

FML

## FIRST MID TERM TEST - 2024

12 - Std

MATHEMATICS

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Time : 1.30 Hrs.

MARKS : 50

## PART - A

## I Choose the correct answer.

10 X 1 = 10

1. If  $|\text{adj}(\text{adj} A)| = |A|^9$ , then the order of the square matrix A is  
a) 3                      b) 4                      c) 2                      d) 5
2. Let  $A = \begin{bmatrix} 2 & -1 & 1 \\ -1 & 2 & -1 \\ 1 & -1 & 2 \end{bmatrix}$  and  $AB = \begin{bmatrix} 3 & 1 & -1 \\ 1 & 3 & x \\ -1 & 1 & 3 \end{bmatrix}$ , if B is the inverse of A, then the value of x is  
a) 2                      b) 4                      c) 3                      d) 1
3. The value of  $\sum_{i=1}^{13} (i^n + i^{n-1})$  is  
a)  $1 + i$                       b)  $i$                       c) 1                      d) 0
4. If  $\left| z - \frac{3}{z} \right| = 2$ , then the least value of  $|z|$  is  
a) 1                      b) 2                      c) 3                      d) 5
5. The principal argument of  $\frac{3}{-1+i}$  is  
a)  $\frac{-5\pi}{6}$                       b)  $\frac{-2\pi}{3}$                       c)  $\frac{-3\pi}{4}$                       d)  $\frac{-\pi}{2}$
6. According to the rational root theorem, which number is not possible rational root of  $4x^7 + 2x^4 - 10^3 - 5$ ?  
a) -1                      b)  $\frac{5}{4}$                       c)  $\frac{4}{5}$                       d) 5
7. The polynomial  $x^3 - kx^2 + 9x$  has three real roots if and only if, k satisfies  
a)  $|k| \leq 6$                       b)  $k = 0$                       c)  $|k| > 6$                       d)  $|k| \geq 6$
8. If the system of linear equations  $x + y + az = b$ ,  $x + 5y + 2z = 6$ ,  $x + 2y + 3z = 3$  has infinitely many solutions then the value of a and b is  
a) 3,7                      b) 7,3                      c) -3, 7                      d) 3,-7
9. If  $z = x + iy$ , then the argument  $\theta$  is  
a)  $[-\pi, \pi]$                       b)  $(-\pi, \pi)$                       c)  $(-\pi, \pi]$                       d)  $[-\pi, \pi)$
10. The sum of all the  $n^{\text{th}}$  root of unity is  
a) 0                      b) 1                      c) -1                      d)  $\frac{1}{n}$

## PART - B

## II Answer any four question. (Q.No. 16 is compulsory)

4 X 2 = 8

11. Prove that  $\begin{bmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{bmatrix}$  is orthogonal.
12. Solve the system of linear equations by matrix inversion method  
 $2x + 5y = -2$ ,  $x + 2y = -3$



13. If  $|z| = 2$  show that  $3 \leq |z + 3 + 4i| \leq 7$ .
14. Show that  $i) (2+i\sqrt{3})^{10} - (2-i\sqrt{3})^{10}$  is purely imaginary.
15. Find a polynomial equation of minimum degree with rational coefficients, having  $2+\sqrt{3}i$  as a root.
16. Find the square root of  $-7 + 24i$ .

**PART - C**

Answer any four questions. (Q.No. 22 is compulsory)

$4 \times 3 = 12$

17. Find the rank of the matrix  $\begin{bmatrix} 2 & -2 & 4 & 3 \\ -3 & 4 & -2 & -1 \\ 6 & 2 & -1 & 7 \end{bmatrix}$ .
18. Test the consistency of the system of linear equations.  
 $x - y + z = -9$ ,  $2x - y + z = 4$ ,  $3x - y + z = 6$ ,  $4x - y + 2z = 7$ .
19. Show that the equation  $z^3 + 2\bar{z} = 0$  has five solutions.
20. If  $z = (\cos \theta + i \sin \theta)$ , show that  $z^n + \frac{1}{z^n} = 2\cos n\theta$  and  $z^n - \frac{1}{z^n} = 2i \sin n\theta$ .
21. If  $p$  and  $q$  are the roots of the equation  $lx^2 + nx + n = 0$ , show that  
 $\sqrt{\frac{p}{q}} + \sqrt{\frac{q}{p}} + \sqrt{\frac{n}{l}} = 0$ .
22. If  $z_1 = r_1 (\cos \theta_1 + i \sin \theta_1)$  and  $z_2 = r_2 (\cos \theta_2 + i \sin \theta_2)$ , prove that  
 $\arg\left(\frac{z_1}{z_2}\right) = \arg(z_1) - \arg(z_2)$ .

**PART - D**

Answer all the questions.

23. a) Solve the systems of linear equations by Cramer's rule :  
 $\frac{3}{4} - \frac{4}{y} - \frac{2}{z} - 1 = 0$ ,  $\frac{1}{x} + \frac{2}{y} + \frac{1}{z} - 2 = 0$ ,  $\frac{2}{x} - \frac{5}{y} - \frac{4}{z} + 1 = 0$ . (OR)
- b) Given the complex number  $z = 3 + 2i$ , represent the complex numbers  $z$ ,  $iz$  and  $z + iz$  on one argand diagram. Show that these complex numbers form the vertices of an isosceles right triangle.
24. a) Investigate for what values of  $\lambda$  and  $\mu$  the system of linear equations  
 $x + 2y + z = 7$ ,  $x + y + \lambda z = \mu$ ,  $x + 3y - 5z = 5$  has i) no solution  
 ii) a unique solution iii) an infinite number of solution. (OR)
- b) If  $2 + i$  and  $3 - \sqrt{2}$  are roots of the equation  
 $x^6 - 13x^5 + 62x^4 - 126x^3 + 65x^2 + 127x - 140 = 0$  find all roots.
25. a) If  $z = x + iy$  and  $\arg\left(\frac{z-i}{z+2}\right) = \frac{\pi}{4}$ , show that  $x^2 + y^2 + 3x - 3y + 2 = 0$ . (OR)
- b) Solve the equation  $6x^4 - 5x^3 - 38x^2 - 5x + 6 = 0$  if it is known that  $\frac{1}{3}$  is a solution.
26. a) If  $n$  is a positive integer, prove that  $(\sqrt{3} + i)^n + (\sqrt{3} - i)^n = 2^{n+1} \cos \frac{n\pi}{6}$  (OR)
- b) Test the consistency of the system of linear equations  $2x + 5y + 7z = 52$ ,  
 $x + y + z = 9$ ,  $2x + y - z = 0$ .

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