



Standard 11

MATHEMATICS

Time Allowed: 3.00 Hours

Maximum Marks: 90

I. Choose the best: **$20 \times 1 = 20$**

- 1) If $A = \{(X,Y) | Y = \sin X, X \in R\}$ and $B = \{(X,Y) : Y = \sin X, X \in R\}$ then $A \cap B$ contains
 - a) can't be determined
 - b) no elements
 - c) infinitely many elements
 - d) only one element
- 2) If the function $f : [-3,3] \rightarrow S$ defined by $f(x) = X^2$ is on to, then S is
 - a) $[0,9]$
 - b) $[-9,9]$
 - c) R
 - d) $[-3,3]$
- 3) The value of $\log_{\sqrt{2}} 512$ is
 - a) 9
 - b) 16
 - c) 12
 - d) 18
- 4) $n_{C_0} + n_{C_1} + \dots + n_{C_n} =$
 - a) 2^{n+1}
 - b) 2^n
 - c) 2^{n-1}
 - d) $2n$
- 5) There are n locks and n matching keys. If all the locks and keys are to be perfectly matched then the max. no. of trials is
 - a) $n(n-1)$
 - b) $n(n+1)$
 - c) n
 - d) $\frac{n(n+1)}{2}$
- 6) $\frac{\sin(A-B)}{\cos A \cos B} + \frac{\sin(B-C)}{\cos B \cos C} + \frac{\sin(C-A)}{\cos C \cos A}$ is
 - a) 0
 - b) $\sin A + \sin B + \sin C$
 - c) $\cos A + \cos B + \cos C$
 - d) 1
- 7) Which of the following is not true?
 - a) $\tan \theta = 25$
 - b) $\sin \theta = \frac{3}{4}$
 - c) $\sec \theta = \frac{1}{4}$
 - d) $\cos \theta = -1$
- 8) The co-efficient of x^5 in the series e^{-2x} is
 - a) $-\frac{4}{15}$
 - b) $\frac{2}{3}$
 - c) $\frac{4}{15}$
 - d) $\frac{3}{2}$
- 9) The sequence $\frac{1}{\sqrt{3}}, \frac{1}{\sqrt{3}+\sqrt{2}}, \frac{1}{\sqrt{3}+2\sqrt{2}}, \dots$ form an
 - a) Harmonic progression
 - b) Arithmetic progression
 - c) Arithmetic - Geometric progression
 - d) Geometric progression
- 10) The pt. lie on the locus of $3x^2 + 3y^2 - 8x - 12y + 17 = 0$
 - a) (1,2)
 - b) (0,0)
 - c) (0,-1)
 - d) (-2,3)

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- 11) If one of the lines given by $6X^2 - XY + 4CY^2 = 0$ is $3X + 4Y = 0$ then C equals to
 a) 3 b) -3 c) 1 d) -1
- 12) If A is a square matrix, then which of the following is not symmetric
 a) $A - A^T$ b) $A + A^T$ c) AA^T d) A^TA
- 13) If $A + I = \begin{bmatrix} 3 & -2 \\ 4 & 1 \end{bmatrix}$ then $(A+I)(A-I)$ is equal to
 a) $\begin{bmatrix} -5 & -4 \\ -8 & -9 \end{bmatrix}$ b) $\begin{bmatrix} -5 & -4 \\ 8 & -9 \end{bmatrix}$ c) $\begin{bmatrix} -5 & 4 \\ -8 & 9 \end{bmatrix}$ d) $\begin{bmatrix} 5 & 4 \\ 8 & 9 \end{bmatrix}$
- 14) If $|\bar{a} + \bar{b}| = 60$, $|\bar{a} - \bar{b}| = 40$ and $|\bar{b}| = 46$ then $|\bar{a}| = ?$
 a) 32 b) 42 c) 12 d) 22
- 15) If \bar{a} and \bar{b} include an angle 120° and their magnitude are 2 and $\sqrt{3}$ then
 $\bar{a} \cdot \bar{b} = ?$
 a) $-\frac{\sqrt{3}}{2}$ b) $\sqrt{3}$ c) $-\sqrt{3}$ d) 2
- 16) $\lim_{x \rightarrow \infty} \frac{\sin x}{x} =$
 a) ∞ b) 1 c) $-\infty$ d) 0
- 17) If $Y = e^{\sin x}$ then $\frac{dY}{dx} =$
 a) $\sin x e^{\sin x}$ b) $\cos x$ c) $\cos x e^{\sin x}$ d) $e^{\cos x}$
- 18) $\int \frac{\sin \sqrt{x}}{\sqrt{x}} dx =$
 a) $-2 \sin \sqrt{x} + C$ b) $2 \cos \sqrt{x} + C$ c) $-2 \cos \sqrt{x} + C$ d) $2 \sin \sqrt{x} + C$
- 19) Ten coins are tossed. The probability of getting atleast 8 head is
 a) $\frac{7}{16}$ b) $\frac{7}{64}$ c) $\frac{7}{128}$ d) $\frac{7}{32}$
- 20) $\int \frac{\sqrt{\tan x}}{\sin 2x} dx$ is
 a) $\frac{1}{2} \sqrt{\tan x} + C$ b) $\sqrt{\tan x} + C$ c) $\frac{1}{4} \sqrt{\tan x} + C$ d) $2\sqrt{\tan x} + C$

II. Answer any seven questions. Question No.30 is compulsory. $7 \times 2 = 14$

21) Resolve the rational expression $\frac{1}{x^2 - a^2}$ into partial fraction.

22) Find the co-efficient of X^5 in the expression of $\left(\frac{1}{X^3}\right)^{17}$
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- 23) Find the equation of the straight line, if the perpendicular from the origin makes an angle of 120° with x-axis and the length of perpendicular from the origin is 6 units.

24) $\tan(45^\circ - A) = \frac{1 - \tan A}{1 + \tan A}$

- 25) Find $|\bar{a} \times \bar{b}|$, where $\bar{a} = \bar{i} + 4\bar{j}$ and $\bar{b} = \bar{i} + \bar{j} + \bar{k}$.

- 26) Find F'' if $f(x) = x \cos x$.

- 27) Find $\sqrt[3]{1001}$ approximately (two decimal places).

28) Evaluate : $\lim_{n \rightarrow \infty} (5^n + 6^n)^{\frac{1}{n}}$.

- 29) a) The odds that the event A occurs is 5 to 7, then find $P(A)$.

- b) Suppose $P(B) = \frac{2}{5}$. Express the odds that the event B occurs.

30) Compute $|A|$ if $A = \begin{bmatrix} 3 & 4 & 1 \\ 0 & -1 & 2 \\ 5 & -2 & 6 \end{bmatrix}$.

III. Answer any seven questions. Question No.40 is compulsory. $7 \times 3 = 21$

31) Find the range of $f(x) = \frac{1}{1 - 3 \cos x}$.

- 32) In how many ways 5 boys and 4 girls can be seated in a row, so that no two girls are together?

33) Find the value of the product $\begin{vmatrix} \log_3 64 & \log_4 3 \\ \log_3 8 & \log_4 9 \end{vmatrix} \times \begin{vmatrix} \log_2 3 & \log_8 3 \\ \log_3 4 & \log_3 4 \end{vmatrix}$.

- 34) Differentiate the function w.r.t x $Y = x e^x \log x$.

35) Evaluate : $\int x e^x dx$.

36) Solve the equation $\sqrt{6 - 4x - x^2} = x + 4$.

- 37) If θ is a parameter, find the equation of the locus of a moving point, whose co-ordinate are $x = a \cos^3 \theta$, $y = a \sin^3 \theta$.

- 38) The probability of an event A occurring is 0.5 and B occur is 0.3. If A and B are mutually exclusive events then the probability of

(i) $P(A \cup B)$ (ii) $P(A \cap B)$ (iii) $P(\bar{A} \cap B)$

39) S.T $\bar{a} \times (\bar{b} + \bar{c}) + \bar{b} \times (\bar{c} + \bar{a}) + \bar{c} \times (\bar{a} + \bar{b}) = \bar{0}$.

- 40) Find the value of $\cos 105^\circ$.

IV. Answer all the questions.

$7 \times 5 = 35$

- 41) a) If $A + B + C = \frac{\pi}{2}$, Prove that $\cos 2A + \cos 2B + \cos 2C = 1 + 4 \sin A \sin B \sin C$.

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- b) S.T the whose points vectors are $4\vec{i} + 5\vec{j} + \vec{k}$, $-\vec{j} - \vec{k}$, $3\vec{i} + 9\vec{j} + 4\vec{k}$ and $-4\vec{i} + 4\vec{j} + 4\vec{k}$ are co-planar.

- 42) a) By the principle of mathematical induction, Prove that for $n \geq 1$,

$$1^2 + 3^2 + 5^2 + \dots + (2n-1)^2 = \frac{n(2n-1)(2n+1)}{3}. \quad (\text{OR})$$

- b) If $Y = \frac{\sin^{-1} X}{\sqrt{1-X^2}}$, S.T $(1-X^2)Y_2 - 3XY_1 - Y = 0$.

- 43) a) Prove that $\sqrt[3]{x^3 + 6} - \sqrt[3]{x^3 + 3}$ is approximately equal to $\frac{1}{x^2}$ when x is sufficiently large. (OR)

- b) There are two identical urns containing respectively 6 black and 4 red balls, 2 black and 2 red balls. An urn is chosen at random and a ball is drawn from it. Find the probability that the ball is black.

- 44) a) Resolve into partial fractions $\frac{2x}{(x^2+1)(x-1)}$. (OR)

- b) Express the matrix $A = \begin{bmatrix} 1 & 3 & 5 \\ -6 & 8 & 3 \\ -4 & 6 & 5 \end{bmatrix}$ as the sum of a symmetric and skew-symmetric matrices.

- 45) a) If the equation $\lambda X^2 - 10XY + 12Y^2 + 5X - 16Y - 3 = 0$ represents a pair of straight lines find

- i) The value of λ and the separate equations of the lines
 - ii) Point of intersection of the lines
 - iii) Angle between the lines
- (OR)

- b) Evaluate : $\int \frac{6x+5}{\sqrt{1-4x-4x^2}} dx$.

- 46) a) If $f: R \rightarrow R$ is defined by $f(x) = 2x - 3$, Prove that f is a bijection and find its inverse. (OR)

- b) Evaluate : $\int \frac{3x+5}{x^2+4x+7} dx$.

- 47) a) State and prove Napier's formula. (OR)

- b) Prove that $\lim_{\theta \rightarrow 0} \frac{\sin \theta}{\theta} = 1$.