HSL

HALF YEARLY EXAMINATION - 2023

Time: 3.00 Hrs

10 - STD

MATHS

Marks: 100

Part - I Answer all the questions.

 $14 \times 1 = 14$

The range of the relation $R = \{(x, x^2) / x \text{ is a prime number less than } 13\}$ is 1.

a) {2, 3, 5, 7}

- b) {2,3,5,7,11}
- c) {4,9,25,49,121}
- d) {1,4,9,25,49,121}

Let $f(x) = \sqrt{1+x^2}$ then 2.

a) $f(xy) = f(x) \cdot f(y)$ b) $f(xy) \ge f(x) \cdot f(y)$ c) $f(xy) \le f(x) \cdot f(y)$ d) none of these

- If 6 times of 6th term of an A.P. is equal to 7 times the 7th term, then the 13th term of the 3. A.P is b) 6 . c) 7 c) 13
- 4. The sum of first n terms of a G.P, when r = 1 is a) an b) n
- Which of the following should be added to make x⁴ + 64 a perfect square 5.

- b) 16x2
- c) 8x2
- The square root of $4m^2 24m + 36 = 0$ is a) 4(m-3) b) 2(m-3) c) $(2m-3)^2$ d) 4(m+3)6.
- In a \triangle ABC, AD is the bisector of \angle BAC, If AB = 8cm, BD = 6cm and DC = 3cm. The length 7. of the side AC is a) 6cm b) 4 cm c) 3 cm d) 8 cm
- The point of intersection of 3x y = 4 and x + y = 8 is 8.

- b) (2,4)
- c) (3,5)
- d)(4,4)
- A straight line PQ cuts the X axis at A and Y axis at B. If the mid point of AB is (2a, 2b) 9. then the cor-ordinates of A and B are
 - a) (a, 0), (0, b)
- b) (2a, 0), (0, 2b) c) (0, b), (a, 0)
- d) (0, 2b), (2a, 0)
- If $\sin \theta + \cos \theta = a$ and $\sec \theta + \csc \theta = b$, then the value of $b(a^2-1)$ is equal to 10.

b) 3a

- c) 0
- If two solid hemispheres of same base radius r units are joined together along their bases, 11. then curved surface area of this new solid is
 - a) $4\pi r^2$ sq. units b) $6\pi r^2$ sq. units c) $3\pi r^2$ sq. units d) $8\pi r^2$ sq. units
- The curved surface area of a right circular cone of height 15cm and base diameter 16cm 12. a) $60 \pi \text{ cm}^2$ b) $66 \pi \text{ cm}^2$ c) $120 \pi \text{ cm}^2$ d) $136 \pi \text{ cm}^2$
- The range of the data 8, 8, 8, 8, 8, 8 is a) 0 13. b) 1 c) 8
- A page is selected at random from a book. The probability that the digit at units place of 14. the page number chosen is less than 7 is

- Part II Answer any 10 questions. Question No. 28 is compulsory.
- If B X A = $\{(-2, 3), (-2, 4), (0, 3), (0, 4), (3,3), (3,4)\}$ find A and B. 15.
- Find k if fof(k) = 5 where f(k) = 2k-1. 16.
- Find the number of terms in the A.P. 3,6,9,12,...... 111. 17.
- 18. If $1^3+2^3+3^3+\ldots+k^3=44100$ then find $1+2+3+\ldots+k$.
- Find the excluded values of the following expression 19.
- 20. What length of ladder is needed to reach a height of 7ft along the wall when the base of the ladder is 4ft from the wall? Round off your answer to the next tenth place.
- 21. If the three points (3, -1), (a, 3) and (1, -3) are collinear, find the value of a.
- Find the equation of a line through the given pair of points (2,3) and (-7,-1). 22.

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- $sec \theta$ Prove that 23.
- The volume of a solid right circular cone is 11088cm3. If its height is 24cm then find the 24. radius of the cone.
- A right circular cylinder just enclose a sphere of radius r units. Calculate i) the surface 25. area of the sphere. ii) the curved surface area of the cylinder.
- Find the standard deviation of first 21 natural numbers. 26.
- A coin is tossed thrice. What is the probability of getting two consecutive tails? 27.
- If $(5 \times 1) \begin{vmatrix} -1 \\ 3 \end{vmatrix} = (20)$ find the value of x? 28.
- Part III Answer any 10 questions. Question No. 42 is compulsory. $10 \times 5 = 50$ Ш
- Let $A = \{x \in W \mid x < 2\}, B = \{x \in N \mid 1 < x \le 4\}$ and $C = \{3,5\}$ Verify that 29. $AX(B \cap C) = (AXB) \cap (AXC)$.
- If f(x) = x-1, g(x) = 3x + 1 and $h(x) = x^2$ show that (fog) oh = fo(goh). 30.
- The product of three consecutive terms of a Geometric progression is 343 and their sum 31. is $\frac{91}{3}$. Find the three terms.
- Rekha has 15 square colour papers of sizes 10cm, 11cm, 12cm, 24cm. How much 32. area can be decorated with these colour papers?
- If $ax^4 + bx^3 + 361x^2 + 220x + 100$ is a perfect square, find the values of a and b. 33.
- If α , β are the roots of the equation $2x^2 x 1 = 0$ then form the equation whose roots 34. are i) $\frac{1}{\alpha}$, $\frac{1}{\beta}$ ii) $2\alpha + \beta$, $2\beta + \alpha$.
- are 1) $_{\alpha}$, $_{\beta}$..., $_{\beta}$..., $_{B}$...

 If $A = \begin{pmatrix} 1 & 2 & 1 \\ 2 & -1 & 1 \end{pmatrix}$, $B = \begin{pmatrix} 2 & -1 \\ -1 & 4 \\ 0 & 2 \end{pmatrix}$ show that $(AB)^{T} = B^{T}A^{T}$.
- State and prove angle bisector theorem. 36.
- Find the area of the quadrilateral whose vertices are at (-9, 0), (-8, 6), (-1, -2) and (-6, -3). 37.
- Find the equation of a straight line parallel to y axis and passing through the point of 38. intersection of the line 4x + 5y = 13, x - 8y + 9 = 0.
- A man is watching a boat speeding away from the top of a tower. The boat makes an 39. angle of depression of 60° with the man's eye when at a distance of 200m from the tower. After 10 seconds, the angle of depression becomes 45°. What is the approximate speed of the boat (in Km/hr), assuming that it is sailing in still water? ($\sqrt{3} = 1.732$)
- A conical container is fully filled with petrol. The radius is 10m and the height is 15m. If the 40. container can release the petrol through its bottom at the rate of 25cu. meter per minute, in how many minutes the container will be emptied. Round off your answer to the nearest minutes.
- Two dice are rolled together. Find the probability of getting a doublet or sum of face as 4. 41.
- A chess board contains 64 equal squares and the area of each square is 6.25cm². A border 42. around the board is 2cm wide. Find the length of the side of the chess board?
- IV Part - IV Answer all questions.

- $2 \times 8 = 16$
- Draw a triangle ABC of base BC = 5.6cm, $\angle A = 40^{\circ}$ and the bisector of $\angle A$ meets BC at D such that CD = 4cm. (OR) b) Draw tangent to the circle from the point P having radius 3.6cm and the centre at O. Point P is at a distance 7.2cm from the centre.
- a) Graph the following linear function $y = \frac{1}{2}x$. Identify the constant of variation and verify it with the graph. Also i) find y when x = 9. ii) find x when y = 7.5. (OR) b) Draw the graph of $y = x^2 + 3x + 2$ and use it to solve $x^2 + 2x + 1 = 0$.