

## MATHEMATICS - XII STANDARD

## CHAPTER - 3 [IMPORTANT QUESTIONS]

If Need answer means cost Rs.25/-

- 1) If  $\alpha$  and  $\beta$  are the roots of quadratic equation  $17x^2 + 43x - 73 = 0$ , construct a quadratic equation whose roots are  $\alpha + 2$  and  $\beta + 2$ .
- 2) If  $\alpha$  and  $\beta$  are the roots of quadratic equation  $2x^2 - 17x + 18 = 0$ , construct a quadratic equation whose roots are  $\alpha^2$  and  $\beta^2$ .
- 3) If  $\alpha, \beta$  and  $\gamma$  are the roots of the equation  $x^3 + px^2 + qx + r = 0$ , find the value of  $\sum \frac{1}{\beta\gamma}$  in terms of the coefficient.
- 4) Find the sum of the squares of roots of  $ax^4 + bx^3 + cx^2 + dx + e = 0$ .
- 5) If  $P$  is real, discuss the nature of roots of the equation  $4x^2 + 4Px + P + 2 = 0$  in terms of  $P$ .
- 6) Find the sum of the squares of roots of eqn  $2x^4 - 8x^3 + 6x^2 - 3 = 0$ .
- 7) Solve the equation  $x^3 - 9x^2 + 14x + 24 = 0$  if it is given that two of its roots are in the ratio 3:2.
- 8) If  $\alpha, \beta$  and  $\gamma$  are the roots of the polynomial equation  $ax^3 + bx^2 + cx + d = 0$ . Find the value of  $\sum \frac{\alpha}{\beta\gamma}$  in terms of coefficients.
- 9) If  $p$  and  $q$  are the roots of equation  $lx^2 + nx + n = 0$ , show that  $\sqrt{p/q} + \sqrt{q/p} + \sqrt{n/l} = 0$ .
- 10) If the equations  $x^2 + px + q = 0$  and  $x^2 + p'x + q' = 0$  have a common root, show that it must be equal to  $\frac{pq' - p'q}{q - q'}$  or  $\frac{q - q'}{p' - p}$ .
- 11) Form a polynomial equation with integer coefficient with  $\sqrt{2}/\sqrt{3}$  as a root.
- 12) Show that if  $p, q, r$  are rational, the roots of the equation  $x^2 - 2px + p^2 - q^2 + 2qr - r^2 = 0$  are rational.
- 13) Find a polynomial equation of minimum degree with rational coefficients, having  $2 + \sqrt{3}i$  are a root.
- 14) Solve the equation  $x^4 - 9x^2 + 20 = 0$ .
- 15) Obtain the condition that roots of  $x^3 + px^2 + qx + r = 0$  are in A.P.
- 16) If the roots of  $x^3 + px^2 + qx + r = 0$  are in H.P. prove that  $9Pqr = 27r^2 + 2q^3$  Assume  $p, q, r \neq 0$ .
- 17) Determine  $k$  and solve the equation  $2x^3 - 6x^2 + 3x + k = 0$  if one of its roots is twice the sum of the other two roots.
- 18) Find solution, if any, of the equation  $2\cos^2 x - 9\cos x + 4 = 0$ .
- 19) Find all real numbers satisfying  $4^x - 3(2^{x+2}) + 2^5 = 0$ .
- 20) Solve:  $8x^{3/2n} - 8x^{-3/2n} = 63$
- 21) Solve:  $2\sqrt{\frac{x}{a}} + 3\sqrt{\frac{a}{x}} = b/a + 6a/b$

- 22) Solve the equation  $6x^4 - 5x^3 - 38x^2 - 5x + 6 = 0$  if it is known that  $\frac{1}{2}$  is a solution.
- 23) Find the exact number of real zeros and imaginary of the polynomial.

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