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Tsi12M		Tenkasi Dist	rict	mm
	Com	mon Half Yearly Exa	mination - 2023	aun
03-	01-2024			
		Standard	12	Martine 00
lime: 3	3.00 Hours	MATHEMAT	TICS	Marks: 90
Choose	the correct Anov	PART - I		2081-20
CHOOSE	e the correct Answ	er `		
1)	The principal argu	ment of $\frac{-2}{1+i\sqrt{3}}$ is	Charles and Charles	
	a) $\frac{\pi}{3}$	b) $\frac{2\pi}{3}$	c) $\frac{-2\pi}{3}$	d) $-\frac{\pi}{2}$
2)	If A ^T A ⁻¹ is symme	tric then $A^2 =$		
	⊿a) A ⁻¹	b) (A ^T) ²	ε) Α ^τ	d) (A ⁻¹) ²
3)	If $x+y = K$ is a nor	rmal to the parabola	$y^2 = 12x$ then the v	alue of K is
	a) 3	b) –1	c) 1	d) 9
4)	According to the razero of $4x^7+2x^4-10^{-10}$	ational root theorem 0x ³ –5?	which number is not	possible rational
	a) –1	b) $\frac{5}{4}$	c) $\frac{4}{5}$	d) 5
5)	The angle betwee	en the line $\vec{r} = (\hat{i} + \hat{j})$	$2\hat{\mathbf{j}} - 3\hat{\mathbf{k}} + t(2\hat{\mathbf{i}} + \hat{\mathbf{j}} - 2\hat{\mathbf{k}})$	and the plane
	$\vec{r} \cdot (\hat{i} + \hat{j}) + 4 = 0$ is		5	
	a) 0°	b) 30°	c) 45°	d) 90°
6)	If $\sin^{-1} \frac{x}{5} + \cos \frac{1}{5}$	$\frac{-1}{4} = \frac{\pi}{2}$ then the	value of x is	
	a) 4	b) 5	c) 2	d) 3
7)	The eccentricity of	the ellipse $(x-3)^2$ -	$+ (y-4)^2 = \frac{y^2}{9}$ is	
	a) $\sqrt{3}/2$	b) $\frac{1}{3}$	c) $\frac{1}{3\sqrt{2}}$	d) $\frac{1}{\sqrt{3}}$
8)	The product of all	four values of (cos	$\frac{\pi}{3} + i \sin \frac{\pi}{3} \Big)^{\frac{3}{4}}$ is	
	a) –2	b) -1	c) 1	d) 2
ʻ 9)	If $\rho(A) = \rho(A'_B)$ the	en the system $Ax =$	B of linear equation	s is
	a) consistent and hc) consistent and h	has unique solution has infinitely many s	olutions	b) consistentd) inconsistent
10)	$2\hat{i} - \hat{j} + 3\hat{k}, 3\hat{i} + 2\hat{j} +$	$\hat{\mathbf{k}}, \hat{\mathbf{i}} + \hat{\mathbf{m}}\hat{\mathbf{j}} + 4\hat{\mathbf{k}}$ are co	planar then m is	
	a) 3	b) 0	c) -3	d) 1
11)	Substraction is not a) R	a binary operation b) Z	in c) N	d) Q
10)	If the function f(x)	- 1/ 50	< h	
12)	function of a continuation r(x)	$r = 7_{12}$ for a < x inuous random var e of a & b	iable x then which	of the following
	a) 0 & b	b) 5 & 17	c) 7 & 19	d) 16 & 24

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13) The volume when the curve $y = \sqrt{3 + x^2}$ from x = 0 to x = 4 is rotated about x axis is d) $\frac{100}{2}$ b) $\frac{100\pi}{9}$ c) $\frac{100\pi}{3}$ a) 100 π 14) P is the amount of certain substance left in after time t. If the rate of evaporation of the substance is proportional to the amount remaining then d) Pt = ca) $P = Ce^{Kt}$ b) $P = Ce^{Kt}$ c) P = cKt15) If $f(x, y) = e^{xy}$ then $\frac{\partial^2 f}{\partial x \partial y}$ is d) (1+x)e^{xy} a) xye^{xy} b) (1+xy)e^{xy} c) (1+y)e^{xy} 16) Point of inflection of the curve $y = x^4$ is at d) nowhere a) x = 0b) x = 1 c) x = 1217) The value of $\int |x| dx$ c) $\frac{5}{2}$ d) $\frac{7}{2}$ a) $\frac{1}{2}$ b) 3/2 18) The integrating factor of the differential equation $\frac{dy}{dx} + y = \frac{1+y}{\lambda}$ is b) e^{λ} a) χ_{λ} c) λe^x d) e^x 19) The mean of a binomial distribution is 5 and its standard deviation is 2 then the value of n and p are b) (25, 4/5) a) $(\frac{4}{5}, 25)$ c) $\left(\frac{1}{5}, 25\right)$ d) $(25, \frac{1}{5})$ 20) The maximum value of the function x^2e^{-2x} , x > 0 is a) 1/2 d) $\frac{4}{e^4}$ b) $\frac{1}{2e}$ c) $\frac{1}{c^2}$ PART-II 7x2=14 Answer any 7 questions. Qn.no. 30 is compulsory. 21) Find the inverse of A = $\begin{pmatrix} 2 & -1 \\ 5 & -2 \end{pmatrix}$ by Gauss-Jordan method. 22) Show that |3z-5+i| = 4 represents a circle and find its centre and radius. 23) Find the domain of $\tan^{-1}\sqrt{9-x^2}$ 24) Examine the position of the point (2, 3) with respect to the circle $x^2+y^2-6x-8y+12=0$ **25) Find the length** of the perpendicular from the point (1, -2, 3) to the plane x-y+z = 526) Solve: $x^3 - 3x^2 - 33x + 35 = 0$. 27) Evaluate: $\int x^{2} (1-x)^{3} dx$

28) The mean and variance of a binomial variate x are respectively 2 and 1.5

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- 29) $A = \begin{pmatrix} 0 & 1 \\ 1 & 1 \end{pmatrix}$ $B = \begin{pmatrix} 1 & 1 \\ 0 & 1 \end{pmatrix}$ be any two boolean matrices of the same type find $A \lor B$ and $A \land B$
- 30) Find the asymptotes of the curve $f(x) = \frac{x^2}{x+1}$

PART - III

Answer any 7 questions. Qn. no. 40 is compulsory.

- 31) Solve 2x+2y+z = 5, x-y+z = 1, 3x+y+2z = 4 by rank method.
- 32) If $\omega \neq 1$ is a cube root of unity. Show that $(1-\omega+\omega^2)^6+(1+\omega-\omega^2)^6 = 128$.
- 33) Prove that an angle in a semi circle is a right angle.
- 34) The orbit of Halley's comet is an ellipse 36.18 astronomical units long and by 9.12 astronomical units wide. Find its eccentricity.

35) Evaluate:
$$\frac{\text{Lt}}{x \to \pi/2} - \frac{\sec x}{\tan x}$$

36) If v(x, y, z) = log (x³+y³+z³) find
$$\frac{\partial u}{\partial x} + \frac{\partial u}{\partial y} + \frac{\partial u}{\partial z}$$

37) Evaluate:
$$\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} x \cos x \, dx$$

- 38) A six sided die is marked 2 on one face, 3 on two of its faces and 4 on remaining three faces. The die is thrown twice. If x denotes the total score in two throws, find the values of the random variable and number of points in its inverse images.
- 39) Construct the truth table $(p \lor q) \land \neg q$
- 40) Form the differential equation by eliminating the arbitrary constants A and B from $y = A \cos x + B \sin x$

PART - IV

7x5=35

7x3=21

Answer all the questions:

41) Investigate for what values of λ and μ the system of linear equations x+2y+z = 7, $x+y+\lambda z = \mu$, x+3y-5z = 5 has (i) no solution (ii) a unique solution (iii) an infinite number of solutions.

(OR)

A garden is to be laidout in a rectangular area and protected by wire fence. What is the largest possible area of the fenced garden with 40 meters of wire.

42) If
$$z = x + iy$$
 and $\arg\left(\frac{z - i}{z + 2}\right) = \frac{\pi}{4}$. Show that $x^2 + y^2 + 3x - 3y + 2 = 0$

(OR)

Find the number of solution of the equation $\tan^{-1}(x^{-1}) + \tan^{-1}(x) + \tan^{-1}(x+1) = \tan^{-1}(3x)$

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43) Find the sum of squares of roots of the equation $2x^4-8x^3+6x^2-3=0$

$$z(x, y) = x \tan^{-1}(x y), x = t^2, y = se^t, s, t, \in \mathbb{R}$$
 find $\frac{\partial z}{\partial s}$ at $s = t = 1$

44) Find the area of the region bounded by $y = \cos x$, $y = \sin x$, the lines $x = \frac{\pi}{4}$ and $x = \frac{5\pi}{4}$

(OR)

Find the equations of tangents to the hyperbola $\frac{x^2}{16} - \frac{y^2}{64} = 1$ which are parallel to 10x-3y+9 = 0.

45) Find the parametric form of vector equation and Cartesian equations of the plane passing through the points (2, 2, 1) (9, 3, 6) and perpendicular to the plane 2x+6y+6z = 9

(OR)

The probability density function of the random variable x is given by

$$f(x) = \begin{cases} 16xe^{-4x} \text{ for } x > 0\\ 0 \text{ for } x \le 0 \end{cases} \text{ find the mean and variance of } x < 0 \end{cases}$$

46) Solve $\frac{dy}{dx} + 2y \cot x = 3x^2 \csc^2 x$

SIVATZUMAR.M, Soi Rouss Matoric Has Vallam-62 2809 Ten Kasi Dist, A bridge has a parabolic arch that is 10 m high in the centre and 30 m wide at the bottom. Find the height of the arch 6 m from the centre on either sides.

47) Suppose a person deposits Rs.10,000 in a bank account at the rate of 5% per annum compounded continuously. How much money will be in his bank account 18 months later?

(OR)

(OR)

 $M = \left\{ \begin{pmatrix} x & x \\ x & x \end{pmatrix} : x \in R - \{0\} \right\}$ and let * be the matrix multiplication. Determine

whether m is closed under *. If so examine the commutative and associative properties, existence of identity, existence of inverse properties for the operation * on M