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03-01-2024
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Time: 3.00 Hours

## Standard 12

MATHEMATICS
PART-I
$20 \times 1=20$

## Choose the correct Answer

1) The principal argument of $\frac{-2}{1+i \sqrt{3}}$ is
a) $\pi / 3$
b) $2 \pi / 3$
c) $-2 \pi / 3$
d) $-\pi / 2$
2) If $A^{\top} A^{-1}$ is symmetric then $A^{2}=$
a) $A^{-1}$
b) $\left(A^{T}\right)^{2}$
c) $A^{\top}$
d) $\left(A^{-1}\right)^{2}$
3) If $x+y=K$ is a normal to the parabola $y^{2}=12 x$ then the value of $K$ is
a) 3
b) -1
c) 1
d) 9
4) According to the rational root theorem which number is not possible rational zero of $4 x^{7}+2 x^{4}-10 x^{3}-5$ ?
a) -1
b) $5 / 4$
c) $4 / 5$
d) 5
5) The angle between the line $\vec{r}=(\hat{i}+2 \hat{j}-3 \hat{k})+t(2 \hat{i}+\hat{j}-2 \hat{k})$ and the plane $\vec{r} .(\hat{i}+\hat{j})+4=0$ is
a) $0^{\circ}$
b) $30^{\circ}$
c) $45^{\circ}$
d) $90^{\circ}$
6) If $\sin ^{-1} x / 5+\operatorname{cosec}^{-1} 5 / 4=\pi / 2$ then the value of $x$ is
a) 4
b) 5
c) 2
d) 3
7) The eccentricity of the ellipse $(x-3)^{2}+(y-4)^{2}=y^{2} / 9$ is
a) $\sqrt{3} / 2$
b) $1 / 3$
c) $1 / 3 \sqrt{2}$
d) $1 / \sqrt{3}$
8) The product of all four values of $(\cos \pi / 3+i \sin \pi / 3)^{3 / 4}$ is
a) -2
b) -1
c) 1
d) 2
9) If $\rho(A)=\rho(A / B)$ then the system $A x=B$ of linear equations is
a) consistent and has unique solution
b) consistent
c) consistent and has infinitely many solutions
d) inconsistent
10) $2 \hat{i}-\hat{j}+3 \hat{k}, 3 \hat{i}+2 \hat{j}+\hat{k}, \hat{i}+m \hat{j}+4 \hat{k}$ are coplanar then $m$ is
a) 3
b) 0
c) -3
d) 1
11) Substraction is not a binary operation in
a) $R$
b) $Z$
c) N
d) Q
12) If the function $f(x)=1 / 12$ for $a<x<b$ represents a probability density function of a continuous random variable $x$ then which of the following cannot be the value of $a \& b$
a) $0 \& b$
b) $5 \& 17$
c) $7 \& 19$
d) $16 \& 24$

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13) The volume when the curve $y=\sqrt{3+x^{2}}$ from $x=0$ to $x=4$ is rotated about $x$ axis is
a) $100 \pi$
b) $\frac{100 \pi}{9}$
c) $\frac{100 \pi}{3}$
d) $\frac{100}{3}$
14) $P$ is the amount of certain substance left in after time $t$. If the rate of evaporation of the substance is proportional to the amount remaining then
a) $\mathrm{P}=\mathrm{Ce}^{\mathrm{Kt}}$
b) $\mathrm{P}=\mathrm{Ce}^{\mathrm{Kt}}$
c) $\mathrm{P}=\mathrm{cKt}$
d) $\mathrm{Pt}=\mathrm{C}$
15) If $f(x, y)=e^{-x y}$ then $\frac{\partial^{2} f}{\partial x \partial y}$ is
a) $x y e^{x y}$
b) $(1+x y) e^{x y}$
c) $(1+y) e^{x y}$
d) $(1+x) e^{x y}$
16) Point of inflection of the curve $y=x^{4}$ is at
a) $x=0$
b) $x=1$
c) $x=12$
d) nowhere
17) The value of $\int_{-1}^{2}|x| d x$
a) $1 / 2$
b) $3 / 2$
c) $5 / 2$
d) $7 / 2$
18) The integrating factor of the differential equation $\frac{d y}{d x}+y=\frac{1+y}{\lambda}$ is
a) $x / e^{\lambda}$
b) $e^{\lambda} / x$
c) $\lambda e^{x}$
d) $e^{x}$
19) The mean of a binomial distribution is 5 and its standard deviation is 2 then the value of $n$ and $p$ are
a) $(4 / 5,25)$
b) $(25,4 / 5)$
c) $(1 / 5,25)$
d) $(25,1 / 5)$
20) The maximum value of the function $x^{2} e^{-2 x}, x>0$ is
a) $1 / e$
b) $1 / 2 \mathrm{e}$
c) $1 / e^{2}$
d) $4 / e^{4}$

## PART - II

## Answer any $\mathbf{7}$ questions. Qn.no. 30 is compulsory.

21) Find the inverse of $A=\left(\begin{array}{ll}2 & -1 \\ 5 & -2\end{array}\right)$ by Gauss-Jordan method.
22) Show that $|3 z-5+i|=4$ represents a circle and find its centre and radius.
23) Find the domain of $\tan ^{-1} \sqrt{9-x^{2}}$
24) Examine the position of the point $(2,3)$ with respect to the circle
25) Find the length of the perpendicular from the point $(1,-2,3)$ to the
plane $x-y+z=5$
26) Solve: $x^{3}-3 x^{2}-33 x+35=0$.
27) Evaluate: $\int_{0}^{1} x^{2}(1-x)^{3} d x$
28) The mean and variance of a binomial variate $x$ are respectively 2 and 1.5 find $P(X=0)$

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29) $A=\left(\begin{array}{ll}0 & 1 \\ 1 & 1\end{array}\right) \quad B=\left(\begin{array}{ll}1 & 1 \\ 0 & 1\end{array}\right)$ be any two boolean matrices of the same type find $A \vee B$ and $A \wedge B$
30) Find the asymptotes of the curve $f(x)=\frac{x^{2}}{x+1}$

## PART - III

$7 \times 3=21$

## Answer any 7 questions. Qn. no. 40 is compulsory.

31) Solve $2 x+2 y+z=5, x-y+z=1,3 x+y+2 z=4$ by rank method.
32) If $\omega \neq 1$ is a cube root of unity. Show that $\left(1-\omega+\omega^{2}\right)^{6}+\left(1+\omega-()^{2}\right)^{6}=128$.
33) Prove that an angle in a semi circle is a right angle.
34) The orbit of Halley's comet is an ellipse 36.18 astronomical units long and by 9.12 astronomical units wide. Find its eccentricity.
35) Evaluate: $\underset{x \rightarrow \pi / 2}{\operatorname{Lt}} \frac{\sec x}{\tan x}$
36) If $v(x, y, z)=\log \left(x^{3}+y^{3}+z^{3}\right)$ find $\frac{\partial u}{\partial x}+\frac{\partial u}{\partial y}+\frac{\partial u}{\partial z}$
37) Evaluate: $\int_{-\pi / 2}^{\pi / 2} x \cos x d x$
38) A six sided die is marked 2 on one face, 3 on two of its faces and 4 on remaining three faces. The die is thrown twice. If $x$ denotes the total score in two throws, find the values of the random variable and number of points in its inverse images.
39) Construct the truth table $(p \vee q) \wedge \neg q$
40) Form the differential equation by eliminating the arbitrary constants $A$ and $B$ from $y=A \cos x+B \sin x$

## Answer all the questions:

41) Investigate for what values of $\lambda$ and $\mu$ the system of linear equations $x+2 y+z=7, x+y+\lambda z=\mu, x+3 y-5 z=5$ has (i) no solution (ii) a unique solution (iii) an infinite number of solutions.
(OR)
A garden is to be laidout in a rectangular area and protected by wire fence. What is the largest possible area of the fenced garden with 40 meters of wire.
42) If $z=x+i y$ and $\arg \left(\frac{z-i}{z+2}\right)=\frac{\pi}{4}$. Show that $x^{2}+y^{2}+3 x-3 y+2=0$
(OR)
Find the number of solution of the equation
$\tan ^{-1}\left(x^{-1}\right)+\tan ^{-1}(x)+\tan ^{-1}(x+1)=\tan ^{-1}(3 x)$

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43) Find the sum of squares of roots of the equation $2 x^{4}-8 x^{3}+6 x^{2}-3=0$
(OR)

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z(x, y)=x \tan ^{-1}(x y), x=t^{2}, y=s e^{t}, s, t, \in R \text { find } \frac{\partial z}{\partial s} \text { at } s=t=1
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44) Find the area of the region bounded by $y=\cos x, y=\sin x$, the lines $x=\pi / 4$ and $x=5 \pi / 4$
(OR)
Find the equations of tangents to the hyperbola $\frac{x^{2}}{16}-\frac{y^{2}}{64}=1$ which are parallel to $10 x-3 y+9=0$.
45) Find the parametric form of vector equation and Cartesian equations of the. plane passing through the points $(2,2,1)(9,3,6)$ and perpendicular to the plane $2 x+6 y+6 z=9$

## (OR)

The probability density function of the random variable $x$ is given by
$f(x)=\left\{\begin{array}{cc}16 x e^{-4 x} & \text { for } x>0 \\ 0 & \text { for } x \leq 0\end{array}\right.$ find the mean and variance of $x$.
46) Solve $\frac{d y}{d x}+2 y \cot x=3 x^{2} \operatorname{cosec}^{2} x$
(OR)
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Tenkasi wist.
A bridge has a parabolic arch that is 10 m high in the centre and 30 m wide at the bottom. Find the height of the arch 6 m from the centre on either sides.
47) Suppose a person deposits Rs. 10,000 in a bank account at the rate of $5 \%$ per annum compounded continuously. How much money will be in his bank account 18 months later?

## (OR)

$M=\left\{\left(\begin{array}{ll}x & x \\ x & x\end{array}\right): x \in R-\{0\}\right\}$ and let * be the matrix multiplication. Determine whether $m$ is closed under *. If so examine the commutative and associative properties, existence of identity, existence of inverse properties for the operation * on M

