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www.Padasalai.Net www.TrbTnpsc.com M 10) The eccentricity of the ellipse $(x-3)^2 + (y-4)^2 = \frac{y^2}{9}$ is V12M b) 1/3 c) $\frac{1}{3\sqrt{2}}$ a) $\sqrt{3}/2$ d) 1/53 11) If $\sin^{-1}x + \sin^{-1}y = \frac{2\pi}{3}$ then $\cos^{-1}x + \cos^{-1}y$ is equal to b) $\frac{\pi}{3}$ c) π/6 a) $2\pi/_{2}$ d) π 12) If $\sin^{-1}x + \sin^{-1}y + \sin^{-1}z = \frac{3\pi}{2}$, the value of $x^{2017}+y^{2018}+z^{2019}-\overline{x^{101}+y^{101}+z^{101}}$ is c) 2 b) 1 d) 3 a) 0 13) If sin x is the integrating factor of the linear differential equation $\frac{dy}{dx} + Py = Q$, then P is b) cos x c) tan x d) cot x a) log sin x 14) Find order and degree of differential equation $x = e^{xy\left(\frac{dy}{dx}\right)}$ c) 1, 1 b) 2, 1 d) 2, 2 a) 1, 2 15) The value of $\int_{0}^{1} x (1-x)^{99} dx$ is b) $\frac{1}{10100}$ c) $\frac{1}{10010}$ a) $\frac{1}{11000}$ d) $\frac{1}{10001}$ 16) Find the area of the region bounded by ellipse $\frac{x^2 + y^2}{a^2 + b^2} = 1$ is a) πa^2 b) πb² c) πab d) πa ' 17) If f(x, y, z) = xy+yz+zx, then f_x-f_z is equal to d) y-xa) z-x b) y-z c) x-z 18) If $u(x, y) = \frac{x + y}{\sqrt{x} + \sqrt{y}}$ then the degree of 'u' is d) $\frac{1}{4}$ c) 1/2 a) 1 b) 2 19) The slope of the line normal to the curve $f(x) = 2 \cos 4x$ at $x = \frac{\pi}{12}$ is a) −4 √3 b) −4 c) $\sqrt{3}/_{12}$ d) $4\sqrt{3}$ 20) The maximum value of the function x^2e^{-2x} , x > 0 is d) $\frac{4}{e^4}$ a) $\frac{1}{2}$ b) 1/2e c) $\frac{1}{2}$

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v12M

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PART - II Answer any seven questions. Question No. 30 is compulsory. 7×2=14

- 21) Find the angle between the planes $\vec{r} \cdot (\hat{i} + \hat{j} + \hat{k}) = 5$ and x y + z = 4
- 22) Show that the percentage error in the nth root of a number is approximately
 - $\frac{1}{n}$ times the percentage error in the number.
- 23) Evaluate: $\int_{0}^{\frac{\pi}{2}} \left| \cos^4 x + 7 \right| dx$
- 24) Show that $y = ax + \frac{b}{x}$, $x \neq 0$ is a solution of the differential equation $x^2y'' + xy' y = 0$

25) If adj A =
$$\begin{vmatrix} -1 & 2 & 2 \\ 1 & 1 & 2 \\ 2 & 2 & 1 \end{vmatrix}$$
 find A⁻¹.

- 26) Show that $(2 + i\sqrt{3})^{10} (2 i\sqrt{3})^{10}$ is purely imaginary.
- 27) Find a polynomial equation of minimum degree with rational coefficients, having $\sqrt{5} - \sqrt{3}$ as a root.
- 28) Find the value of $\sin^{-1}(10)$.
- 29) Find the equation of the parabola whose vertex is (1, -2) and focus is (4, -2)
- 30) Find the critical point of the function f(x) = |x-17|

PART - III

7×3=21

- Answer any seven questions. Question No. 40 is compulsory. 31) Obtain the Cartesian form of the locus of z if |2z-3-i| = 3.
 - 32) Find the value of $\sec^{-1}\left(-\frac{2\sqrt{3}}{3}\right)$
 - 33) Find the torque of the resultant of three forces represented by $-3\hat{i} + 6\hat{j} 3\hat{k}$,
 - $4\hat{i} 10\hat{j} + 12\hat{k}$ and $4\hat{i} + 7\hat{j}$ acting the point with position vector $8\hat{i} 6\hat{j} 4\hat{k}$

about the point with position vector $18\hat{i} + 3\hat{j} - 9\hat{k}$

34) Prove that the point of intersection of the tangents at t_1 and t_2 on the parabola $y^2 = 4ax$ is $[at_1t_2, a(t_1+t_2)]$

35) Evaluate:
$$\int_{-\log 2}^{\log 2} e^{-|x|} dx$$

36) Suppose f(x) is a differentiable function for all x with $f'(x) \le 29$ and f(2) = 17. What is the maximum value of f(7)?

37) Solve
$$\frac{dy}{dx} = e^{x+y} + x^3 e^y$$

38) Solve
$$\sin^2 x - 5 \sin x + 4 = 0$$

- 39) Solve by Cramer's rule: $\frac{3}{x} + 2y = 12$, $\frac{2}{y} + 3y = 13$
- 40) Find the area of the circle of radius r.

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PART - IV

41) a] Solve (x-5)(x-7)(x+6)(x+4) = 504Answer all the questions:

- - b] Find the number of solutions of the equations. Find the number of $x^{-1}(x+1) = \tan^{-1}(3x)$ $\tan^{-1}(x-1) + \tan^{-1}x + \tan^{-1}(x+1) = \tan^{-1}(3x)$

42) a] Prove by vector method that the perpendiculars from the vertices to the opposit sides of a triangle are concurrent. (OR)

- b] A semi elliptical archway over a one-way road has a height of 3 m and a width of 12 m. The truck has a width of 3 m and a height of 2.7 m. Will the truck clear the opening of the archway?
- 43) a] A pot of boiling water at 100° C is removed from a store at time t = 0 and left to cool in the kitchen. After 5 minutes, the water temperature has decreased to 80°C and another 5 minutes later it has dropped to 65°C. Determine the temperature of the kitchen.

(OR)

- b] A watermelon has an ellipsoid shape which can be obtained by revolving an ellipse with major axis 20 cm and minor axis 10 cm about its majoraxis. Find its volume using integration.
- 44) a] Derive the intercept form of the equation of a plane using vector method. (OR)
 - b] Salt is poured from a conveyer belt at a rate of 30 cubic metre per minute forming a conical pile with a circular base whose height and diameter of base are always equal. How fast is the height of the pile increasing when the pile is 10 meter high?

45) a] If
$$u = \tan^{-1}\left(\frac{x^3 + y^3}{x + y}\right)$$
, show that $x\frac{\partial u}{\partial x} + y\frac{\partial u}{\partial y} = \sin 2u$

(OR)

- b] Solve $z^4 = 1 \sqrt{3} i$.
- 46) a] If ax^2+bx+c is divided by x+3, x-5 and x-1 the remainders are 21, 61 and 9 respectively. Find a, b and c. (Use Gaussian Elimination method)

(OR)

- b] Find the equation of the circular passing through the points. (1, 1) (2, -1) and (3, 2)
- 47) a] Prove that $\int_{0}^{\frac{\pi}{4}} \log(1 + \tan x) dx = \frac{\pi}{8} \log 2$

(OR)

b] A rectangular page is to contain 24 cm² of print. the margins at the top and bottom of the page are 1.5 cm and the margins at other sides of the page is 1 cm. What should be the dimensions of the page so that the area of the paper used is minimum.

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7×5=35