + z_2 + z_3 \neq 0$ . show that  $\left| \frac{z_1 z_2 + z_2 z_3 + z_3 z_1}{z_1 + z_2 + z_3} \right| = r$
- 12) Show that the equation  $z^3 + 2\bar{z} = 0$  has five solutions
- 13) Find the square root of  $-5-12i$
- 14) Show that  $|3z - 5 + i| = 4$  represents circle. Find centre, radius
- 15) If  $z = x+iy$  is a complex number such that  $\operatorname{Im}\left(\frac{2z+1}{iz+1}\right) = 0$  show that locus of  $z$  is  $2x^2 + 2y^2 + x - 2y = 0$
- 16) If  $z = x+iy$  and any  $\left(\frac{z-1}{z+1}\right) = \frac{\pi}{2}$ , show that  $x^2 + y^2 = 1$
- 17) If  $(x_1+iy_1), (x_2+iy_2), \dots, (x_n+iy_n) = a+ib$ , show that  $(x_1^2+y_1^2)(x_2^2+y_2^2)\dots(x_n^2+y_n^2) = a^2+b^2$
- 18) Find the fourth roots of unity
- 19) Solve the equation  $z^3 + 8i = 0$ , where  $z \in \mathbb{C}$
- 20) Suppose  $z_1, z_2$  and  $z_3$  are vertices of equilateral triangle inscribed in circle  $|z| = 2$ , If  $z_1 = 1+i\sqrt{3}$  find  $z_2$  and  $z_3$

G. Rajesh M.Sc., B.Ed., MBA, M.Sc.(Psych)  
MA(Eco). MA(Yoga). MA(Tam)  
Dept of Mathematics.