

RS3

## THIRD REVISION EXAMINATION - 2025

10 - Std

MATHEMATICS

TIME : 3.00 Hrs

PART - I

MARKS : 100

CHOOSE THE CORRECT ANSWER:

14X1=14

1. Let  $n(A) = m$  and  $n(B) = n$  then the total number of non-empty relations that can be defined from A to B is  
 (a)  $m^n$       (b)  $n^m$       (c)  $2^{mn} - 1$       (d)  $2^{mn}$
2. The function  $f : N \rightarrow Z$  is defined by  $f(x) = (-1)^x$ . then the function f is  
 (a) one to one function      (b) many-one function  
 (c) constant function      (d) identity function
3. Using Euclid's division lemma, if the cube of any positive integer is divided by 9 then the possible remainders are  
 (a) 0,1,8      (b) 1,4,8      (c) 0,1,3      (d) 1,3,5
4. An A.P consists of 31 terms. If its 16<sup>th</sup> term is m, then the sum of all the terms of this A.P. is  
 (a) 16m      (b) 62m      (c) 31m      (d)  $\frac{31m}{2}$
5. The square root of  $\frac{256x^8y^4z^{10}}{25x^6y^6z^6}$  is equal to  
 (a)  $\frac{16}{5} \sqrt{\frac{x^2z^4}{y^2}}$       (b)  $16 \sqrt{\frac{y^2}{x^2z^4}}$       (c)  $\frac{16}{5} \sqrt{\frac{y}{xz^2}}$       (d)  $\frac{16}{5} \sqrt{\frac{xz^2}{y}}$
6. For the given matrix  $A = (0 \ 0 \ 0)$  then the order of the matrix  $A^T$  is  
 (a)  $0 \times 0$       (b)  $1 \times 3$       (c)  $3 \times 1$       (d)  $1 \times 0$
7. In a  $\Delta ABC$ , AD is the bisector of  $\angle BAC$ . If  $AB = 8\text{cm}$ ,  $BD = 6\text{cm}$  and  $DC = 3\text{cm}$ . The length of the side AC is  
 (a) 6cm      (b) 4 cm      (c) 3 cm      (d) 8cm
8. The slope of the line which is perpendicular to a line joining the points (0,0) and (-8,8) is  
 (a) -1      (b) 1      (c)  $\frac{1}{3}$       (d) -8
9. Which one of the following equation of straight line passing through origin?  
 (a)  $x = 2y + 5$       (b)  $y = \frac{1}{2}x$       (c)  $y = 7$       (d)  $x = 4$

10. If  $x = a \tan \theta$  and  $y = b \sec \theta$  then
- (a)  $\frac{y^2}{b^2} - \frac{x^2}{a^2} = 1$                       (b)  $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$
- (c)  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$                       (d)  $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 0$
11. In a hollow cylinder, the sum of the external and internal radii is 14cm and the width is 4 cm. If its height is 20 cm, the volume of the material in it is
- (a)  $5600 \pi \text{ cm}^3$     (b)  $1120 \pi \text{ cm}^3$     (c)  $56\pi \text{ cm}^3$                       (d)  $3600\pi \text{ cm}^3$
12. The CSA of a right circular cone whose height is equal to its radius -----(sq. units)
- (a)  $2\pi r^2$                       (b)  $\pi r l$                       (c)  $\sqrt{2} \pi r^2$                       (d)  $\sqrt{2} \pi r$
13. Which of the following is not a measure of dispersion?
- (a) Range                      (b) standard deviation    (c) arithmetic mean                      (d) variance
14. Which of the following values cannot be a probability of an event?
- (a)  $\frac{3}{10}$                       (b)  $\frac{4}{5}$                       (c) 0                      (d)  $\frac{7}{4}$

## PART - II

ANSWER ANY 10 QUESTIONS. QUESTION NO.28 IS COMPULSORY:                      10 X 2 = 20

15. If  $B \times A = \{(-2, 3), (-2, 4), (0, 3), (0, 4), (3, 3), (3, 4)\}$  find A and B.
16. Find the value of k, such that  $f \circ g = g \circ f$  if  $f(x) = 2x - k$ ,  $g(x) = 4x + 5$ .
17. Find the 15<sup>th</sup> term of an A.P given by 3, 15, 27, 39, ...
18. Find the sum of 8 term of the G.P 1, -3, 9, -27, ...
19. Find the square root of the following rational expression  $\frac{400 x^4 y^{12} z^{16}}{100 x^8 y^4 z^4}$
20. If  $\alpha$  and  $\beta$  are the roots of  $x^2 + 7x + 10 = 0$ . Find the value of  $\alpha - \beta$ .
21. Construct a 3X3 matrix whose element are given by  $a_{ij} = |i - 2j|$ .
22. If  $\Delta ABC \sim \Delta DEF$  such that area of  $\Delta ABC$  is  $9 \text{ cm}^2$  and the area of  $\Delta DEF$  is  $16 \text{ cm}^2$  and  $BC = 2.1 \text{ cm}$ . Find the length of EF.

23. Find the value of 'a', if the line through (-2,3) and (8,5) is perpendicular to  $y = ax + 2$ .
24. Prove that  $\tan^2\theta - \sin^2\theta = \tan^2\theta \cdot \sin^2\theta$
25. The external radius and the length of a hollow wooden log are 16cm and 13 cm respectively. If its thickness is 4cm then find its T.S.A.
26. Find the range and coefficient of range of the following data : 25, 67, 48, 53, 18, 39, 44.
27. If A and B are two mutually exclusive events of a random experiment and  $P(\text{not } A) = 0.45$ ,  $P(A \cup B) = 0.65$ , then find  $P(B)$ .
28. The hill in the form of a right triangle has its foot at (5,0) . The inclination of the hill to the ground is  $30^\circ$  . Find the equation of the hill joining the foot and top.

## PART III

ANSWER ANY 10 QUESTIONS. QUESTION NO.42 IS COMPULSORY:  $10 \times 5 = 50$

29. Let A= The set of all natural numbers less than 8, B= The set of all prime numbers less than 8, C= The set of even prime number. Verify that  $A \times (B - C) = (A \times B) - (A \times C)$ .

30. If the function  $f: [-5,9] \rightarrow \mathbb{R}$  is defined as follows  $f(x) = \begin{cases} 6x + 1 & ; -5 \leq x < 2 \\ 5x^2 - 1 & ; 2 \leq x < 6 \\ 3x - 4 & ; 6 \leq x \leq 9 \end{cases}$

then find the values of (i)  $f(-3) + f(2)$  (ii)  $f(7) - f(1)$

(iii)  $2f(4) + f(8)$  (iv)  $\frac{2f(-2) - f(6)}{f(4) + f(-2)}$

31. The 104<sup>th</sup> term and 4<sup>th</sup> term of an A.P are 125 and 0. Find the sum of first 35 terms.

32. In a Geometric progression, the 4<sup>th</sup> term is  $\frac{8}{9}$  and the 7<sup>th</sup> term is  $\frac{64}{243}$ . Find the Geometric Progression.

33. Simplify  $\frac{1}{x^2 - 5x + 6} + \frac{1}{x^2 - 3x + 2} - \frac{1}{x^2 - 8x + 15}$

34. A bus covers a distance of 90 km at a uniform speed. Had the speed been 15km/hour more it would have taken 30 minutes less for the journey. Find the original speed of the bus.

35. Let  $A = \begin{pmatrix} 1 & 2 \\ 1 & 3 \end{pmatrix}$   $B = \begin{pmatrix} 4 & 0 \\ 1 & 5 \end{pmatrix}$   $C = \begin{pmatrix} 2 & 0 \\ 1 & 2 \end{pmatrix}$  show that  $(A-B)C = (AC-BC)$ .
36. State and prove Thales theorem.
37. A quadrilateral has vertices at A (-4, -2), B (5, -1), C (6, 5) and D (-7, 6). Show that the mid points of its sides form a parallelogram.
38. Find the equation of a straight line through the point of intersection of the lines  $8x+3y=18$ ,  $4x+5y=9$  and bisecting the line segment joining the points (5, -4) and (-7, 6).
39. From the top of a 12 m high building, the angle of elevation of the top of a cable tower is  $60^\circ$  and the angle of depression of its foot is  $30^\circ$ . Determine the height of the tower.
40. Nathan, an engineering student was asked to make a model shaped like a cylinder with two cones attached at its two ends. The diameter of the model is 3 cm and its length is 12 cm. If each cone has a height of 2 cm, find the volume of model that Nathan made.
41. The number of televisions sold in each day of a week are 13, 8, 4, 9, 7, 12, 10. Find its standard deviation.
42. Two dice are rolled once. Find the probability of getting a composite number on the first die or a prime number on the second die.

### PART - IV

ANSWER ALL THE QUESTIONS:

2 X 8 = 16

43. (a) Take a point which is 11 cm away from the centre of a circle of radius 4 cm and draw the two tangents to the circle from that point. Also measure the length of the tangents: **(OR)**
- b) Construct a  $\Delta PQR$  in which  $PQ = 8\text{ cm}$ ,  $\angle R = 60^\circ$  and the median  $RG$  from  $R$  to  $PQ$  is 5.8 cm. Find the length of the altitude from  $R$  to  $PQ$ .
44. a) Nishanth is the winner in a marathon race of 12km distance. He ran at the uniform speed of 12 km/hr and reached the destination in 1 hour. He was followed by Aradhana, Ponmozhi, Jeyanth, Sathya and Swetha with their respective speed of 6 km/hr, 4 km/hr, 3 km/hr, 2 km/hr. And, they covered the distance in 2hrs, 3 hrs, 4 hrs and 6 hrs respectively. Draw the speed-time graph and use it to find the time taken to Kaushik with his speed of 2.4 km/hr. **(OR)**
- (b) Draw the graph of  $y = 2x^2$  and hence solve  $2x^2 - x - 6 = 0$ .