

ROYAL TUITION CENTER, ELAMPILLAI, CELL: 9080244280

CLASS : XII
SUBJECT : MATHS



MARKS : 70
TIME : 150 Min

I. ANSWER ANY 10 QUESTIONS

10x2 = 20

1. Find the inverse of the matrix $\begin{bmatrix} 2 & -1 & 3 \\ -5 & 3 & 1 \\ -3 & 2 & 3 \end{bmatrix}$.
2. If $A = \begin{bmatrix} 3 & 2 \\ 7 & 5 \end{bmatrix}$ and $B = \begin{bmatrix} -1 & -3 \\ 5 & 2 \end{bmatrix}$, verify that $(AB)^{-1} = B^{-1}A^{-1}$.
3. Reduce the matrix $\begin{bmatrix} 0 & 3 & 1 & 6 \\ -1 & 0 & 2 & 5 \\ 4 & 2 & 0 & 0 \end{bmatrix}$ to a row-echelon form.
4. Find the inverse of the non-singular matrix $A = \begin{bmatrix} 0 & 5 \\ -1 & 6 \end{bmatrix}$, by Gauss-Jordan method.
5. Solve the following system of linear equations by matrix inversion method:
 - (i) $2x + 5y = -2, x + 2y = -3$
6. Solve the following systems of linear equations by Gaussian elimination method:
 - (i) $2x - 2y + 3z = 2, x + 2y - z = 3, 3x - y + 2z = 1$
7. Simplify the following: $\sum_{n=1}^{10} i^{n+50}$
8. Simplify $\left(\frac{1+i}{1-i}\right)^3 - \left(\frac{1-i}{1+i}\right)^3$ into rectangular form
9. If $|z| = 2$ show that $3 \leq |z + 3 + 4i| \leq 7$
10. Find the square roots of (i) $4 + 3i$
11. Obtain the Cartesian form of the locus of $z = x + iy$ in each of the following cases:
 - (i) $[\operatorname{Re}(iz)]^2 = 3$
12. Represent the complex number (i) $-1 - i$

II. ANSWER ANY 10 QUESTIONS. 20 AND 21 IT'S A COMPULSORY QUESTIONS 10x5 =50

13. Find all cube roots of $\sqrt{3} + i$.

14. Find the rectangular form of the complex numbers

5

$$(i) \left(\cos \frac{\pi}{6} + i \sin \frac{\pi}{6} \right) \left(\cos \frac{\pi}{12} + i \sin \frac{\pi}{12} \right) \quad (ii) \frac{\cos \frac{\pi}{6} - i \sin \frac{\pi}{6}}{2 \left(\cos \frac{\pi}{3} + i \sin \frac{\pi}{3} \right)}$$

15. Show that the equation $z^3 + 2\bar{z} = 0$ has five solutions.

16. If $z = x + iy$ and $\arg \left(\frac{z-1}{z+1} \right) = \frac{\pi}{2}$, show that $x^2 + y^2 = 1$.

17. If $z_1 = 3 + 4i$, $z_2 = 5 - 12i$, and $z_3 = 6 + 8i$, find $|z_1|$, $|z_2|$, $|z_3|$, $|z_1 + z_2|$, $|z_2 - z_3|$, and $|z_1 + z_3|$.

18. Investigate for what values of λ and μ the system of linear equations

$$x + 2y + z = 7, \quad x + y + \lambda z = \mu, \quad x + 3y - 5z = 5$$

has (i) no solution (ii) a unique solution (iii) an infinite number of solutions.

19. An amount of ₹ 65,000 is invested in three bonds at the rates of 6%, 8% and 10% per annum respectively. The total annual income is ₹ 4,800. The income from the third bond is ₹ 600 more than that from the second bond. Determine the price of each bond. (Use Gaussian elimination method.)

20. A chemist has one solution which is 50% acid and another solution which is 25% acid. How much each should be mixed to make 10 litres of a 40% acid solution? (Use Cramer's rule to solve the problem).

21. Four men and 4 women can finish a piece of work jointly in 3 days while 2 men and 5 women can finish the same work jointly in 4 days. Find the time taken by one man alone and that of one woman alone to finish the same work by using matrix inversion method.

22. Show that the matrix $\begin{bmatrix} 3 & 1 & 4 \\ 2 & 0 & -1 \\ 5 & 2 & 1 \end{bmatrix}$ is non-singular and reduce it to the identity matrix by elementary row transformations.

23. If $A = \frac{1}{7} \begin{bmatrix} 6 & -3 & a \\ b & -2 & 6 \\ 2 & c & 3 \end{bmatrix}$ is orthogonal, find a, b and c , and hence A^{-1} .

24. By using Gaussian elimination method, balance the chemical reaction equation:
 $C_2H_6 + O_2 \rightarrow H_2O + CO_2$