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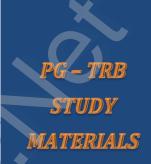
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STATISTICAL MECHANICS

- ➤ In physics, statistical mechanics is a mathematical framework that applies statistical methods and probability theory to large assemblies of microscopic entities.
- ➤ It does not assume or postulate any natural laws, but explains the macroscopic behavior of nature from the behavior of such ensembles.
- Sometimes called statistical physics or **statistical thermodynamics**, its applications include many problems in the fields of physics, biology, chemistry, and neuroscience.
- ➤ Its main purpose is to clarify the properties of matter in aggregate, in terms of physical laws governing atomic motion
- > Statistical mechanics arose out of the development of classical thermodynamics, a field for which it was successful in explaining macroscopic physical properties—such as temperature, pressure, and heat capacity—in terms of microscopic parameters that fluctuate about average values and are characterized by probability distributions.
- The founding of the field of statistical mechanics is generally credited to three physicists:
- ➤ Ludwig Boltzmann, who developed the fundamental interpretation of entropy in terms of a collection of microstates

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- ➤ James Clerk Maxwell, who developed models of probability distribution of such states
- > Josiah Willard Gibbs, who coined the name of the field in 1884
- ➤ While classical thermodynamics is primarily concerned with thermodynamic equilibrium, statistical mechanics has been applied in non-equilibrium statistical mechanics to the issues of microscopically modeling the speed of irreversible processes that are driven by imbalances. Examples of such processes include chemical reactions and flows of particles and heat. The fluctuation—dissipation theorem is the basic knowledge obtained from applying non-equilibrium statistical mechanics to study the simplest non-equilibrium situation of a steady state current flow in a system of many particles.
- (i) Classical Statics Maxwell Boltzmann statics. molecules
- (ii) Quantum statistics Fermi Dirac statistics
 - ½ spin Elementary particle
 - Bose Einstein statics o.spin (or) Integral spin

photons

Phase space (T space):

The combined Position $\Sigma(x, y, z)$ and momentum (Px,Py, Pz) space is called as phase space .

A point in the space represents the Politian and momentum of the particle at some particular instant .

Constraints:

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The restriction imposed by physical laws on the distribution of molecules among the cells in the Phase space are called the constraints of the system

Total no of molecules N

n₁ molecules in cell 1

n₂ molecules in cell 2

n_r molecules in cell r

The constraints required $\sum_{i=1}^{r} n_i = N$

Accessible states the permitted number of microstates under the constraints imposed upon the system are called accessible states.

Total energy be E

Suppose n₁ molecules have energy E₁

Suppose n₂ molecules have energy E₂

We have the constraints $\sum_{i=1}^{r} n_i \, \varepsilon_i = E$

Ensembles:

An ensemble is defined as a collection of large number of assemblies which are essentially independent of one another but which have been made macroscopically as identical as possible.

Micro canonical ensemble:

It is a collection of essentially independent assemblies having the same energy E volume- V and number N of the system all the system are of the same type.

1. The locus of all the phase points having equal energies in phase space is called an energy surface (or) Ergodic surface

E,V,N	E,V,N	E,V,N
E,V,N	E,V,N	E,V,N
E,V,N	E,V,N	E,V,N

- 2. Walls are Rigid, impermeable, well insulated walls
- 3. No exchange of energy (or) particle take place

Canonical ensemble:

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1. It is a collection of essentially independent assemblies having the same temperature –T, Volume- V, and number of identical particles N

T,V,N	T,V,N	T,V,N
T,V,N	T,V,N	T,V,N
T.V.N	T.V.N	T.V.N

[System contacted with a heat reservior]

- 2. Walls are Rigid, impermeable, diathermic walls
- Here system can exchange energy but not particles 3.

Grand canonical ensemble:

1. It is a collection of essentially independent assemblies having the same temperature- T, Volume- V, and chemical potential u

T,V,µ	T,V,μ	T,V,μ
T,V,µ	T,V,µ	T,V,µ
T,V,µ	T,V,µ	T,V,µ

- Walls are permeable, diathermic walls 2.
- 3. Exchange of energy as well as of particles takes place with the heat reservoir

Lioville's theorem:

The theorem consists of two parts

i) The principle of conservation of density in phase space:-

This part states the conservation of density in phase space (ie) the rate of change of density of phase point in phase space is zero $\frac{\partial p}{\partial p} = 0$

ii) The principle of conservation of extension of phase -space:-



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$$\frac{d}{dt} \left(\partial \Gamma \right) = 0$$

Symbol for volume extension

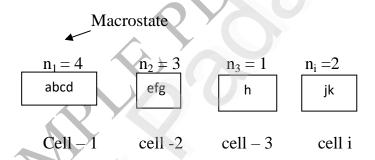
The volume at the disposal of a particular number of phase points is conserved through out the phase space

Microstates:

Each arrangement of specified system (or) molecules with their representative points in particular cell is called microstate

A microstate of an ensemble may be defined by the specification of the individual partition of phase point in each, system (or) molecule of the ensemble.

Macro states: A macrostate of the ensemble may be defined by the specification of phase point in each cell (I,e) by specifying the numbers only and over looking the identities of the system (or) molecule.



❖ There may be different microstates corresponding to the same microstate .

Most probable distribution:

M.P. distribution is a number of particles in each cell is portioned to the size of the cell.

$$g_t = \frac{n_t}{n}$$

 $n_t-number\ of\ particles\ in\ cell\ t$



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- n-Total number of particles
- g_t The probability of any one particle in cell t

Pivilion of phare space in to cells:

Phase space is divided in to 6 dimentioned cells whose sides are dx,xy,dz, and dp_x,dp_y,dp_z . Such cells are called phase cells.

Number of phase cells in the volume element is

$$=\frac{\delta q_{1},\delta q_{2},.....\delta q_{f},\delta p_{1}.\delta p_{2}.\delta p_{f}}{hf}$$

h = is any arbitrary constant

 $h - \delta qi \delta pi$

h_f – size of each cell

- 1) The assemblies in general consist of three types of particles
 - Identical but distinguishable particles
 - Obey Maxwell Baltzmem law
 - ❖ Molecules of a gas are the particles of this kind
- 2) Identical but indistin guishable particles of zero (or) integral spin.
 - Obey Bose Einstein statistics
 - Photons are the particles of this kind
 - Helium at low temp obey Bose Einstein stations
- 3) Indentical but indistinguishable particles of spin ½
 - Obey pauli's exclusion principle and Fermi piracy statics
 - Fermions are the paticls of this kind ex & electron, Protons, neutrons

Maxwell Boltzmann statistics:

❖ Maxwell is used to determine equilibrium state of the system, means, which is most probable

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- ❖ When the gas is in equilibrium the probability is maximum.
- ❖ This law tell us how a fixed amont of energy is distributed among various member of on assembly identical particle.

Consider a system having n disting vishable particles. Let these particles are divided in to quantum on groups such that $n1,n2, \ldots ni$ particles lie in groups having energies $E_1,E_2,E_2 \ldots Ei$ respectively.

Let g_i be the statistical weight of ith quantum group.

The conditions in Maxwell – Bolizman staties are

- 1) Particles are distinguishable (ic) there are no symmetry restriction.
- 2) Each eigen states of ith group may contain 0,1,2, ... n_i particles
- 3) The total no of particles in the entire system is always constant.

(ie)
$$n = n_1 + n_2 + + n_i = \sum ni = constant$$

4) The sum of energies of all the particles in different quantum groups taken together constitue the total energy of the system

Number of particles =
$$Ni = \frac{gi}{e^{\infty} + \beta Ei}$$

 ∞ , B are constant . In terms of temp

$$\beta = \frac{1}{KT} \qquad e^{-\alpha} = \frac{N}{Z}$$

$$Ni = gi \frac{N}{Z} \qquad e \frac{-Ei}{KT}$$

Max well's law of Distribution of velocities:

$$dx = n \left(\frac{m}{2\pi KT}\right)^{3/2} e^{-m} \left(x^2 + y^2 + 2^2\right) / 2KT + dx dy dz$$

Which is the form of the Maxwell distribution law for the no of level having components of velocity in the range x to x + dx, y to y + dy and z to z + dz



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$$dn = \frac{2\pi n}{(\pi KT)^{3/2}} e^{-\sum_{KT}} \varepsilon^{1/2} d\varepsilon$$

gives the number of molecules with Kinetic energy (translational) lying between ϵ and ϵ +d ϵ in any direction. This is known as Maxwell – Boltzmann distribution law of energies.

In M.B statics of perfect g the average K.E per molecules is 3/2 KT.

Mean speed the mean speed \bar{c} is the speed of all particles divided by the total number of particles .

$$\overline{c} = \sqrt{\frac{8KT}{\Lambda m}}$$

$$\overline{c} = 1.5 \quad \overline{c} = \sqrt{\frac{SKT}{\pi m}}$$

$$\overline{c} = 1.59 \quad \frac{kT}{m}$$

← average (or) mean speed

Mean square speed

$$\overline{(c)}^2 = \frac{3KT}{m}$$

Root mean square speed:

c.r.m.s =
$$\sqrt{(c)^2} = \sqrt{\frac{3KT}{m}} = 1.73 \sqrt{\frac{KT}{m}}$$

Most probable speed:



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For the most probable speed the probability of the speed must be maximum.

$$C_{mp} = c \sqrt{\frac{2KT}{m}}$$

R.M.V of the molecule is define by the equ $C^2 = \frac{1}{N} \int_{0}^{\infty} c^2 dN$

Mean free path

The path covered by a molecule between any two consecutive collision is a straight line and is called mean free path.

Number of collision occur the path appears zig zag.

During N collision the distance travelled in s

According to Baltzman
$$\lambda = \frac{3}{4\pi d^2 n}$$

Mean free path
$$\lambda = \frac{S}{N}$$

According to Maxwell
$$=\frac{1}{\sqrt{2\pi d^2 n}}$$

Bose – Einstein Statistics:

The particles are indistinguishable. So, the interchange of two particles between two energy states will not produce any new state.

The condition of B.E statistics are

- 1) The particles are indistinguishable from each other. So, that there is no distribution between the different ways in which n_i particles can be choosen.
- 3) The sum of energies of all the particles in the different quantum groups taken together constitutes the total energy of the system.



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Number of particles $n_i = e^{\alpha} + pEi$

This represents the most probable distribution of the elements among varies energy levels for a system obeying Bose – Einstein statistics Fermi Dirac statistics .

In M-B statistics (or) B.E statistics, there is no restriction on the particles to be present in any energy state But in of Fermi – Dirac, Statistics, applicable to particle like electrons and obeying Pauli exclusion can principle (no two electrons in an atom have some energy state). only one particle can occupy only a single energy state.

Thus in Fermi – Dirac statistics the conditions are

- (1) The particles are indis-tin guidable from each other. (ie) there is no restriction between different ways in which n_i Particles are cho
- (2) Each sublevel (or) well may contain O (or) one particle. Obviously gi must be greater than (or) equal to **ni**
- (3) The sum of energies of all the particles in the different quantum groups taken together constitute the, total energy of the system.

$$ni = \frac{g_i}{e^{\alpha + BEi} + 1}$$

$$\infty = -E_f / KT \qquad \beta = \frac{1}{KT}$$

$$ni = \frac{g_i}{e^-(E_f - E_r) / KT + 1}$$

Fermi energy:

At absolute zero of temp the maximum K.E that a free electron can have is called Fermi energy.

Comparison of the statistics

S.No	Max well Boltz	Fermi – Dirac	Bose – Einstein
	mann		
1	Particles are	Particles are in	Particles are
	distinguishable and	distinguish able and	indistinguishable
	only particles are	quantum states are	and quantum states

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	taken in to	taken into	are taken in to
	consideration	consideration	consideration
2	There is no	Only one particle	No restriction on the
	restriction on the	may be in a given	number of particles
	number of particles	quantum state	in a given quantom
	in a given state		states
3	Applicable to ideal	Applicable to	Applicable to
	gas molecule	electron and	photons and
		elementary long	symmetrical
		particle	particles
4	Volume in six	In Phase space is	In phase space is
	dimensional space	known h ³	known h ³
	is not known		
5	Internal energy of	Even at absolute	The energy at
	ideal gas molecules	zero, the energy is	absolute zero is
	at absolute zero is	not zero	taken as zero
	taken as zero		
6	-	At high tamp Fermi	At high tamp B.E
		distribution	distribution
		approaches M-B	approaches M.B
		distribution	distribution
7	$ni = \frac{g_i}{e^{\alpha + \beta Ei}}$	$\mathbf{ni} = \frac{g_i}{e^{\alpha + \beta Ei} + 1}$	$ni = \frac{g_i}{e^{\alpha + \beta Ei} - 1}$
	\circ		

Black body Radiation:

The most important application of Bose Einstein statistics to electron magnetic radiation in thermal equilibrium, called "Black body radiation".

In quantum theory, radiation energy occurs in energy packets (or) photon (or) light quantum of energy hV and momentum $\frac{hv}{c}$. Photons have zero rest mass and a spin quantum number of 1, they obey Bose – Einstein statistics.

Consider a black body radiation chamber of volume containing radiation in equili brium with the walls at temp T.

Total energy density is

$$\frac{u}{v} = \frac{8\pi h}{c^3} \left(\frac{KT}{h}\right)^4 \frac{\pi}{15}$$

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$$\frac{u}{v} = bT^4 - Stefan - Boltzmann + 2 mann law$$

Where b =
$$\frac{8\pi K^4 \pi^4}{15c^3 h^3}$$

Wein – constructed black body in the from of cylinder. Lummer and kurlban bolometer is used to measure the intensity of heat .

Electron Gas

- ❖ Electrons in the metal are free to move exactly like the particle of gas
- ❖ Free electron gas in a solid obey Fermi Dirac statistics.
- ❖ A metal can be considered to be compiled of a system of fixed positive nuclei and a number of mobile electrons returned to as the electron gas.

Fermi energy
$$E_f = \frac{h^2}{2m} \left(\frac{3n}{8\pi v} \right)^{\frac{2}{3}}$$

Fermi Temp
$$T_f = \left(\frac{E_F}{K}\right)$$

Zero point energy
$$=\frac{3}{5}n \varepsilon_{\rm f}$$

- $\ \ \, \ \ \,$ All the levels below E_F are completely filled
- ightharpoonup All the above E_F are completely empty
- ❖ At T = levwl OK all electrons have energies less than (or) equal to Fermi energy

♣ Degeneracy factor of electron gas =
$$\frac{1}{D} = \frac{h^2}{2 \times 9.1 \times 10^{-28} \times \text{KT}} \left(\frac{3n}{8\pi v}\right)^{\frac{2}{3}} = \frac{10^5}{15T}$$

For electron gas, the classical statistics is not valid, and can be applied only at temperatures of the order of 10^5 K.

At low temp, it is necessary to use F-D statistics to study electron gas in the metals.

Pressure of electron gas
$$P_o = \frac{2}{5} \frac{n \epsilon_f}{v}$$



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$$=\frac{nh^2}{20mv}\left(\frac{3n}{\pi v}\right)^{\frac{2}{3}}$$

Which means at 10^5 atoms normal temperature the pressure of the gas is sufficiently high.

Pauli's theory of par magnetism:

In metals free conduction electrons are present. As each atom is endowed with intrinsic magnetic moment u. it acts like a elementary magnet. Thus all free electrons acting as elementary magnets, can orient them selves in the direction of an applied magnetic field Band make metals highly paramagnetic.

Let us consider an assembly of N free fermions of spin $\frac{h}{2}$ each of which is describe by a single particle Hamiltonian.

$$H = \frac{P^2}{2m} - \overrightarrow{\mu} \cdot \overrightarrow{B}$$
 and the single particle, energy levels

$$E_{is} = \frac{P^2}{2m} - \mu SB$$
 Where $S = \pm 1$

Intensity of magnetization I = totalmagnetcmoment Volume

$$= \frac{\mu \left(\overline{N_+} - \overline{N} \right)}{V}$$

 $\overline{N_+}$ - average no of molecules spin up to

 \overline{N}_{-} - average no of molecules spin down to

μ- magnetic moment

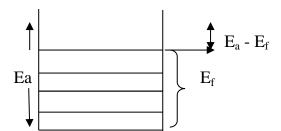
Thermionic emission:

In free electron model of a metal, thezero of the energy is taken at the bottom. At the absolute zero of temp, the electrons will fill $\ n/2$ lowest energy states up to the energy value $\ \epsilon_f$

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The minimum amount of energy necessary to remove an electron from the metal is equal to $(E_a$ - $E_f)$ and is defined as the work function ϕ of the metal.

Emission current density as per unit area = $J = AT^2 e^{-e\phi/KT}$

eφ is called Work function

$$e\phi = E_a - E_f$$

$$A = \frac{4\pi mek^2}{h^3}$$

This equation is called Richardson – Dush man equation of thermionic emission.

As the temp of the filament is doubled, thermionic currant increases 4 times.

Gas degeneracy , the deviation from perfect gas behaviorus exhibited by Bose – Einstei ga is termed as degeneracy .

The gas degeneracy is obviously a function of $=\frac{1}{D}$

$$\frac{1}{D} = \frac{n}{gsZt}$$
 Here Zt – translation Partition function

Phonon gas

- ❖ Quantum of acoustical energy is commonly referred as phon-on
- ❖ Phonon Vibrates with the frequency of 10⁴ to 10¹³ cycles per second
- Low frequency part is acoustic range

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- ❖ High frequency part is infra red range
- ❖ In solid it travels like a short elastic waves, In solid travels with, the velocity of sound
- ❖ In elastic ether medium travels with the velocity of light.
- ❖ Indistinguishable particle
- More phonons can be created by increasing the temp of the crystal Momentum $P = \frac{h}{}$

Properties of Liquid Helium (An application of B.E statistic)

Liquefaction of helium

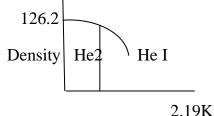
Helium was the last gas to be liquefied because of it extremely low critical presser

Tc = -5.25K

- ❖ Temperature of inversion Ti for Helim is 33K
- ❖ Kamerling onnes precooled helim to 23K by means of liquid hydrogen boiling under reduced pressure and then liquefied it by subjecting it to J.T expansion.

Properties of liquid helium:

- ❖ Kamerling onnes found a specific discontinuity in the density of helium at 2.19K
- ❖ The dencity of liquid helium increases as the temp decreases from 4K to 2.19K



۷.

Temp

❖ The density becomes maximum (146.2 kg/m³) at 2.19K

Thus liquid helium which is contracting when cooled, suddenly begin to expand below 2.19K

Later Keesan also found another specific discontinuity at 2.19K.

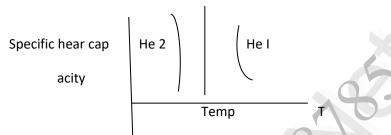
1. He measured the specific heat capacity of helium at different temp.

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2. As helium is gradually cooled from 4.2K the specific heat capacity remain constant at first and near 2.19K it increases a little



- 3. Exactly at 2.19.12 S.P. heat capacity increases suddenly to a ney large rule. Then it gradually falls as the temperature is reduces from 2.19.12.
- 4. The graph resembles the Greek letter λ and hence in this temp at which the S.P. heat changes abruptly is called the λ point.
- 5. The properties of liquid helium above and below λ point are quite different.
- 6. Liquid helium above 2.19K is called Helium I and it behave in a normal manner.
- 7. Liquid helium below 2.19K is called helium II, because of its abnormal properties.

Helium II is called superfluid why?

- ❖ Co- efficient of viscosity of liquid, increase with decrease in temperature .
- Viscosity of liquid helium decrease with decrease in temp.
- The viscosity of helium II is almost zero and it can flow rapidly through narrow capillary tube.
- ❖ Hence it is called a super fluid.

Some peculiar properties of Helium II:

Extreme fluidity:

He II has practically zero viscosity and is called super fluid.

***** High heat conductivity:

He II has on extra ordinarily high co-efficient of thermal conductivity. He II is said to be about 800 times more conducting than copper .

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Principle of equi portion of energy:

The law states that the total 12KE of a dynamical system consisting of a large number of particles. InGeneral is equally divided among its all the degrees of freedom.

The average energy associated with each degree of freedom is ½ KT.

The Relation between the partition function (z) and thermo dynamic quantities.

Various thermodynamical quantities such as energy E, Helm – holtzs free energy, Entropys 3 and specific heat $C_{\rm v}$ etc....

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Energy E = RT²
$$\frac{\partial}{\partial T}$$
 (logZ)
= $\frac{RT^2}{Z}$ $\left(\frac{\partial z}{\partial T}\right)$

Helum holtz free energy
$$F = -RT \log z$$
 and $Cv = \left(\frac{\partial E}{\partial T}\right)_{V} = \frac{\partial}{\partial T} \left[\frac{RT^{2}}{z}\left(\frac{\partial z}{\partial T}\right)\right]$

Comparison of Ensembles

S.No	Property	Microcomonical	Canonical	Grand
			0-	canonical
1	Contact with the	Isolated system, (ie)	System in	System can
	environment	energy and the	thermal	exchange both
		number of particles	contact with	energy and
		of the system are	heat reservoir.	particles (-2 +
		constant E,V,N	(ie) system can	nu –E) / KT
			exchange	$(\Omega + nu - E)$
			energy but not	\overline{KT}
			particles	
2	Probability	P(E) = constant in	$P(E) = Ae^{E/KT}$	P(n) = e
	distribution	range E and E + dE		
		= O. out side this		
		range		
3	Fluctuation	None	In energy only	In energy and
				number of
				particles
4	Partition function	ΔΓ	$Z = \int^{-BE} d\Gamma$	$Z = {\epsilon \over n} e^{un/-z}$

Some important points:

- All accessible microstates, corresponding to possible macro states are equally probable.
- An equilibrium microscopic state is one for which the number of microscopic state is maximum.
- ightharpoonup Stirling's approximation to find n! logn! = n logn n
- ❖ The classical partition function z gives the sum of states of the system.
- ❖ The partition function Z is related to the thermo dynamical quantities in the following way.



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$$S = Nk \log z + \frac{3}{2} KT$$

$$S$$
 – en tropy

$$NK = R$$

$$S = R \log Z + \frac{E}{T}$$

More points in phase space:

The phase space available to the 3- dimensional harmonic oscillator having energy between E and E + dE, is given by

$$\delta A = 2\pi \sqrt{m/K} \delta E$$

A – Area of the ellipse

A – semi major axis

B - semi minor axis = πab

$$A = 2\pi E \sqrt{m/K}$$

Volume of phase space:

$$\Delta \tau = 4\pi P^2 \, dp. V$$

P – momentum

V = Volume in ordinary space

Number of phase cells in given energy range of

harmonic oscillator
$$=$$
 $\frac{Area \text{ of phase space}}{Area \text{ of phase cell}}$

$$=\frac{E_{v}}{h}=\frac{E}{hv}$$

No of phase cells in the given energy range for 3- dimensional free particle.

$$=\frac{4\pi v}{3h^3}$$
 (2mE) $\frac{3}{2}$

 h^3 = volume of phase cell.

The unit of phase space volume is Kg³ m⁶ s⁻³ (or) J³ S³

Gibbs function:

$$G = F + Pv$$

H- enthalpy

$$G = H - Ts$$

F- Helmholl2fn

$$G = U = TS + PV$$

s - entropy



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U – Internal energy

Gibbs function -pdv - work

- 1. Gibbs function has also be called the free energy of a system
- 2. Gibb's function is also known as thermo dynamical potential
- 3. Gibb's function is the difference between enthalpy and latent energy
- 4. Gibb's function is constant in sublimation

Gibbs paradox:

It the particles in the two systems are the same and if for convenience we take

$$V_a = V_b = v$$
 $n_a = n_b = n$.

We have to consider 3n particles in a volume 2v.

We get
$$S_{ab} = S_a + S_b + 2nK \log_e^2$$

Which shows that by joining two moles of two different gaves by removing a partition between than, the entropy of the joint system increases by an additional factor $2nK \log_e^2 which$

Can not be accounted.

This is called Gibbs paradox:

- ❖ Gibbs paradox can be resolved, by the removal of partition, by considering the two systems as the same .
- Hence the gas molecules are completely identical and indistinguishable.
- ❖ Gibbs paradox is thus resolved by a concept of quantum mechanics
- ❖ Gibbs paradox in statistical mechanics can be resolved if the Maxwell Boltzmann constant is divided by N!

Thermodynamics & statistical Mechanics

Polytechnic

Laws of thermodynamics:

1) Zeroth law:

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If two systems are separately in thermal equilibrium with a third, they will also be in thermal equilibrium.

Equation of state:

At low pressure Pv = nRT for all gases (ideal) but real gases don't have this equation.

At high pressure, there is correction in P and V so that

$$(P + \frac{a}{v^2})$$
 (V-b) = RT \Longrightarrow Vander waal's equation V- Volume of gas

$$P = \frac{RT}{V - b} - \frac{a}{v^2}$$

Critical constants:

$$Pc = \frac{a}{27b^2}$$
; $T_c = \frac{8a}{27}$; $Vc = 3b$

When a,b, are critical constants then $\frac{RTc}{PcVc} = \frac{8}{3}$; Boyle's temperature $T_B = \frac{a}{Rb}$ temperature inversion $T_i = 2 T_B = \frac{2a}{Rb}$.

Work done in various process:

- 1) sothermal process W = RT ln $(\frac{V_2}{V_1})$
- 2) adiabatic Process W =?
- 3) Isochoric Process $W = \int P dv = 0$
- 4) Isobaric process $W = P(V_2 V_1)$

First law of thermodynamics:

The change is heat of a system is dQ = du + dw

$$dQ = du + Pdv$$



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Heat capacity:

$$C_v = \left(\frac{2Q}{2T}\right)_v \frac{1}{m}$$
 m = mass of the gas

$$dQ = m C_v \Delta T$$

$$Cp = \left(\frac{2Q}{2T}\right)_p \frac{1}{m}$$
; $dQ = m Cp\Delta T$

Heat conduction: $\frac{dQ}{dt} = -KA \frac{dT}{dx}$

- Arr Cp Cv = R is called Mayer's relation
- $TV^{\gamma-1}$ = Constant adiabatic equation in T & V
- ❖ PV = Constant isothermal equations
- Cp = $\left(\frac{\partial H}{\partial T}\right)_n$ Where H = U + PV; H enthalpy
- F = U-Ts; G = F + PV F = Helmholtz+2 free function

G – Gibbs free function

Chemical potential:

It governs the flow of particles between two systems ie the particles flow from the system of higher chemical potential to the systems of lower chemical potential.

$$\mu = \left(\frac{2F}{2n}\right)_{\text{T,V}}; \ \mu = \left(\frac{\partial G}{\partial m}\right)_{\text{T,P}}$$

 $dF = (\mu_1 - \mu_2)dn$; F always decreases (or) remains constant

 $\mu_1 > \mu_2$ means the system at higher chemical Potential are transferred to the system at lower chemical Potential.

Phase equilibrium:

$$\mathbf{G} = \mu_1 \, \mathbf{n}_1 + \mu_2 \, \mathbf{n}_2$$

$$d_G = \mu dn_1 + \mu dn_2$$

At equilibrium $d_G = 0$; $dn_1 = -dn_2$

ie = $\mu_1 = \mu_2$



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Thus one component system having two Phases in equilibrium, the chemical Potential of the two phases must be the same.

Clausius – clapeyron equation (or) I-Latent heat equilies:

$$dP/dT = \frac{L}{T(V_2 - V_1)}$$
. L-latent heat

At boiling point: $v_2 > v_1$

$$v_2 - v_1 = +ve$$
; $dP/dT = +ve$

the boiling point of a liquid must rise or fall according as P increases or decreases

At Melting Point:

 v_2 - v_1 = -ve like ice which contract on melting

= +ve like paraffin which expand on melting

 $\frac{dP}{dT}$ = - ve melting points decrease with increase of pressure

When $v_2 = v_1$:

 $v_2 - v_1 = 0$; $dP/dT = \infty$ (or) $\ell = 0$ thus when a liquid passes in to vapour state with little no absorption of heat at a temperature to the critical point . $\ell = 0$.

In fusion th specific volume of liquid and solid are nearly same v_2 - v_1 is very small ie $dP/_{dT}=\infty$

Richardson – Dustmen's equation:

$$I = AT^2 e^{-s}/KT$$

I - thermo unic current; T - temper unto of to filam -eul

Claudius equation (or) II latent heat equation:

$$C_2 - C_1 = \frac{d\ell}{dT} - \ell / T$$



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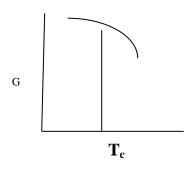
Changes of phase I – Order phase change:

Let
$$dG = -SdT + Vdp = Vdp - SdT$$

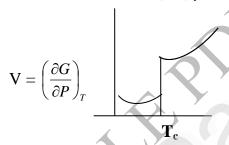
isothermal – isobaric process (T- Constant, P-Constant)

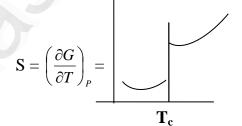
$$dG = 0$$
; $G = constant$

to the value of specific Gibbs potential is same continuous in either phase (liquid > Solid; vapour)



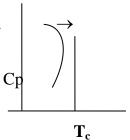
The first derivatives of G; $\left(\frac{\partial G}{\partial P}\right)_T = V \& \left(\frac{\partial H}{\partial T}\right)_p = S$ are a discontinuous change





The heat capacity $Cp = T \left(\frac{\partial S}{\partial T} \right)_p$ also discontinuous and attain





II order phase change:

At constant P & constant T there is no . change (continuous) in first - order derivatives of Gibb's Potential

$$S = \left(\frac{\partial G}{\partial T}\right)_P + V = \left(\frac{\partial G}{\partial P}\right)_T \text{ transition from one phase into the other}$$

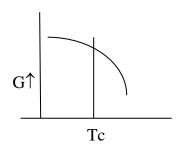


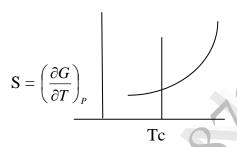
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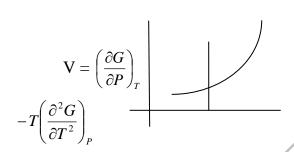
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- The heat capacity $C_p = \left(\frac{\partial S}{\partial T}\right)_p$ changes discontinuously but does not becomes infinite
- ❖ The Gibbs Potential change continuously ie same in either phase.







 $Cp\uparrow$ Cp =

Tc Tc

The second order phase change is characterized by discontinuous changes in the second order derivatives $\left(\frac{\partial^{2G}}{\partial T^{2}}\right)_{n}$ of Gibb's potential

Examples of II order phase change:

- * Translation of ferro magnetic material into a Paramagnetic at curie point
- Order disorder transitions of certain alloy & chemical compounds at a definite temperature

Planck's radiation law:

The commission of energy takes place in discrete integral multiple of a minute elementary unit of energy called quantam (E=hv)

The total energy of variations between the wavelength range $\lambda \& \lambda + d\lambda$ is

$$dE = \frac{8\pi}{\lambda^4} \quad \frac{hc/\lambda}{e_{-1}^{hc/k\lambda T}} \qquad d\lambda = \frac{8\pi}{\lambda^5} \quad \frac{hc}{e_{-1}^{hc/\lambda kT}} \quad d\lambda$$



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When
$$hc/\lambda kT \ll 1$$
 ie low f; high λ = when $\frac{w^2}{\pi^2 c^3}$ KT Rayleigh – Jean's law

When
$$hc/\lambda kT >> 1$$
 high low $\lambda = \frac{\hbar w^3}{\pi^2 c^3}$ which is wien's law

Bose – Einstein condensation:

If the no. of density of particles is increased (or) temperate is reduced, then the behavior of the gas departs more and more from the behaviour of a perfect ideal gas. It is called degeneracy.

Let us consider equation
$$N = N_0 + \frac{V}{h^3} (2\pi m kT)^{\frac{3}{2}} \frac{2}{\sqrt{\pi}} \int_0^{\infty} \frac{\sqrt{x} dx}{e^x - 1}$$
 (or)

$$N = N_0 + \frac{V_{h^3}}{(2\pi \text{ m kT})^{3/2}} \xi(3/2)$$

$$N_0 = N + \frac{V_{h^3}}{(2\pi m kT)^{3/2}} \xi (3/2)$$

Thus as T – decrees, the number of partied in the ground state $\left(N_{_{0}}\right)$ increases. At absolute Zero $\left(O^{o}K\right)$ all the partides condense in to the zero-energy ground state. This is called B.E condensation eg above 2.17K helium is called He –I; below phase 2.17k is known as

He- II ; λ - point is called transition temperature . The normal fluid costs is of He – atoms in the excited state & in super fluid consists of He – atoms in the ground state . He- II has zero viscosity and infinite thermal conductivity

Einstein Model $\varepsilon = (n + \frac{1}{2}) \hbar w$ discrete values of energy the average energy

of an oscillator =
$$\frac{\hbar \omega}{e_{-1}^{\hbar w/_{KT}}}$$
 for N – oscillator – 3 degres of freedom $\varepsilon = \frac{3N\hbar w}{e^{\hbar \omega/_{KT}}} - 1$

$$Cv = \frac{\partial E}{\partial T} = 3NK \left(\frac{\hbar \omega}{KT}\right)^{2} \qquad \left(e^{\hbar \omega/KT} - 1\right)^{2}$$

At high temp
$$e^{\hbar w/KT} = 1 + \frac{\hbar \omega}{KT} + \dots$$



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$$Cv = 3NK \left(\frac{\hbar\omega}{KT}\right)^{2} \quad \frac{\left(1 + \frac{\hbar\omega}{KT}\right)}{\left(\hbar w/KT\right)^{2}} = 3NK \left(1 + \frac{\hbar\omega}{KT}\right)$$

Ps T
$$\rightarrow$$

$$C_v = 3Nk = 3R$$

At low temperature

$$Cv = 3NK \left(\frac{\hbar w}{KT}\right)^{2} \qquad \frac{e}{\left(e^{\frac{\hbar w}{KT}} - 1\right)^{2}} = 3NK \left(\frac{\hbar w}{KT}\right)^{2} \cdot \frac{1}{e^{\frac{\hbar w}{KT}}}$$

Debye's Model:

The atoms in a solid cannott be assumed to be independent, but we must take in to account their cooperative interactions.

The energy of the system is

$$E = 9NKT \left(\frac{KT}{\hbar w}\right)^{3} \int_{0}^{\theta} \frac{D}{T} \frac{x^{3} dx}{e^{x} - 1}$$

When
$$\theta_D = \frac{\hbar w}{K}$$
; $x = \frac{\hbar w}{KT}$

At high temperature $T >> \theta_D$

$$\frac{x^3}{e^x - 1} = \frac{x^3}{\left(1 + \frac{x}{1} + \frac{x^2}{2}\right) - 1}$$

$$\therefore E = \frac{9NKT}{x^3} \left(\frac{x^3}{3} \right) = 3NKT$$

$$C_v = \frac{\partial E}{\partial T} = 3NK = 3R$$

At low temperature $T << \theta_D$ $\int_0^{\theta} \frac{x^3}{e^x - 1} dx = \frac{\pi^4}{15}$

:.E = 9NKT
$$\left(\frac{KT}{\hbar w}\right)^3 \cdot \frac{\pi^4}{15} = \frac{9\pi^4 NK^4}{15\hbar^3 w^3} T^4$$

$$Cv = \frac{2E}{2T} = \frac{9NK^4}{60 h^3 w^3} T^3$$

 $C_v \propto T^3$ = This law known as Debye T^3 law



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Quantum statistics: (B.E &F.D)

B.E

 \bullet The total number of particle in perfect B.E gas is n =

$$\frac{V}{h_3} (2\pi \text{mKT})^{\frac{3}{2}} \left[A + \frac{A^2}{2^{\frac{3}{2}}} + \frac{A^2}{2^{\frac{3}{2}}} + ... \right]$$

• The energy of the particle of perfect B.E gas $E = \frac{3}{2} \frac{V}{\hbar^3} \frac{V^{(2\pi mKT)^{3/2}}}{KT(A+1)^3}$

$$A + \frac{A^2}{2^{\frac{5}{2}}} + \frac{A^2}{3^{\frac{5}{2}}} + ...$$

F.D:

Weak degeneracy:

Total number of particle of prefect F-D gas

•
$$n = g_s \frac{V}{h_3} (2\pi mKT)^{\frac{3}{2}} [A - \frac{A^2}{2^{\frac{3}{2}}} + \frac{A^2}{3^{\frac{3}{2}}} ...]$$

$$E = \frac{3}{2} gs \frac{V}{\hbar^3} (2\pi nKT)^{\frac{3}{2}} KT(A - \frac{A^2}{2^{\frac{5}{2}}} + \frac{A^2}{3^{\frac{5}{2}}} - \dots)$$

$$\star E_n = \frac{3}{2} \text{ KT } \left[1 + \frac{A}{2^{\frac{5}{2}}} - \frac{A}{2^{\frac{5}{2}}} + \dots \right]$$

Ideal gas:

* E =
$$\frac{3}{2}$$
 gs $\frac{V}{h^3}^{(2\pi mKT)^{\frac{3}{2}}}$ KTA

$$E_n = \frac{3}{2} \text{ KT}$$

Equation 1 & 2 is known as Ehrenfest's equation.

Statistics : (B.E, F. + M.B)

Stilling approximation

 $\log n! = n \log n - n$



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M.B The number of ways n_i particles arranged is The total number of microstates

$$\Omega = \frac{Ni}{\pi ni} \pi g_i^{ni}$$

The Grand Canonical Distribution:

The most probable distribution of assemblies in grand canonical ensemble is given by

 $M_{N_i} = e^{\alpha N + \beta E_{N_i}}$ and the grand canonical partition function

$$Q = \sum_{N} \sum_{l} \exp \left(\frac{\mu N - E_{Ni}}{KT}\right)$$

Thermo dynamical Properties of Grand Canonical Ensemble:

1. S= K
$$[1nQ + \frac{\overline{E} - \mu \overline{N}}{kT}]$$

2.
$$P = kT \frac{\partial}{\partial V} (In Q)$$

3.
$$\mu = U - Ts + PV$$

4.
$$\overline{E} = kT^2 \frac{\partial}{\partial T} (\ln Q) + \mu kT \frac{\partial}{\partial \mu} (\ln Q)$$

5.
$$PV = kT \ln Q$$

Semi – Classical Grand Partition Function:

The grand partition function in terms of chemical potential µand

Partition function Z per system is given by

$$Q = \exp\left(Ze^{\frac{\mu}{kT}}\right)$$

The mean number of systems in the ι th assembly $\overline{N} = kT$

$$\left(\frac{\partial}{\partial \mu} \left(Z e^{\frac{\mu_{\text{kT}}^T}{}} \right) \right)_{\text{V,T}}$$

Microcanonical Ensemble

The Microcanonical Ensemble:

The ensemble in which system has same fixed energy and also the same number of particles is called a microcanonical ensemble



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Partition Function:

Partition function indicates how the gal molecules of an assembly are distributed or partitioned among the various energy levels.

$$Z = \sum_{i} g_{i} e^{-\epsilon i/kT}$$

Translational partition function for a gas molecule : $=\frac{V}{h^3}(2\pi mkT)^{\frac{3}{2}}$

Properties Relating Partition Function and Thermodynamical Quantities

- 1. Entropy: $S = Nk \text{ In } Z + \frac{3}{2} Nk$
- 2. Free energy: F = NkT In Z
- 3. Total energy : $E = NkT^2 \left(\frac{\partial (InZ)}{\partial T} \right)_V$
- 4. Enthalpy: $H = NkT^2 \left(\frac{\partial (InZ)}{\partial T} \right)_V + RT$
- 5. Gibb's potential G: $G = NkT^2 \left(\frac{\partial (InZ)}{\partial T}\right)_V + RT NkT InZ \frac{3}{2}Nk T$
- 6. Pressure : $P = NkT \left(\frac{\partial (InZ)}{\partial T} \right)_T$
- 7. Specific heat at constant volume Cv

$$Cv = Nk \left[2T \frac{\partial (\ln Z)}{\partial V} + T^2 \frac{\partial^2 (\ln Z)}{\partial T^2} \right]$$

Virial Coefficient:

Consider the real gas, virial expansion is given by $\frac{PV}{NkT} = 1 + \text{correction}$

$$=\sum_{i=1}^{\infty}a_1(T)\left(\frac{\lambda^3}{\nu}\right)^{i-1}$$

Where
$$a_1 = 1$$
 or $\frac{PV}{NkT} = 1 + a_2 \frac{\lambda^3}{V} + a_3 \left(\frac{\lambda^3}{v}\right)^2 + \dots$ and $a_2 = \frac{2\pi}{\lambda^3} \int_0^\infty (1 - e^{-\beta\mu(r)}) r^2 dr$

... $B_2(T) = a^2 \lambda T^3$ is known as second virial coefficient for perfect gas $\frac{PV}{NkT} = 1$

For real gas,
$$\frac{-PV}{NkT} = 1 + \frac{B_2(T)}{V}$$

Note -2^{nd} virial coefficient:

I. If B_2 is negative, then P is less than the ideal gas



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- II. If B_2 is positive, P is more than the ideal gas where V, N, T are constants. Put B_2 (T) = o for calculating the Boyle's temperature.
- III. Boyle's temperature for a hard sphere is not defined because B₂ (T) is independent of

The factor 2Nk In 2 arises due to the distinguishability of classical particles and is known as the mixing term.

Semi – Classical Gas:

It consists of indistinguishable particles

$$Z = \frac{V}{h^3} (2\pi mkT)^{\frac{3}{2}}$$
 and $S = Nk \left[In \frac{V}{Nh^3} (2\pi mkT)^{\frac{3}{2}} + \frac{5}{2} \right]$ is also known as

Sackur – Tetrode equation for the entropy of a semi – classical gas.

Free energy :
$$F = -kT \left[\text{In } \frac{Z^N}{N!} \right]$$

$$F = -kT \text{ in } (Z)$$

Total energy:
$$E = NkT^2 \frac{\partial}{\partial T} (In Z)$$

Pressure :
$$P = NkT \left[\frac{\partial}{\partial V} (InZ) \right]$$
 and gas equation is $PV = NkT$

Separation of Partition Function:

The total partition function can be expressed as the product of the partition function for individual degrees of freedom . $Z = Z_t Z_r Z_v Z_e$

Canonical Ensemble

The Canonical Ensemble:

In the canonical ensemble the assemblies are having the same volume V, number of system N and are in thermal contact with each other so that they are in equilibrium and have the same temperature T.

The canonical partition function is given by $Z = \sum e^{-E_{kT}}$

The Modynamical Properties of the canonical ensemble:

(i) Entropy:
$$S = \frac{E}{T} + k \text{ In } Z$$
 (ii) Free energy: $F = -kT \text{ In } Z$

(ii) Free energy :
$$F = -kT$$
 In Z

(iii) Pressure :
$$P = \sum_{i} P_{i} \left(\frac{\partial E_{i}}{\partial V} \right)_{N}$$
 (iv) Chemical Potential : $\mu = \sum_{i} P_{i} \left(\frac{\partial E_{i}}{\partial V} \right)_{V}$

Total Partition Function:



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The canonical Partition function of the semiclassical ensemble is given as $Z = \frac{z^N}{N!}$ and classical expression $Z = \frac{1}{h^3 N} \int e^{-E/kT} d\tau$.

Thermo dynamical Properties of a Real Gas:

The real gas particles exert a force of attraction on each other. The total energy of the gas is made up of the kinetic energy of the motion of the gas particles and potential energy of interactions between them.

(i) Total energy:

$$E = \frac{1}{2m} \sum_{i=1}^{N} (P_{x_i}^2 + P_{y_i}^2 + P_{z_i}^2) + \sum_{i=1}^{N} \sum_{j>1} U_{ij}$$

(ii) Partition function:

$$Z = \frac{1}{h^3 N!} (2\pi m kT)^{3N/2} Z_r$$

(iii) Fermi energy:

$$Z = -kT \left[In \left\{ \frac{\left(2\pi mKT\right)^{3N/2}}{2} \right\} + In Z_{r} \right]$$

(iv) Pressure:

$$P = \frac{NkT}{V}$$

(v) Gibb's free energy:

$$G = kT \left[-\ln Z + \left(\frac{\partial \ln Z_r}{\partial \ln V} \right)_T \right]$$

(vi) Entropy:

$$S = k \left[\ln Z + \left(\frac{\partial \ln Z}{\partial \ln V} \right)_T \right]$$

(vii) Specific heat:

$$C_{v} = K \left[2 \left(\frac{\partial \ln Z}{\partial \ln T} \right)_{V} + T^{2} \left(\frac{\partial^{2} \ln Z}{\partial T^{2}} \right) \right]$$



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The Grand Canonical Ensemble

The Grand Canonical Ensemble:



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The grand canonical ensemble is a collection of independent assemblies having the same temperature T, volume V and the chemical potential μ .

Partition function is $Z = \frac{V}{h^3} (2\pi mkT)^{3N/2}$ entropy $S = NK \log Z + \frac{3}{2}NK F.$

ideal gas

Helmholtz free energy $F = E - Ts = NKT \log_e Z$

Total energy (E)
$$\bar{\varepsilon} = \frac{E}{N} = \frac{\sum \text{ni } \varepsilon i}{\sum ni}$$

 $\bar{\varepsilon}$ = average energy of assembly of 'N' independent systems.

$$E = NkT^2 \left[\frac{2\log z}{2T} \right]$$

Enthalpy (H) H = E + Pv

$$H = NKT^2 \left[\frac{2^{\log z}}{2T} \right] + RT$$

Gibbs potential (G) $G = H-TS = log Z - \frac{3}{2}NKT$

B.E:

The total number of possible ways in which n_i particles can be distributed g_i section is

$$i\frac{gi[(n_i+g_i-1)!]}{n_i! g_i!}$$

The total number of distinguishable arrange mats are given by

$$G = \pi \frac{(n_i + g_i)i}{n_i!g_i!}$$

Eg '2' identical particles, which can be any one of '3' Singh particle state, the number of states (w) of the system an possible in B.E statics is

$$N_i = 2; g_i = 3$$

$$W = \frac{(N_i + g_i - 1)i}{n_i!(g_i - 1)!} = 6$$

F.D: The number of distinguishable arrangements of n_i particles in g_i cells are

$$\frac{g_i}{n!(g_i-n_i)}$$



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The total number of regress states of the whole system is π

$$\frac{g_i!}{n_i!(g_i-n_i)!}$$

Black body radiation:

- \star λT = Constant wine's displacement law = 0.289 cm -k
- ❖ Stefan's Boltzmann radiate w $E = \sigma T^4$
- Wien's law $\frac{e_{\lambda}}{e_{\lambda}} = \left(\frac{T}{T}\right)^5$
- Average energy of planek's oscillator $\overline{E} = \frac{hv}{\left(e^{hv/K_{i}}\right)}$
- Stefari's constant $\sigma = \frac{2\pi^5 K^4}{15a^2 h^3}$

u every density

- Pressure of radiation (diffuse) $P = \frac{1}{3}^{u}$ for perfect reflector $P = \frac{2}{3}^{u}$
- Plank's distribution law energy density $u(v) = \frac{8\pi\gamma^3}{c^3} = \frac{h\gamma}{\left(e^{h\gamma/k_T} 1\right)} d\gamma$
- * $\frac{8\pi hc}{\lambda^5}$ $\frac{1}{e^{\frac{hc}{\lambda}KT}-1}$ d λ $C = \gamma\lambda$ -obeys B.E states is * Small γ (or 0 laye ' λ '
- $* μ (γ) = \frac{8πγ^2}{λ^5}$ KTdv Raleigh jeens $law = E λ dλ = \frac{8πKT}{λ^4} dλ$
- ♦ Her laye γ (or) small 'λ' $u(v) = \frac{8\pi hc}{\lambda^5} e^{\frac{1}{hc/KT}}$
- ♦ Wien's law $\therefore d\gamma = \frac{C}{2^2} d\lambda$

Holium – II

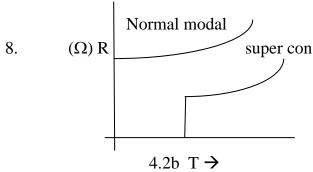
- Never bubbles
- ❖ He I & He II both same type of entropy and continues across the curve
- ❖ Viscosity increase as temperatune decrease in normal liquid (He −I)
- ❖ He II has almost Zero viscosity behavior high heat conductivity internal friction is zero

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- Viscosity of He II $\approx 10^{-3}$ / He II = 10^3 He II viscosity of He I
- * Heat conductivity He II = 800 times of 'w'
- * Electrical resistant is almost zero
- * Super fluid bean of zero vistosity
- ❖ He-I heat conductivity in order of 10⁻⁴ bet He- II very high



M.B F.D B.E
$$n_{i} = \frac{gi}{e\beta \in_{i}} \qquad n_{i} = \frac{gi}{e^{\prec} + \beta \in_{i} + 1} \qquad n_{i} = \frac{gi}{e^{\prec} + \beta \in_{i} - 1}$$
Who $\infty = \frac{h1}{KT}$; $\beta = \frac{1}{KT}$

At high 'T' \prec - very low $A = e^{-\alpha} << 1$ terms $e^{-\alpha} + \beta \epsilon 1$ very lase compane '1' so the F.D & B.E becomes M.B.

- ❖ Fermion → electron, proton, Neutron, -positron & holes (F.D)
- ❖ Bosons → Photons, Phonons, mesons, ∞ particle & He II (B.E)
- ❖ O₂,H₂ are mole obey M-B has any spin value
- ❖ F.D particles only can not be zero energy at absolute zero temperature
- ***** Boltzmann's statistical definition for entropy is $S = K \log \Omega$
- Spin degeneracy Gs = (2S + 1) S-spin

Fermi temperature
$$T_f = \frac{\epsilon_f(0)}{K} = \frac{h_1 F}{K} = \frac{h^3}{2mK} \left(\frac{3n}{4\pi rgs}\right)^{\frac{2}{3}} = \frac{h^2}{2m^{\frac{5}{2}}K} \left(\frac{3\rho}{4\pi rgs}\right)^{\frac{2}{3}}$$

- ❖ when $(g_s = 2s + 1)$
- $\in_f (0) = h1F = \frac{h^2}{2m} \left(\frac{3n}{4\pi vgs} \right)^{\frac{2}{3}} = \left(\frac{n}{v} = \ell \right)$
- Zero Point energy of \bar{e} gas $E_0 = \frac{3}{5} n \in (0)$
- \bullet Zero point energy of \overline{e} gas pressure



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Physics Unit – IV **Previous Year Questions**

2001:								
1.	The value of permittivity of free space in C ² N ⁻¹ m ⁻² is							
	A) $36 \pi \times 10^9$ B) 36	$6 \pi \times 10^{-9}$	C) 10 ⁻⁹ / 36	π D) 36π				
2.	The total normal electric flux over a closed surface surrounding a charge is							
	A) directly proportional to	the charge						
	B) Inversely proportional to the charge							
	C) directly proportional to the square of the charge							
	D) Inversely proportional to the square of the charge							
3.	Laplace's equation for free space is							
	A) $\nabla_2 V = 0$ B) ∇	V = 0	C) $\nabla_2 \mathbf{V} \neq 0$	D) ∇ V \neq 0				
4.	Only one phase point can occupy one phase cell according to							
	A) classical statistics		B) Bose – Einstein statistics					
	C) Fermi- Dirac statistics		D) All of th	iese				
5.	The statistical theory which	ch readily leads	s to Plank's l	aw of radiation is				
	A) Maxwell – Boltzmann	statistics	B) B	ose – Einstein statistics				
	C) Fermi – Dirac statistcs		D) N	lone of these				
6.	The statistical theory which supports the zero point energy of a gas even at absolute zero is							
	A) Classical statistics	B) B.E.Statis	stics C) F	D.Statistics D) All of				
these				,				
7.	According to M.B. statist	ics, the numbe	r of particles	in the given energy range				
	is given by							
	A) $n_i = \frac{Z_i}{Ae^{Ei/KT}}$	B) <i>n</i> _i	$= \frac{Z_i}{Ae^{Ei/KT} - 1}$					
	C) $n_i = \frac{Z_i}{Ae^{Bi/KT} + 1}$	D) <i>n</i> _i	$= \frac{Z_i}{Ae^{Ei/KT} \pm 1}$					
8.	Phase points are endowed with a distinct unchanging individuality of their own,							

- according to
 - A) classical statistics

B) B.E. Statistics

C) F.D. Statistics

- D) None of these
- The number of dimensions of phase space is 9.

A) 3

6

B) 4

C) 5

D)

A divergence in the behavior of an actual gas from that of a perfect gas is 10. referred to as



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	A) entropy of the gas C) thermodynamic probability of the		acy of the gas e of the gas					
2002	<u>– 2003:</u>							
41.	An equilibrium macroscopic state is one for which the number of microscopic							
	states is		~0/2					
	A) zero B) minimum an	d non-zero C) n	naximum D)					
infinit								
42.	As the energy of a cell increases, the number of particles distributed in the cell							
	A) decreases B) increases							
4.0	C) increases and then decreases	D) decreases and t	then increases					
43.	The unit of phase space volume is	C) 3	D) 1 3 6 -3					
4.4	A) $J^3 s^{-3}$ B) Js	C) m ³	D) $kg^3 m^6 s^{-3}$					
44.	Pauli's exclusion principle is imposed on							
	A) Maxwell – Boltzmann statistics		Einstein statistics					
45.	C) Fermi-Dirac statistics D) All these three Planck's law governing the blackbody radiation can be deduced using							
43.	A) Maxwell- Boltzmann statistics		nstein statistics					
	C) Fermi-Direc statistics	D) All thes						
46.	The width of the energy band gap is							
40.			L					
	A) insulators C) metals B) semiconductors D) organic materials							
47.	The value of $(\varepsilon_0 \mu_0)^{-1/2}$ in ms ⁻¹ is	organic materials						
T /.	A) 3×10^8 B) 3×10^7	C) 3×10^9	D) 3×10^6					
48.	The vector $\vec{E} \times \vec{H}$ represents the	C) 3 X 10	D) 3 X 10					
40.) energy per unit area						
) intensity of the wave						
10 🛦	The wave produced by an oscillating	,						
47) cylindrical wave						
~) plane wave						
50.	-	-	heerver at rest the					
50.	If a light source moves with a velocity v towards an observer at rest, the velocity of light (C) as observed by him is							
	A) $C + v$ B) $C - v$	C) C	D) $C \pm v$					
51.	If a sphere is carred by an observer i	,	,					
J1.	A) sphere B) cube	C) plane surface	D) ellipsoid					
52.	As the temperature of the filament is	· •	· •					
•	T	,	•					

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- A) varies exponentially
- B) increases 4 times

C) decreases

- D) decreases 4 times
- 53. Which of the following statements is wrong?

Gibbs function is

- A) also known as thermodynamic potential
- B) the difference between enthalpy and latent energy
- C) a constant in sublimation
- D) a constant in an adiabatic process
- The electrostatic force between two charges separated by 3m distance is 0.075 54.
 - N. If the total charge is 20 μ C, the individual charges are
 - A) 5 μ C, 15 μ C

B) $10 \mu C$, $10 \mu C$

C) 2 μC, 18 μC

- D) 1 μ C, 19 μ C
- 55. Gauss's divergence theorem relates
 - A) line integral and volume integral
- B) line integral and surface

integral

- C) volume integral and surface integral
- D) any two integrals

2003 – 2004:

- Fermi temperature θ_F is given by 56.
 - A) $\theta_F = K \times \theta_F$

- C) $\theta_F = \frac{K}{E_F}$ D) $\theta_F = K + \theta_F$
- 57. Ideal gas molecule is explained by
 - A) Maxwell Boltzmann Statistics
- B) Bose-Einstein Statistics

C) Fermi-Dirac Statistics

- D) All these three
- The displacements of all atoms in a linear triatomic molecule are equal and in 58. the same direction if

A)
$$\omega = \sqrt{\frac{k}{m}}$$

B)
$$\omega = 0$$

B)
$$\omega = 0$$
 C) $\omega = \left\{ \frac{k}{m} \left(1 + \frac{2m}{M} \right) \right\}^{\frac{1}{2}}$

$$\omega = \left\{ \frac{k}{m} \left(1 + \frac{2m}{M} \right) \right\}^{-\frac{1}{2}}$$

- For electron the degeneracy factor is 59.
 - A) Q = 0
- B) Q = 1
- C) Q = 3
- D) Q = 2

- In canonical ensembles 60.
- A) sub-systems exchange particles energy
- B) sub-systems exchange



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- C) sub-systems exchange energy but not particles
- D) sub-systems exchange both energy and particles
- 61. Law of addition of velocities applies only when the two velocities are in
 - A) Perpendicular direction
- B) opposite direction

C) the same direction

- D) all of these
- 62. In Galilean transformation
 - A) Acceleration is invariant
- B) Velocity is invariant

C) time varies

- D) Acceleration varies
- 63. The relativistic mass of a particle moving with a velocity 0.9C is
 - A) 3 m_0
- B) $2 m_0$
- C) $2.3 m_0$
- D) 1.25 m_0

- 64. Minkowski space is
 - A) six dimensional space
- B) four dimensional space
- C) three dimensional space
- D) three dimensional curvilinear space
- 65. The macrostate is defined by
 - A) Pressure, temperature and volume of the gas
 - B) position and velocity component of molecules
 - C) pressure and temperature of the gas
 - D) pressure and volume of the gas
- 66. Bose-Einstein Statistics is applied to the system
 - A) identical and indistinguishable particle
 - B) identical and distinguishable particle
 - C) identical, distinguishable and obeying pauli's exclusion principle
 - D) identical, indistinguishable and obeying pauli's exclusion principle
- 67. The distribution law according to Maxwell-Boltzmann statistics is

A)
$$n_i = \frac{g_i}{f e^{BE_i} - 1}$$

$$B) n_i = \frac{g_i}{f e^{BE_i} + 1}$$

C)
$$n_i = \frac{g_i}{e^{BE_i}}$$

D)
$$n_i = \frac{g_i}{f e^{BE_i}}$$

- 68. Micro- canonical ensemble describes
 - A) The systems which are perfectly insulated
 - B) The system which are in thermal contact with heat reservoir
 - C) The systems which are in statistical equilibrium
 - D) The systems which are in thermal equilibrium



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2004 – 2005:

- Fermi-Dirac statistics is applicable to
 - A) ideal gas molecule

B) electrons of high

- concentration
 - C) photons and symmetrical particles
- electrons of low D)

- concentration
- In a liner triatomic molecule the motion is translation if 70.
- A) $\omega = 0$ B) $\omega = \frac{\sqrt{k}}{m}$ C) $\omega = \left\{ \frac{k}{m} \left(1 + \frac{2m}{M} \right) \right\}^{\frac{1}{2}}$
- $\omega = \left\{ \frac{k}{m} \left(1 + \frac{2m}{M} \right) \right\}^{-\frac{1}{2}}$
- 71. Grand canonical ensemble is one which allows



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- A) The subsystem to exchange energy
- B) The subsystem to exchange number of particles
- C) exchange of both
- D) The subsystem to exchange neither energy nor number of particles
- 72. The microstate is defined by
 - A) pressure and volume of the gas
 - B) pressure and temperature of the gas
 - C) pressure, temperature and volume of the gas
 - D) position and velocity component of the molecules
- 73. Fermi-Dirac statistics is applied to systems of
 - A) identical and indistinguishable particles
 - B) identical and distinguishable particles
 - C) identical and indistinguishable particles obeying pauli's exclusion principle
 - D) identical and distinguishable particles obeying pauli's exclusion principle
- 74. The distribution law according to Bose- Einstein statistics is

A)
$$n_i = \frac{g_i}{f e^{BE_i}}$$

B)
$$n_i = \frac{g_i}{fe^{BE}_i - 1}$$

C)
$$n_i = \frac{g_i}{e^{BE}_i}$$

$$D) n_i = \frac{g_i}{f e^{BE}_i +}$$

2005 – 2006:

- 75. Fermi-Dirac statistics is applied to systems of
 - a) identical and indistinguishable particles
 - B) identical and distinguishable particles
 - C) identical and indistinguishable particles obeying Pauli's exclusion Principle
 - D) identical and distinguishable Particles obeying Pauli's exclusion Principle
- 76. Grand canonical ensemble is one which allows
 - A) the subsystem to exchange energy
 - B) the subsystem to exchange number of particles
 - C) exchange of both
 - D) the subsystem to exchange neither energy nor number of particles.

2011 - 2012:

- 77. According to which statistics the energy at absolute zero cannot be zero?
 - A) Fermi-Dirac
- B) Maxwell-Boltzmann
- C) Bose-Einstein
- D) Both Maxwell-Boltzmann and Bose-Einstein



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78. Boson have spin value

- A) zero or one
- B) zero
- C) one
- D) $\frac{1}{2}$

The most probable velocity of the molecules in a gas is 79.

A)
$$\sqrt{\frac{3KT}{m}}$$

B)
$$\sqrt{\frac{8KT}{m}}$$

C)
$$\sqrt{\frac{6KT}{m}}$$

D)
$$\sqrt{\frac{2KT}{m}}$$

Which of the following is correct? 80.

A)
$$\overline{V} < V_{rms} < Vp$$

B)
$$V_{rms} < Vp < \overline{V}$$

C)
$$Vp < \overline{V} < rms$$

D)
$$V_{rms} < Vp < \overline{V}$$

Where \overline{V} - mean velocity

 V_{rms} - root mean square velocity

- most probable velocity of the molecules of a gas $V_{\rm p}$

Richardson - Dushman equation for thermionic emission is 81.

A)
$$J = T^4 e^{-\phi/KT}$$

B)
$$J = AT^2_e^{-\phi/KT}$$

C)
$$J = AT^3 e^{-\phi/KT}$$

D)
$$J = AT^4 - \phi/KT$$

Liouville's Theorem is 82.

A)
$$\left(\frac{\partial p}{\partial t}\right) + \sum_{j} \left(\frac{\partial p}{\partial q_{j}} \dot{q}_{j} + \frac{\partial p}{\partial p_{j}} \dot{p}\right) = 0$$

$$\mathbf{B} \cdot \left(\frac{\partial^2 p}{\partial t^2} \right) + \sum_{j} \left(\frac{\partial \mathbf{p}}{\partial \mathbf{q}_{j}} \mathbf{q}_{j} + \frac{\partial p}{\partial p_{j}} \mathbf{p}_{j} \right) = 0$$

C)
$$\left(\frac{\partial p}{\partial t}\right) + \sum_{j} \left(\frac{\partial p}{\partial q_{j}} \stackrel{\bullet}{p}_{j} + \frac{\partial p}{\partial p_{j}} \stackrel{\bullet}{p}_{j}\right) = 0$$

C)
$$\left(\frac{\partial p}{\partial t}\right) + \sum_{j} \left(\frac{\partial p}{\partial q_{j}} \dot{p}_{j} + \frac{\partial p}{\partial p_{j}} \dot{p}_{j}\right) = 0$$
 D) $\left(\frac{\partial^{2} p}{\partial t^{2}}\right) + \sum_{j} \left(\frac{\partial p}{\partial q_{j}} \dot{p}_{j} + \frac{\partial p}{\partial p_{j}} \dot{q}_{j}\right) = 0$

83. A micro-canonical ensemble represents

- A) an isolated system in equilibrium
- B) a system in contact with a heat reservoir
- C) a system that can exchange both energy and momentum
- D) a system that undergoes pressure change

2012 – 2013:

84. Stirling approximation gives $\log n! = \dots$

- A) nlogn
- B) nlog n-n!
- C) nlogn+n!
- D) n! –nlogn

The Probable distribution of the Fermi-Dirac gas is 85.

A)
$$n_i = \frac{gi}{e^{\alpha} + \beta \varepsilon_i}$$

B))
$$n_i = \frac{e^{\alpha} + \beta \varepsilon_i}{gi}$$

C)
$$n_i = \frac{gi}{e^{\alpha} + \beta \varepsilon_i - 1}$$

D))
$$n_i = \frac{gi}{e^{\alpha} + \beta \varepsilon_i + 1}$$

86. Total energy of perfect Bore-Einstein gas is



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A)
$$E = \frac{3}{2}nkL\left[1 - \frac{A}{2\frac{5}{2}} - \frac{A^2}{3\frac{5}{2}} - \dots \right]$$
 B) E

$$\frac{1}{2}nkL\left[1-\frac{A}{2\frac{5}{2}}-\frac{A^{2}}{3\frac{5}{2}}-\dots\right]$$

C) E =
$$\frac{3}{2}nkL\left[1+\frac{A}{2\frac{5}{2}}+\frac{A^2}{3\frac{5}{2}}+\dots\right]$$

$$\frac{1}{2}nkL\left[1 + \frac{A}{2\frac{5}{2}} + \frac{A^{2}}{3\frac{5}{2}} + \dots \right]$$

- 87. The independent systems having is called micro canonical ensembles
 - A) same energy E, Volume V and temperature
 - B) same temperature T, volume V and the number of particles N
 - C) same temperature T, volume V and the chemical potential u
 - D) same energy E, volume V and the number of particles N
- Maxwell Boltzmann's Statistics states that the average kinetic energy per 88. molecule associated with each degree of freedom is
 - A) KT
- B) $\frac{1}{2}$ KT
- C) $\frac{3}{2}$ KT
- D) KT
- According to Dulong-Petit's law, the high temperature limit of specific heat 89. capacity becomes
- A) $C_v = 3NK_B$ B) $C_{V\alpha T^3}$ C) $CV\alpha \frac{1}{T^3}$

 $C_{\rm V}$

$$\alpha \exp \left(-\frac{\hbar W}{K_{P}T}\right)$$

- The mean square speed of gas molecules in equilibrium is proportional to
- $B)T^2$
- C) T^3
- 91. Which of the following statement is wrong for Helium – II?
 - A) The viscosity is a almost zero
 - B) Thermal conductivity is very low
 - C) Density is same as Helium -1
 - D) Flow through capillaries is independent of pressure difference



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The average energy of Plank's Oscillator $\varepsilon = \dots$ 92.

A)
$$\bar{\varepsilon} = \frac{hv}{e \, hv/KT}$$

B)
$$\bar{\varepsilon} = \frac{e^{hv}/kT}{hv}$$

C)
$$\bar{\varepsilon} = \frac{hv}{e^{hv}/kT + 1}$$

D)
$$\bar{\varepsilon} = \frac{hv}{e^{\frac{hv}{KT}-1}}$$

2014 – 2015:

93. Consider a gas of only two particles A, B obeying B-E statistics and each particle be in one of the three possible quantum states 1, 2, 3. How many possible states exist for the whole gas?

A) 9

D) 2

The total energy of the system of 'n' electrons at T = 0 K, using Fermi-Dirac 94. law of distribution of energy is

A) zero

B) $\frac{3}{5}n\mu f$ C) 1

D) $\frac{3}{2}$

A particle of mass 'm' obeys Maxwellian velocity distribution. The average 95. speed of the particle is

A) $\frac{1}{2}KT$

B) $\sqrt{\frac{2KT}{m\pi}}$ C) $\frac{3KT}{m}$

D) $\sqrt{\frac{8KT}{m\pi}}$

96. In a grand canonical ensemble, the system are capable, of exchanging

A) Only energy

B) Only particles

C) Both energy and particles

D) None of the above

The co-efficient of viscosity of liquid helium II is 97.

A) Low

B) Abnormally low

C) High

D) Abnormally

high

The particles which obey Fermi-Dirac statistics are known as 98.

B) Photons

C) Fermions

D) Phonons

99. In thermionic emission, the thermionic current varies with the temperature of the filament as

A) T

B) T^2

C) T^{-1}

D) $\frac{1}{r^2}$

100. The energy emitted by a black body at a temperature of 600K is

A) $7350 \text{ watt/} m^2$

B) $0.0204 \ watt/m^2$

C) $3600 \text{ watt/}m^2$

D) $36000 \text{ watt/}m^2$

101. In a monoatomic gas, the molecular phase-space has dimension of

A) 2

B) 3

C) 4

D) 6



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102. According to Debye's T^3 law, the specific heat at constant volume C_V at high temperature is

A) Proportional to T^3

B) Proportional to T^2

C) Proportional to T

D) Independent of temperature

Answer Keys:

1	21		41		61		81	
2	22		42		62		82	
3	23		43		63		83	
4	24		44		64		84	
5	25		45		65	(85	
6	26		46		66		86	
7	27		47		67		87	
8	28		48		68		88	
9	29		49		69		89	
10	30		50		70	100	90	
11	31		51		71		91	
12	32		52		72		92	
13	33		53		73		93	
14	34		54		74		94	
15	35		55		75		95	
16	36		56		76		96	
17	37		57	4/01	77		97	
18	38		58		78		98	
19	39	^	59		79		99	
20	40		60		80		100	

101

102.

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