

Sample Question Paper
CLASS: XII
Session: 2022-23
Applied Mathematics (Code-241)
Marking Scheme

Section – A

Each question carries 1-mark weightage

1.	$x \equiv 27 \pmod{4}$ $\Rightarrow x - 27 = 4k$, for some integer k $\Rightarrow x = 31$ as $27 < x \leq 36$ (C) option
2.	(D) option
3.	$n = 26 \Rightarrow t = 3.07 > t_{25}(0.05) = 2.06$ (B) option
4.	$n = 34 \Rightarrow v = 34 - 1 = 33$ (B) option
5.	Speed of boat downstream = $u = 10$ km/h And, speed of boat upstream = $v = 6$ km/h \Rightarrow Speed of stream = $\frac{1}{2}(u - v) = 2$ km/h (B) option
6.	(C) option
7.	Truck A carries water = $100 - \left(\frac{20 \times 1500}{1000}\right) = 70$ l Truck B carries water = $80 - \left(\frac{20 \times 1000}{1000}\right) = 60$ l (C) option
8.	Let the face value of the bond = x Then, $\frac{10}{200}x = 1800 \Rightarrow x = 36000$ (D) option
9.	(C) option
10.	(D) option
11.	$D = \frac{C - S}{n} = \frac{480000 - 25000}{10} = 45500$ (B) option
12.	(A) option
13.	$\int \frac{dy}{y \log y} = \int \frac{dx}{x}$ $\Rightarrow \log(\log y) = \log x + \log C $ $\Rightarrow \log(\log y) = \log Cx $ $\Rightarrow y = e^{ Cx }$

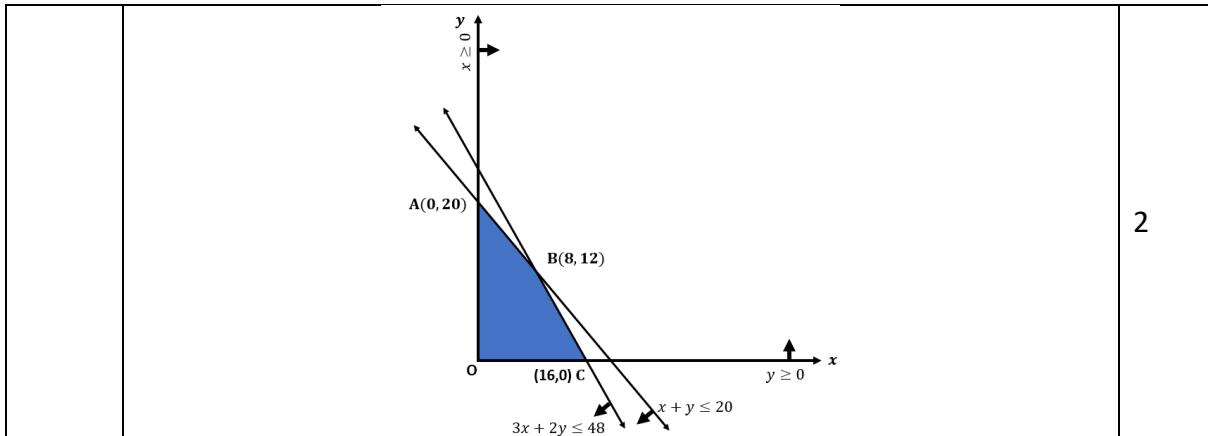
	(B) option	
14.	$\left[\left(\frac{60000}{10000} \right)^{\frac{1}{4}} - 1 \right] \times 100 = [\sqrt[4]{6} - 1] \times 100$	
15.	<p style="text-align: center;"> Cheaper 0 Dearer 480 ↙ ↘ Mean 300 ↘ ↙ 180 300 </p> <p>⇒ 180 : 300 = 3 : 5</p>	
16.	(D) option	
17.	(C) option	
18.	(B) option	
19.	<p>P(Win in one game) = P(Lose in one game) = $\frac{1}{2}$</p> <p>⇒ P (Beena to win in 3 out of 4 games) = ${}^4C_3 \cdot \left(\frac{1}{2}\right)^4 = \frac{1}{4} = 25\%$</p> <p>Assertion is correct and Reason is the correct explanation for it</p>	
20.	<p>Effective rate of interest = Nominal rate – inflation rate = 12.5 – 2 = 10.5%</p> <p>Assertion is correct</p> <p>Reason is true but not supportive of assertion</p>	
Section – B		
Each question carries 2-mark weightage		
21.	<p>P = 250000, R = 7500, $i = r/400$</p> <p>⇒ $250000 = \frac{7500 \times 400}{r} \Rightarrow r = 12$</p>	1
	⇒ $r = 12$	1
22.	<p>$a - 8 = 1 \Rightarrow a = 9$</p> <p>$3b = -2 \Rightarrow b = -\frac{2}{3}$</p> <p>$-c + 2 = -28 \Rightarrow c = 30$</p>	1
	⇒ $2a + 3b - c = -14$	1
	OR	
	Expanding C_1 , we get $\Delta = 1(2x^2 + 4) - 2(-4x - 20) = 86$	1
	$\Rightarrow x^2 + 4x - 21 = 0$ $\therefore x = 3, -7$	1
23.	<p>Let the number of hardcopy and paperback copies be x and y respectively</p> <p>⇒ Maximum profit $Z = (72x + 40y) - (9600 + 56x + 28y) = 16x + 12y - 9600$</p>	1

	Subject to constraints: $x + y \leq 960$ $5x + y \leq 2400$ $x, y \geq 0$	1
24.	Speed of boat in still waters = x km/h Speed of stream = y km/h Distance travelled = d km Time taken to travel downstream = $\frac{d}{x+y}$ Time taken to travel upstream = $\frac{d}{x-y}$	1
	Then, $\frac{2d}{x+y} = \frac{d}{x-y} \Rightarrow x : y = 3 : 1$	1
	OR	1
	Param runs 5 m in 3 seconds \Rightarrow time taken to run 200 m = $\frac{3}{5} \times 200 = 120$ seconds	
	Anuj 's time = $120 - 3 = 117$ seconds	1
25.	$V_f = 437500, V_i = 350000$ Nominal rate = $\frac{V_f - V_i}{V_i} \times 100$	1
	$= \frac{437500 - 350000}{350000} \times 100 = 25\%$	1
Section – C		
Each question carries 3-mark weightage		
26.	$f'(x) = x^3 - 6x^2 + 11x - 6 = (x - 1)(x - 2)(x - 3)$ $\Rightarrow x = 1, 2, 3$	1
	Strictly increasing in $(1, 2) \cup (3, \infty)$	1
	Strictly decreasing in $(-\infty, 1) \cup (2, 3)$	1
27.	Daily diet of team A = $[2 \ 3 \ 1] \begin{bmatrix} 2500 & 65 \\ 1900 & 50 \\ 2000 & 54 \end{bmatrix} = \begin{bmatrix} 12700 \\ 334 \end{bmatrix}$ Team A consumes 12700 calories and 334 g vitamin	1.5
	Daily diet of team B = $[1 \ 2 \ 2] \begin{bmatrix} 2500 & 65 \\ 1900 & 50 \\ 2000 & 54 \end{bmatrix} = \begin{bmatrix} 10300 \\ 273 \end{bmatrix}$ Team B consumes 10300 calories and 273 g vitamin	1.5
28.	$\int \frac{dx}{(1 + e^x)(1 + e^{-x})}$ $= \int \frac{e^x dx}{(1 + e^x)^2}$	3

	$= \int \frac{dt}{t^2}, \text{ where } t = e^x + 1 \text{ and } dt = e^x dx$ $= \frac{-1}{t} + C$ $= \frac{-1}{1+e^x} + C$ <p style="text-align: center;">OR</p> $\int \frac{x \log(1+x^2) dx}{I}, \text{ Integration by parts}$ $= \log(1+x^2) \cdot \int x dx - \int \left[\frac{d}{dx} \log(1+x^2) \cdot \int x dx \right] dx$ $= \frac{x^2}{2} \log(1+x^2) - \int \left[\frac{2x}{1+x^2} \cdot \frac{x^2}{2} \right] dx$ $= \frac{x^2}{2} \log(1+x^2) - \int \frac{x^3}{1+x^2} dx$ $= \frac{x^2}{2} \log(1+x^2) - \int \left[x - \frac{x}{1+x^2} \right] dx$ $= \frac{x^2}{2} \log(1+x^2) - \frac{x^2}{2} + \frac{1}{2} \log(1+x^2) + C$ $= \frac{1}{2} [(1+x^2) \log(1+x^2) - x^2] + C$	
29.	<p>Under pure competition, $p_d = p_s$</p> $\Rightarrow \frac{8}{x+1} - 2 = \frac{x+3}{2}$ $\Rightarrow x^2 + 8x - 9 = 0$ $\Rightarrow x = -9, 1$ $\therefore x = 1$	1.5
	<p>When $x_0 = 1 \Rightarrow p_0 = 2$</p> $\therefore \text{Produce surplus} = 2 - \int_0^1 \frac{x+3}{2} dx = 2 - \left[\frac{x^2}{4} + \frac{3x}{2} \right]_0^1 = \frac{1}{4}$	1.5
	<p style="text-align: center;">OR</p> $p = 274 - x^2$ $\Rightarrow R = px = 274x - x^3$ $\frac{dR}{dx} = 274 - 3x^2$ <p>Given $MR = 4 + 3x$</p> <p>In profit monopolist market,</p> $MR = \frac{dR}{dx} \Rightarrow 4 + 3x = 274 - 3x^2$ $\Rightarrow x^2 + x - 90 = 0$	1.5

	$\Rightarrow x = -10,9$ $\therefore x = 9$	
	When $x_0 = 9 \Rightarrow p_0 = 193$ \therefore Consumer surplus $= \int_0^9 (274 - x^2) dx - 193 \times 9$ $= \left[274x - \frac{x^3}{3} \right]_0^9$ $= 486$	1.5
30.	Purchase = ₹ 40,00,000 Down payment = x Balance = $40,00,000 - x$ $i = \frac{9}{1200} = 0.0075, n = 25 \times 12 = 300$ E = ₹ 30,000	1
	$\Rightarrow 30000 = \frac{(4000000 - x) \times 0.0075}{1 - (1.0075)^{-300}}$ $\Rightarrow 30000 = \frac{(4000000 - x) \times 0.0075}{1 - 0.1062}$ $\Rightarrow x = 424800$ Down payment = ₹ 4,24,800	2
31.	$n = 10 \times 2 = 20, S = 10,21,760, i = \frac{5}{200} = 0.025, R = ?$ $S = R \left[\frac{(1+i)^n - 1}{i} \right]$	1.5
	$\Rightarrow 1021760 = R \left[\frac{(1+0.025)^{20} - 1}{0.025} \right]$ $\Rightarrow 1021760 = R \left[\frac{1.6386 - 1}{0.025} \right]$ $\Rightarrow R = \left[\frac{1021760 \times 0.025}{0.6386} \right]$ $\Rightarrow R = ₹ 40,000$ Mr Mehra set aside an amount of ₹ 40,000 at the end of every six months	1.5
Section – D		
Each question carries 5-mark weightage		
32.	Probability of defective bucket = 0.03 $n = 100$ $m = np = 100 \times 0.03 = 3$ Let $X =$ number of defective buckets in a sample of 100 $P(X = r) = \frac{m^r e^{-m}}{r!}, r = 0, 1, 2, 3, \dots$	1
	(i) $P(\text{no defective bucket}) = P(r = 0) = \frac{3^0 e^{-3}}{0!} = 0.049$	2
	(ii) $P(\text{at most one defective bucket}) = P(r = 0, 1)$ $= \frac{3^0 e^{-3}}{0!} + \frac{3^1 e^{-3}}{1!}$	2

	$= 0.049 + 0.147$ $= 0.196$	
	OR	
	<p>$X =$ scores of students, $\mu = 45, \sigma = 5$</p> $\therefore Z = \frac{X - \mu}{\sigma} = \frac{X - 45}{5}$	1
	<p>(i) When $X = 45, Z = 0$ $P(X > 45) = P(Z > 0) = 0.5$ \Rightarrow 50% students scored more than the mean score</p>	2
	<p>(ii) When $X = 30, Z = -3$ and when $X = 50, Z = 1$ $P(30 < X < 50) = P(-3 < Z < 1) = P(-3 < Z \leq 1)$ $= P(-3 < Z \leq 0) + P(0 \leq Z < 1)$ $= P(0 \leq Z < 3) + P(0 \leq Z < 1)$ $= 0.4987 + 0.3413 = 0.84$ \Rightarrow 84% students scored between 30 and 50 marks</p>	2
33.	<p>Let x be the number of guests for the booking Clearly, $x > 100$ to avail discount \therefore Profit, $P = [4800 - \frac{200}{10}(x - 100)]x = 6800x - 20x^2$</p>	2
	$\Rightarrow \frac{dP}{dx} = 6800 - 40x \Rightarrow x = 170$	1
	As $\frac{d^2P}{dx^2} = -40 < 0, \forall x$	1
	<p>A booking for 170 guests will maximise the profit of the company And, Profit = ₹ 5,78,000</p>	1
	OR	
	$P(x) = R(x) - C(x)$ $= 5x - (100 + 0.025x^2)$	2
	$\Rightarrow P'(x) = 5 - 0.05x \Rightarrow x = 100$	1
	As $P''(x) = -0.05 < 0, \forall x$	1
	<p>\therefore Manufacturing 100 dolls will maximise the profit of the company And, Profit = ₹ 1,50,000</p>	1
34.	<p>Let the number of tables and chairs be x and y respectively (Max profit) $Z = 22x + 18y$ Subject to constraints: $x + y \leq 20$ $3x + 2y \leq 48$ $x, y \geq 0$</p>	1.5



2

The feasible region OABCA is closed (bounded)

Corner points	$Z = 22x + 18y$
O (0,0)	0
A (0,20)	360
B (8,12)	392
C (16,0)	352

1.5

Buying 8 tables and 12 chairs will maximise the profit

35.

$$A = \begin{bmatrix} 1 & 2 & 3 \\ 3 & 2 & 2 \\ 2 & 3 & 2 \end{bmatrix}$$

$\Rightarrow |A| = 9 \Rightarrow A^{-1}$ exists

$$\text{And } A^{-1} = \frac{1}{9} \begin{bmatrix} -2 & 5 & -2 \\ -2 & -4 & 7 \\ 5 & 1 & -4 \end{bmatrix}$$

2

$$AX = B \Rightarrow X = A^{-1}B$$

$$\Rightarrow X = \frac{1}{9} \begin{bmatrix} -2 & 5 & -2 \\ -2 & -4 & 7 \\ 5 & 1 & -4 \end{bmatrix} \begin{bmatrix} 85 \\ 105 \\ 110 \end{bmatrix} = \begin{bmatrix} 15 \\ 20 \\ 10 \end{bmatrix}$$

$\Rightarrow p_1 = 15, p_2 = 20, p_3 = 10$

3

Section – E

Each Case study carries 4-mark weightage

36.	CASE STUDY - I	
a)	Pipe C empties 1 tank in 20 h $\Rightarrow \frac{2}{5}$ th tank in $\frac{2}{5} \times 20 = 8$ hours	1
b)	Part of tank filled in 1 hour = $\frac{1}{15} + \frac{1}{12} - \frac{1}{20} = \frac{1}{10}$ th \Rightarrow time taken to fill tank completely = 10 hours	1
c)	At 5 am,	2

Let the tank be completely filled in 't' hours
 ⇒ pipe A is opened for 't' hours
 pipe B is opened for 't-3' hours
 And, pipe C is opened for 't-4' hours

⇒ In one hour,
 part of tank filled by pipe A = $\frac{t}{15}$ th
 part of tank filled by pipe B = $\frac{t-3}{15}$ th
 and, part of tank emptied by pipe C = $\frac{t-4}{15}$ th

Therefore $\frac{t}{15} + \frac{t-3}{12} - \frac{t-4}{20} = 1$
 ⇒ $t = 10.5$
 Total time to fill the tank = 10 hours 30 minutes

OR
 6 am, pipe C is opened to empty ½ filled tank
 Time to empty = 10 hours
 Time for cleaning = 1 hour
 Part of tank filled by pipes A and B in 1 hour = $\frac{1}{15} + \frac{1}{12} = \frac{3}{20}$ th tank
 ⇒ time taken to fill the tank completely = $\frac{20}{3}$ hours
 Total time taken in the process = $10 + 1 + \frac{20}{3} = 17$ hour 40 minutes

37. CASE STUDY - II

a)

Year	Y	X	X ²	XY
2015	35	-2	4	-70
2016	42	-1	1	-42
2017	46	0	0	0
2018	41	1	1	41
2019	48	2	4	96
	212		10	25

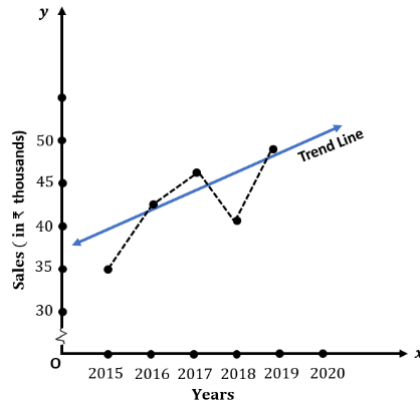
$a = \frac{\sum Y}{n} = \frac{212}{5} = 42.4$ and $b = \frac{\sum XY}{\sum X^2} = \frac{25}{10} = 2.5$

$Y_c = 42.4 + 2.5X$

OR

Year	Y	3-year moving average
2015	35	-
2016	42	41
2017	46	43
2018	41	45
2019	48	-

2



b) For year 2022,

$$Y_{2022} = 42.4 + 2.5(2022 - 2017) = 54.9$$
 \Rightarrow the estimated sales for year 2022 = ₹ 54,900

c)

$$Y_C = 42.4 + 2.5X$$

$$\Rightarrow 67.4 = 42.4 + 2.5X$$

$$\Rightarrow X = 10$$
 Sales will be ₹ 67,400 in year (2017+ 10) = year 2027

38. CASE STUDY - III

a)

$$\frac{k}{6} + \frac{2k}{6} + \frac{3(1-k)}{6} + \frac{4k}{2} = 1 \Rightarrow k = \frac{1}{4}$$

b) P (getting admission on applying at least 2 weeks ahead of application deadline)
 $= P(X = 2,3,4)$
 $= \frac{1}{12} + \frac{3}{8} + \frac{1}{2} = \frac{23}{24}$
 [alternate method: $1 - P(X = 1) = 1 - \frac{1}{24} = \frac{23}{24}$]

c) X = week applied ahead of application deadline

X	1	2	3	4
P(X)	$\frac{1}{24}$	$\frac{1}{12}$	$\frac{3}{8}$	$\frac{1}{2}$
XP(X)	$\frac{1}{24}$	$\frac{1}{6}$	$\frac{9}{8}$	2

$\therefore E(X) = \frac{80}{24} = 3\frac{1}{3}$ weeks

OR

X = Scholarship money awarded for the week applied in, before the deadline

Week applied in	1	2	3	4
X	9600	12000	20000	50000

P(X)	$\frac{1}{24}$	$\frac{1}{12}$	$\frac{3}{8}$	$\frac{1}{2}$
XP(X)	$\frac{9600}{24}$	$\frac{12000}{12}$	$\frac{60000}{8}$	$\frac{50000}{2}$
$\therefore E(X) = ₹ 33,900$				
