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- 1) Let us assume that the shape of a soap bubble is sphere. Use linear approximation the increase in the surface area of a soap bubble as its radius increases from 5 cm to 5.2 cm. Also calculate the percentage error.
- 2) Find the linear approximation for $f(x) = \sqrt{1+x}$, $x \geq -1$, at $x_0 = 3$. Use the linear approximation to estimate $f(3.2)$.
- 3) The time T , taken for a complete oscillation of a single pendulum with length l is given by the equation $T = 2\pi\sqrt{l/g}$, where g is a constant. Find the approximate percentage error in the calculated value of T corresponding to an error of 2 percent in the value of l .
- 4) Show that the percentage error in the n^{th} root of a number is approximately $1/n$ times percentage error in number.
- 5) Let $f, g: (a, b) \rightarrow \mathbb{R}$ be differentiable functions. Show that $d(fg) = f dg + g df$.
- 6) Let $g(x) = x^2 + \sin x$. Calculate the differential dg .
- 7) If the radius of a sphere, with radius 10 cm, has to decrease by 0.1 cm, approximately how much will its volume decrease?
- 8) Find df for $f(x) = x^2 + 3x$ and evaluate it; $x = 2$ and $dx = 0.1$.
- 9) Assuming $\log_{10} e = 0.4343$, find an approximate value of $\log_{10} 100$.
- 10) In a newly developed city, it is estimated that the voting population (in thousands) will increase according to $v(t) = 30 + 12t^2 - t^3$, $0 \leq t \leq 8$ where t is the time in years. Find the approximate change in votes for the time change from 4 to $4\frac{1}{6}$ years.
- 11) Show that $f(x, y) = \frac{x^2 - y^2}{y^2 + 1}$ is continuous at every $(x, y) \in \mathbb{R}^2$.
- 12) Let $w(x, y) = xy + \frac{ey}{y^2 + 1}$ for all $(x, y) \in \mathbb{R}^2$. Calculate $\frac{d^2 w}{dy dx}$ and $\frac{d^2 w}{dx dy}$.
- 13) Let $u(x, y) = e^{-2y} \cos(2x)$ for all $(x, y) \in \mathbb{R}^2$. Prove that u is a harmonic function in \mathbb{R}^2 .
- 14) If $U(x, y, z) = \log(x^3 + y^3 + z^3)$, find $\frac{\partial U}{\partial x} + \frac{\partial U}{\partial y} + \frac{\partial U}{\partial z}$.

- 15) If $w(x, y, z) = x^2y + y^2z + z^2x$, $x, y, z \in \mathbb{R}$, find differential dw
- 16) Let $z(x, y) = x^2y + 3xy^4$, $x, y \in \mathbb{R}$. find linear approximation for z at $(2, -1)$
- 17) Verify $\frac{dw}{dt} = \frac{dw}{dx} \frac{dx}{dt} + \frac{dw}{dy} \frac{dy}{dt}$ for $F(x, y) = x^2 - 2y^2 + 2xy$ and $x(t) = \cos t$, $y(t) = \sin t$, $t \in [0, 2\pi]$
- 18) Let $z(x, y) = x^3 - 3x^2y^3$, where $x = se^t$, $y = se^{-t}$, $s, t \in \mathbb{R}$. Find $\frac{dz}{ds}$ and $\frac{dz}{dt}$
- 19) $F(x, y) = \frac{x^2 + 5xy - 10y^2}{3x + 7y}$, show that $F(x, y)$ is a homogenous function of degree 1 .
- 20) If $u = \sin^{-1} \left(\frac{x+y}{\sqrt{x+y}} \right)$, show that $x \frac{du}{dx} + y \frac{du}{dy} = \frac{1}{2} \tan u$
- 21) If $u(x, y) = \frac{x^2 + y^2}{\sqrt{x+y}}$, prove that $x \frac{du}{dx} + y \frac{du}{dy} = \frac{3}{2} u$
- 22) If $v(x, y) = \log \left(\frac{x^2 + y^2}{x+y} \right)$, prove that $x \frac{dv}{dx} + y \frac{dv}{dy} = 1$

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