

Clas:10

Time: 1.30 hrs

Relations and functions

Marks:

50

I. Answer any five of the following. Q. No 06 is compulsory $5 \times 2 = 10$

1. $(-2, 3), (-2, 4), (0, 3), (0, 4), (3, 3), (3, 4)$ find A and B.
2. A Relation R is given by the set $\{ (x, y) / y = x + 3, x \in \{ 0, 1, 2, 3, 4, 5 \} \}$. Determine its domain and range.
3. Define Cartesian product and Range.
4. Represent the function $f(x) = \sqrt{2x^2 - 5x + 3}$ as a composition of two functions.
5. Find k if $f \circ f(k) = 5$, where $f(k) = 2k - 1$
6. The distance S (in kms) travelled by a particle in time 't' $S(t) = \frac{t^2 + t}{2}$. Find the distance travelled by the particle after
 - (1) Three and half hours
 - (2) Eight hours and fifteen minutes

II. Answer any seven of the following: Q.No14 is compulsory $7 \times 5 = 35$

7. Let A = The set of all natural numbers less than 8, B = The set of all prime numbers less than 8, and C = The set of all even prime numbers. Then verify that
 - (1) $(A \cup B) \times C = (A \times C) \cup (B \times C)$
 - (2) $A \times (B \cap C) = (A \times B) \cap (A \times C)$
8. A function f is defined by $f(x) = 2x - 3$
 - (i) find $\frac{f(0) + f(1)}{2}$
 - (ii) find x such that $f(x) = 0$
 - (iii) find x such that $f(x) = x$
 - (iv) find x such that $f(x) = f(1 - x)$

9. Show that $(f \circ g) \circ h = f \circ (g \circ h)$, $f(x) = x^2$, $g(x) = 2x$, $h(x) = x+4$.

10. If the function $f: \mathbb{R} \rightarrow \mathbb{R}$ is defined by

$$f(x) = \begin{cases} 2x+7, \\ x^2-2, \\ 3x-2, \end{cases}$$

(!) $f(4)$ (!!) $f(-2)$ (!!!) $f(4)+2f(1)$ (!V) $\frac{f(1)-3f(4)}{f(-3)}$

11. Let $A \rightarrow B$ be a function defined by $f(x) = \frac{x}{2} - 1$, where $A = \{2, 4, 6, 10, 12\}$

$B = \{0, 1, 2, 4, 5, 9\}$ represent f by

- (!) Set of ordered pairs (!!) table
 (!!!) an arrow diagram (!V) a graph

12. If $f(x) = 3x - 2$, $g(x) = 2x + k$, and if $f \circ g = g \circ f$, then find the value of k

13. (!) A function f is defined by $f(x) = 3 - 2x$, then find x such that

$$f(x^2) = (f(x))^2$$

(!!) A plane is flying at a speed of 500 km per hour. Express the distance d travelled by the plane as function of time t in hours.

14. Find x if $g \circ f(x) = f \circ g(x)$, given $f(x) = 3x+1$, and $g(x) = x+3$

Answer the following: $1 \times 5 = 5$

15. Draw a circle of diameter 6 cm from a point which is 8 cm away from its centre, Draw the two tangents and measure their lengths

Prepared by: R. VIGNESH, M Sc., B Ed.,

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