



# JAYAM TUITION CENTRE.

VETTAVALAM. TIRUVANNAMALAI-DT.

STD: 12  
SUB: MATHS  
MARKS: 25

## EXERCISE TEST -5 (EX:2-7)

### 2 Mark Questions

$5 \times 2 = 10$

1. Find the principal argument  $\operatorname{Arg} z$ , when  $z = \frac{-2}{1+i\sqrt{3}}$ .
2. Find the product  $\frac{3}{2} \left( \cos \frac{\pi}{3} + i \sin \frac{\pi}{3} \right) \cdot 6 \left( \cos \frac{5\pi}{6} + i \sin \frac{5\pi}{6} \right)$  in rectangular form.
3. Find the quotient  $\frac{2(\cos \frac{9\pi}{4} + i \sin \frac{9\pi}{4})}{4(\cos(\frac{-3\pi}{2}) + i \sin(\frac{-3\pi}{2}))}$  in rectangular form.
4. If  $\frac{1+z}{1-z} = \cos 2\theta + i \sin 2\theta$ , show that  $z = i \tan \theta$ .
5. Write in polar form of the following complex number  $\frac{i-1}{\cos \frac{\pi}{3} + i \sin \frac{\pi}{3}}$

### 5 Mark Questions

$3 \times 5 = 15$

6. If  $z = x + iy$  and  $\arg \left( \frac{z-i}{z+2} \right) = \frac{\pi}{4}$ , show that  $x^2 + y^2 + 3x - 3y + 2 = 0$ .
7. If  $z = x + iy$  and  $\arg \left( \frac{z-1}{z+1} \right) = \frac{\pi}{2}$ , show that  $x^2 + y^2 = 1$ .
8. If  $\cos \alpha + \cos \beta + \cos \gamma = \sin \alpha + \sin \beta + \sin \gamma = 0$ , show that
  - (i)  $\cos 3\alpha + \cos 3\beta + \cos 3\gamma = 3 \cos(\alpha + \beta + \gamma)$  and
  - (ii)  $\sin 3\alpha + \sin 3\beta + \sin 3\gamma = 3 \sin(\alpha + \beta + \gamma)$ .