

## X - MATHS (reduced syllabus) 2021-2022

### Self Evaluation

Success = Sum of all efforts  
 Don't stop until you are success.  
 Use the mind not the mouth  
 - A.Balaiah  
 Tirunelveli(9750493961)

### 1.Relations and Functions:

PROPERTY	CARTESIAN PRODUCT
Commutative	$A \times B \neq B \times A$
Associative	$AX(BXC)=(AXB)XC$
Distributive	$\begin{array}{c} \cup \quad \cup \\ AX(B \cap C)=(AXB) \cap (AXC) \\ - \quad - \end{array}$

### 2.Sequences and Series

Euclids lemma :  $a=bq+r$  condition for  $r : 0 \leq r < |b|$  Odd integer :  $2k-1$

Even integer:  $2k+1$  divides (the) : then Find HCF divisible by : then Find LCM

	A.P
GENERAL FORM	$a, a+d, a+2d, a+3d, \dots$
GENERAL TERM	$t_n = a + (n-1)d$
THREE CONSECUTIVE TERMS/FOUR	$a-d, a, a+d$ / $a-3d, a-d, a+d, a+3d$
NUMBER OF TERMS	$n = \frac{l-a}{d} + 1$
5 terms Temperature sum	$a-d, a, a+d, a+2d, a+3d$

### 3.ALGEBRA

Three digit number :  $100x+10y+z$  Area of the rectangular path =outer area -inner area

Bus/Train sum:  $T_1 - T_2 = \frac{1}{2}$  hr /  $T_1 - T_2 = 1$  hr Flower bed sum :  $3(10-2x)^2 + 4(100-(10-2x)^2) = 364$

The pole sum :  $x^2 + y^2 = 20^2$

$(a+b)^2 = (a+b)(a+b)$	$\alpha - \beta = \sqrt{(\alpha + \beta)^2 - 4\alpha\beta}$
$(a-b)^2 = (a-b)(a-b)$	$\alpha^2 + \beta^2 = (\alpha + \beta)^2 - 2\alpha\beta$
$a^2 - b^2 = (a+b)(a-b)$	$\alpha^4 + \beta^4 = \alpha^2^2 + \beta^2^2$
$(a+b+c)^2 =$	$\alpha^3 + \beta^3 = (\alpha + \beta)^3 - 3\alpha\beta(\alpha + \beta)$
$a^3 + b^3 = (a+b)(a^2 - ab + b^2)$	$\beta - \alpha = -(\alpha - \beta)$
$a^3 - b^3 = (a-b)(a^2 + ab + b^2)$	$\alpha^3 - \beta^3 = (\alpha - \beta)^3 + 3\alpha\beta(\alpha - \beta)$
$a^4 + a^2 + 1 = (a^2 + a + 1)(a^2 - a + 1)$	$X^4 + 4x^2 + 16 = (x^2 + 2x + 4)(x^2 - 2x + 4)$

sum of zeros (  $\alpha + \beta$  ) =  $-\frac{b}{a}$

product of zeros (  $\alpha \beta$  ) =  $\frac{c}{a}$

Formula for solving quadratic equation  $= \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

Formation of quadratic polynomials :  $p(x) = x^2 - (\text{sum of zeros})x + \text{product of zeros}$

Formation of quadratic equation :  $x^2 - (\text{sum of roots})x + \text{product of roots}$

For finding Nature of roots  $\Delta = b^2 - 4ac$

If  $\Delta > 0$  , roots are real and unequal

If  $\Delta = 0$  , roots are real and equal

If  $\Delta < 0$  , No real roots

#### 4. Geometry

Write the statement , To prove and Draw the diagram

- Thales Theorem

**Statement :** A straight line drawn parallel to a side of triangle intersecting the other two sides, divides the sides in the same ratio.

**To prove :**  $\frac{AD}{DB} = \frac{AE}{EC}$

- Angle Bisector Theorem

**Statement :** The internal bisector of an angle of a triangle divides the opposite side internally in the ratio of the corresponding sides containing the angle.

**To prove :**  $\frac{AB}{AC} = \frac{BD}{DC}$

- Pythagoras Theorem

**Statement :** In a right angle triangle, the square on the hypotenuse is equal to the sum of the squares on the other two sides.

**To prove :**  $BC^2 = AB^2 + AC^2$

Height of the point of intersection of two pole  $= \frac{ab}{a+b}$

#### 5. Co-ordinate Geometry

The midpoint of the line segment :  $(\frac{x_1+x_2}{2}, \frac{y_1+y_2}{2})$

When want to draw graph : To find Area

Area of a triangle :  $\frac{1}{2} \begin{vmatrix} x_1 & x_2 & x_3 & x_1 \\ y_1 & y_2 & y_3 & y_1 \end{vmatrix}$  sq. units

Area of the quadrilateral :  $\frac{1}{2} \begin{vmatrix} x_1 & x_2 & x_3 & x_4 & x_1 \\ y_1 & y_2 & y_3 & y_4 & y_1 \end{vmatrix}$  sq. units

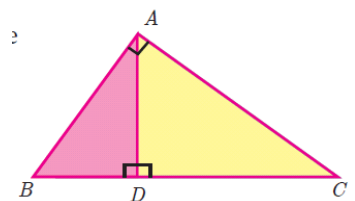
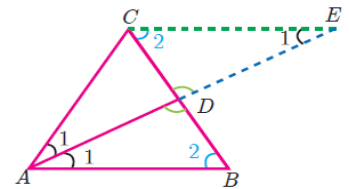
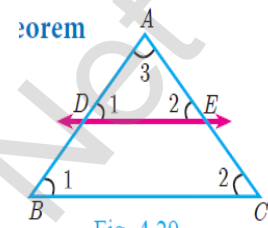
Slope i.  $m = \frac{y_2 - y_1}{x_2 - x_1}$  ii.  $m = \frac{-\text{coeff of } x}{\text{coeff of } y}$  iii.  $m = \tan \theta$

y-intercept  $c : \frac{-\text{constant term}}{\text{coeff of } y}$

To prove : Parallelogram ( $AB \parallel CD$   $BC \parallel AD$ ) , Trapezium ( $AB \parallel CD$   $BC \nparallel AD$ ) ,

Right angle triangle ( $m_1 \times m_2 = -1$ ) ,

Midpoints are parallelogram (four mid point , then ( $AB \parallel CD$   $BC \parallel AD$ ) )



**Equation :****Equation of straight line in various forms**

Form	Name	Form	Name
$ax + by + c = 0$	General form	$\frac{x}{a} + \frac{y}{b} = 1$	Intercept form
$y - y_1 = m(x - x_1)$	Point-slope form	$x = c$	Parallel to Y axis
$y = mx + c$	Slope-intercept	$y = b$	Parallel to X axis
$\frac{y - y_1}{y_2 - y_1} = \frac{x - x_1}{x_2 - x_1}$	Two point form		

**Steps for find the Equation :**

**Altitude :**  $m_1, m_2$ , equation **Median :** mid point ,equation **Perpendicular:**  $m_1, m_2$  , equation

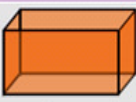

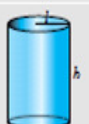

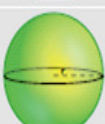
**Sum of intercepts 7 :**  $a=a, b=7-a$  **Equal Intercepts :**  $a=k, b=k$  **Ratio 3:5 :**  $a=3k, b=5k$




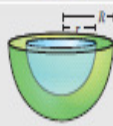
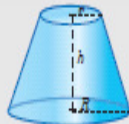
**Equal and opposite sign :**  $a=k, b=-k$

**TRIGONOMETRY:**

$\theta$	$0^\circ$	$30^\circ$	$45^\circ$	$60^\circ$	$90^\circ$
sin	0	$\frac{1}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{\sqrt{3}}{2}$	1
cos	1	$\frac{\sqrt{3}}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{1}{2}$	0
tan	0	$\frac{1}{\sqrt{3}}$	1	$\sqrt{3}$	$\infty$

**7.MENSURATION**

Points to Remember				
Solid	Figure	Curved surface Area / Lateral surface Area (in sq. units)	Total surface Area (in sq. units)	Volume (in cubic units)
Cuboid		$2h(l + b)$	$2(lb + bh + lh)$	$l \times b \times h$
Cube		$4a^2$	$6a^2$	$a^3$
Right Circular Cylinder		$2\pi rh$	$2\pi r(h + r)$	$\pi r^2 h$
Right Circular Cone		$\pi rl$ $l = \sqrt{r^2 + h^2}$ $l = \text{slant height}$	$\pi rl + \pi r^2$ $= \pi r(l + r)$	$\frac{1}{3} \pi r^2 h$
Sphere		$4\pi r^2$	$4\pi r^2$	$\frac{4}{3} \pi r^3$

hemisphere		$2\pi r^2$	$3\pi r^2$	$\frac{2}{3} \pi r^3$
hollow cylinder		$2\pi(R + r)h$	$2\pi(R + r)(R - r + h)$	$\pi(R^2 - r^2)h$
hollow sphere		$4\pi R^2 = \text{outer surface area}$	$4\pi(R^2 + r^2)$	$\frac{4}{3} \pi(R^3 - r^3)$
hollow hemisphere		$2\pi(R^2 + r^2)$	$\pi(3R^2 + r^2)$	$\frac{2}{3} \pi(R^3 - r^3)$
frustum of right circular cone.		$\pi(R + r)l$ where $l = \sqrt{h^2 + (R - r)^2}$	$\pi(R + r)l + \pi R^2 + \pi r^2$	$\frac{1}{3} \pi h [R^2 + r^2 + Rr]$

SHAPE	C.S.A	T.S.A(SA)	VOLUME(Capacity)
Jewel Box	—	$2(l + b)h_1 + lb + \frac{1}{2}(2\pi rh_2)$ sq.units	$lbh_1 + \frac{1}{2}(\pi r^2 h_2)$ cu. units
Hemisphere on Cube	-- -----	$5a^2 + 2\pi r^2 + a^2 - \pi r^2$ $= 6a^2 + \pi r^2$	-----
1litre = $\frac{1}{1000}m^3$	1litre = 1000 cm <sup>3</sup>	1m = 100 cm	1km = 1000 m
1cm = 10 mm	14.64 m/s = 14.64 x $\frac{3600}{1000}$ km/hr		

$$\text{Base area} = \pi r^2$$

$$\text{Base circumference} = 2\pi r$$

$$\text{Cone} \quad l = \sqrt{h^2 + r^2} \quad h = \sqrt{l^2 - r^2} \quad r = \sqrt{l^2 - h^2}$$

$$\text{Frustum} \quad l = \sqrt{h^2 + (R - r)^2}$$

### 8.STATISTICS AND PROBABILITY

$$p(\bar{A} \cap B) = p(B) - p(A \cap B) \quad p(A \cap \bar{B}) = p(A) - p(A \cap B)$$

$$P(A) + P(\bar{A}) = 1 \quad P(\bar{A}) = 1 - p(A)$$

1.Tossing an unbiased coin twice  $S = \{HH, HT, TH, TT\}$

2.Tossing an unbiased coin thrice

$$S = \{HHH, HHT, HTH, HTT, THH, THT, TTH, TTT\}$$

3.Sum as a prime number on tossing 2 dice:

$$\left\{ \begin{array}{l} (1, 1), (1, 2), (1, 4), (1, 6), (2, 1), (2, 3), (2, 5), \\ (3, 2), (3, 4), (4, 1), (4, 3), \\ (5, 2), (5, 6), (6, 1), (6, 5) \end{array} \right\}$$

4.Tossing 3 coin i) atleast 2 tail =  $\{HTT, THT, TTH, TTT\}$

ii) 2 consecutive tail =  $\{HTT, TTH, TTT\}$

iii) atmost 2 head =  $\{HHT, HTH, HTT, THH, THT, TTH, TTT\}$

iv) In 1 to 1000 Perfect Square greater than 500 =  $\{23^2, \dots, 31^2\}$

- No of cards 52-
- Black card -26
- Red card -26
- Red king -2
- Black Queen -2
- Red diamond -13
- Red spade -0
- Face cards -12
- Number cards - 36

\_\_\_\_\_ ALL THE BEST