

PART - ACHOOSE THE CORRET ANSWER :-

20 X 1 = 20

- 1) If $P = \begin{bmatrix} 1 & x & 0 \\ 1 & 3 & 0 \\ 2 & 4 & -2 \end{bmatrix}$ is the adjoint of 3×3 matrix A and $|A| = 4$, then x is
 (a) 15 (b) 12 (c) 14 (d) 11
- 2) If $A = \begin{bmatrix} 3 & -3 & 4 \\ 2 & -3 & 4 \\ 0 & -1 & 1 \end{bmatrix}$, then $\text{adj}(\text{adj } A)$ is
 (a) $\begin{bmatrix} 3 & -3 & 4 \\ 2 & -3 & 4 \\ 0 & -1 & 1 \end{bmatrix}$ (b) $\begin{bmatrix} 6 & -6 & 8 \\ 4 & -6 & 8 \\ 0 & -2 & 2 \end{bmatrix}$ (c) $\begin{bmatrix} -3 & 3 & -4 \\ -2 & 3 & -4 \\ 0 & 1 & -1 \end{bmatrix}$ (d) $\begin{bmatrix} 3 & -3 & 4 \\ 0 & -1 & 1 \\ 2 & -3 & 4 \end{bmatrix}$
- 3) The value of $\left(\frac{1+\sqrt{3}i}{1-\sqrt{3}i}\right)^{10}$ is
 (a) $\text{cis } \frac{2\pi}{3}$ (b) $\text{cis } \frac{4\pi}{3}$ (c) $-\text{cis } \frac{2\pi}{3}$ (d) $-\text{cis } \frac{4\pi}{3}$
- 4) A zero of $x^3 + 64$ is
 (a) 0 (b) 4 (c) $4i$ (d) -4
- 5) The equation $\tan^{-1} x - \cot^{-1} x = \tan^{-1}\left(\frac{1}{\sqrt{3}}\right)$ has
 (a) no solution (b) unique solution (c) two solutions (d) infinite number of solutions
- 6) The circle passing through $(1, -2)$ and touching the axis of x at $(3, 0)$ passing through the point
 (a) $(-5, 2)$ (b) $(2, -5)$ (c) $(5, -2)$ (d) $(-2, 5)$
- 7) If a vector \vec{a} lies in the plane of $\vec{\beta}$ and $\vec{\gamma}$, then
 (a) $[\vec{a}, \vec{\beta}, \vec{\gamma}] = 1$ (b) $[\vec{a}, \vec{\beta}, \vec{\gamma}] = -1$ (c) $[\vec{a}, \vec{\beta}, \vec{\gamma}] = 0$ (d) $[\vec{a}, \vec{\beta}, \vec{\gamma}] = 2$
- 8) The tangent to the curve $y^2 - xy + 9 = 0$ is vertical when
 (a) $y = 0$ (b) $y = \pm\sqrt{3}$ (c) $y = \frac{1}{2}$ (d) $y = \pm 3$
- 9) If $g(x, y) = 3x^2 - 5y + 2y^2$, $x(t) = e^t$ and $y(t) = \cos t$, then $\frac{dg}{dt}$ is equal to
 (a) $6e^{2t} + 5 \sin t - 4 \cos t \sin t$ (b) $6e^{2t} - 5 \sin t + 4 \cos t \sin t$
 (c) $3e^{2t} + 5 \sin t + 4 \cos t \sin t$ (d) $3e^{2t} - 5 \sin t + 4 \cos t \sin t$
- 10) The value of $\int_0^{\frac{2}{3}} \frac{dx}{\sqrt{4-9x^2}}$ is (a) $\frac{\pi}{6}$ (b) $\frac{\pi}{2}$ (c) $\frac{\pi}{4}$ (d) π

- 11) The value of $\int_0^1 (\sin^{-1} x)^2 dx$ is
 (a) $\frac{\pi^2}{4} - 1$ (b) $\frac{\pi^2}{4} + 2$ (c) $\frac{\pi^2}{4} + 1$ (d) $\frac{\pi^2}{4} - 2$
- 12) The solution of the differential equation $\frac{dy}{dx} = 2xy$ is
 (a) $y = Ce^{x^2}$ (b) $y = 2x^2 + C$ (c) $y = Ce^{-x^2} + C$ (d) $y = x^2 + C$
- 13) Let X have a Bernoulli distribution with mean 0.4, then the variance of $(2X - 3)$ is
 (a) 0.24 (b) 0.48 (c) 0.6 (d) 0.96
- 14) Subtraction is not a binary operation in
 (a) \mathbb{R} (b) \mathbb{Z} (c) \mathbb{N} (d) \mathbb{Q}
- 15) The proposition $p \wedge (\neg p \vee q)$ is
 (a) a tautology (b) a contradiction (c) logically equivalent to $p \wedge q$ (d) logically equivalent to $p \vee q$
- 16) If z is a complex number of unit modulus and argument θ , then $\arg\left(\frac{1+z}{1+\bar{z}}\right)$ equals
 (a) $-\theta$ (b) $\frac{\pi}{2} - \theta$ (c) θ (d) $\pi - \theta$
- 17) If $x = \sin^{-1}(\sin 10)$ and $y = \cos^{-1}(\cos 10)$, then $y - x$ is
 (a) π (b) 7π (c) 0 (d) 10
- 18) If $[\vec{a} + \vec{b} \quad \vec{b} + \vec{c} \quad \vec{c} + \vec{a}] = \lambda [\vec{a} \quad \vec{b} \quad \vec{c}]$ then the value of λ is
 (a) 0 (b) 1 (c) 2 (d) 3
- 19) The point on the curve $y = x^2 - 5x + 5$ at which the tangent is parallel to the line $4x - 2y + 1 = 0$ is
 (a) $\left(\frac{1}{4}, \frac{7}{2}\right)$ (b) $\left(\frac{7}{2}, -\frac{1}{4}\right)$ (c) $\left(\frac{1}{8}, \frac{7}{2}\right)$ (d) $\left(\frac{7}{2}, -\frac{1}{8}\right)$
- 20) The order and degree of the differential equation $\frac{d^2}{dx^2}\left(\frac{d^2y}{dx^2}\right) = 0$
 (a) 2, 2 (b) 4, 4 (c) 2, 1 (d) 4, 1

PART - B

ANSWER ANY SEVEN QUESTIONS (Q.NO : 30 IS COMPULSORY) :- 7 X 2 = 14

21. Find the rank of the matrix $\begin{bmatrix} 1 & 2 & 3 \\ 2 & 1 & 4 \\ 3 & 0 & 5 \end{bmatrix}$

22. Find the square roots of $-6 + 8i$

23. Determine the number of positive and negative roots of the polynomial $x^5 - 19x^4 + 2x^3 + 5x^2 + 11$.

24. Find the equation of the parabola with focus $(-\sqrt{2}, 0)$ and directrix $x = \sqrt{2}$.

25. Prove that the function $f(x) = x^2 - 2x - 3$ is strictly increasing in $(2, \infty)$.

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26. A circular plate expands uniformly under the influence of heat. If its radius increases from 10.5cm to 10.75cm, then find an approximate change in the area.
27. Evaluate : $\int_{-\log 2}^{\log 2} e^{-|x|} dx$.
28. A train arrives punctually at a station every half an hour. Everyday in the morning, a student leaves his house to the train station. Let X denote the amount of time, in minutes, that the student waits for the train from the time he reaches the train station. It's known that the pdf of X is $f(x) = \begin{cases} \frac{1}{30}, & 0 < x < 30 \\ 0, & \text{elsewhere} \end{cases}$
- Obtain and interpret the expected value of the random variable X .
29. Let $*$ be defined on \mathbb{R} by $(a * b) = a + b + ab - 7$.
Is $*$ binary on \mathbb{R} ? If so, find $3 * \left(\frac{-7}{15}\right)$.
30. Find the value of $\tan\left(\cos^{-1}\left(-\frac{2}{7}\right) - \frac{\pi}{2}\right)$.

PART - C

ANSWER ANY SEVEN QUESTIONS (O.NO : 40 IS COMPULSORY) :- 7 X 3 = 21

31. If $A = \begin{bmatrix} 3 & 2 \\ 7 & 5 \end{bmatrix}$ and $B = \begin{bmatrix} -1 & -3 \\ 5 & 2 \end{bmatrix}$, verify that $(AB)^{-1} = B^{-1}A^{-1}$.
32. Simplify $\left(\frac{1+\cos 2\theta+i \sin 2\theta}{1+\cos 2\theta-i \sin 2\theta}\right)^{30}$.
33. Show that $\cot(\sin^{-1} x) = \frac{\sqrt{1-x^2}}{x}$, $-1 \leq x \leq 1$ and $x \neq 0$.
34. Find the magnitude and direction cosines of the torque (moment) of a force represented by $3\hat{i} + 4\hat{j} - 5\hat{k}$ about the point with position vector $2\hat{i} - 3\hat{j} + 4\hat{k}$ acting through a point whose position vector is $4\hat{i} + 2\hat{j} - 3\hat{k}$.
35. Expand $\log(1+x)$ as a Maclaurin's series upto 4 non-zero terms for $-1 < x \leq 1$.
36. The time T , taken for a complete oscillation of a single pendulum with length l , is given by the equation $T = 2\pi \sqrt{\frac{l}{g}}$, where g is a constant. Find the approximate percentage error in the calculated value of T corresponding to an error of 2 percent in the value of l .
37. Solve : $\frac{dy}{dx} = e^{x+y} + x^3 e^y$.
38. Suppose a discrete random variable can only take the values 0,1, and 2. The probability mass function is defined by $f(x) = \begin{cases} \frac{x^2+1}{k}, & \text{for } x = 0,1,2 \\ 0 & \text{otherwise} \end{cases}$ Find (i) the value of k (ii) $P(X \geq 1)$.
39. Establish the equivalence property: $p \rightarrow q \equiv \neg p \vee q$.
40. Solve : $\int_{-\frac{x}{\sqrt{2}}}^x \frac{dt}{\sqrt{1-t^2}} = \frac{\pi}{2}$.

ANSWER ALL THE QUESTIONS :-

- 41 a. Investigate the values of λ and μ the system of linear equations $2x + 3y + 5z = 9$, $7x + 3y - 5z = 8$, $2x + 3y + \lambda z = \mu$, have (i) no solution (ii) a unique solution (iii) an infinite number of solutions. (OR)
- b. A bridge has a parabolic arch that is 10m high in the centre and 30m wide at the bottom. Find the height of the arch 6m from the centre, on either sides.
- 42 a. Show that the points $1, \frac{-1}{2} + i\frac{\sqrt{3}}{2}$, and $\frac{-1}{2} - i\frac{\sqrt{3}}{2}$ are the vertices of an equilateral triangle. (OR)
- b. Find the area of the region bounded by $2x - y + 1 = 0$, $y = -1$, $y = 3$ and y -axis.
- 43 a. If $u = \sin^{-1}\left(\frac{x+y}{\sqrt{x+y}}\right)$, Show that $x\frac{\partial u}{\partial x} + y\frac{\partial u}{\partial y} = \frac{1}{2}\tan u$. (OR)
- b. The probability density function of X is given by $f(x) = \begin{cases} k & 1 \leq x \leq 5 \\ 0 & \text{otherwise} \end{cases}$ then find
(i) the value of k (ii) Distribution function (iii) $P(2 < X < 4)$.
- 44 a. Find the value of $\sin\left(\tan^{-1}\left(\frac{1}{2}\right) - \cos^{-1}\left(\frac{4}{5}\right)\right)$. (OR)
- b. Find the vector parametric, vector non-parametric and Cartesian form of the equation of the plane passing through the points $(-1, 2, 0)$, $(2, 2, -1)$ and parallel to the straight line $\frac{x-1}{1} = \frac{2y+1}{-2} = \frac{z+1}{-1}$.
- 45 a. If $\vec{a} = \hat{i} - \hat{j}$, $\vec{b} = \hat{i} - \hat{j} - 4\hat{k}$, $\vec{c} = 3\hat{j} - \hat{k}$ and $\vec{d} = 2\hat{i} + 5\hat{j} + \hat{k}$,
verify that $(\vec{a} \times \vec{b}) \times (\vec{c} \times \vec{d}) = [\vec{a}, \vec{b}, \vec{d}]\vec{c} - [\vec{a}, \vec{b}, \vec{c}]\vec{d}$. (OR)
- b. Suppose a person deposits ₹10,000 Indian rupees in a bank account at the rate of 5% per annum compounded continuously. How much money will be in his bank account 18 months later?
- 46 a. For the function $f(x) = 4x^3 + 3x^2 - 6x + 1$ find the intervals of concavity and points of inflection. (OR)
- b. Verify (i) closure property, (ii) commutative property, (iii) associative property, (iv) existence of identity, and (v) existence of inverse for the operation $+_5$ on \mathbb{Z}_5 using table corresponding to addition modulo 5.
- 47a. Find the equation of the circle passing through the points $(1, 1)$, $(2, 4)$, and $(5, 3)$. (OR)
- b. Show that the two curves $y = x^3$ and $x^2 + 6y = 7$ are cut orthogonally.

①	d) 11	⑦	c) $[a^2 \vec{a} \vec{b} \vec{c}] = 0$	⑮	c) logically equivalent to p and q	
②	a) $\begin{bmatrix} 3 & -3 & 4 \\ 2 & -3 & 4 \\ 0 & -1 & 1 \end{bmatrix}$	⑧	d) $y \pm 3$	⑯	c) 0	
③	a) $\frac{2\pi}{3}$	⑨	a) $6e^{at} + 5\sin t - 4\cos t \sin t$	⑰	a) π	
④	d) -4	⑩	a) $\frac{\pi}{6}$	⑱	b) 1	
⑤	b) unique solution	⑪	d) $\frac{\pi^2}{4} - 2$	⑲	b) $(\frac{7}{2}, -\frac{1}{4})$	
⑥	c) (5, -2)	⑫	a) $y = ce^{x^2}$	⑳	d) (4, 1)	
		⑬	d) 0.96			
		⑭	c) N			
21	$A = \begin{bmatrix} 1 & 2 & 3 \\ 2 & 1 & 4 \\ 3 & 0 & 5 \end{bmatrix}$ $ A \neq 0$ — ① Reduc 2x2 matm. $ A = 1 - 4 = -3 \neq 0$ $\rho(A) = 2$ — ①	28	$\int_{-a}^a x f(x) dx = 0$ $E(x) = 15 \text{ mins}$			
22	$\sqrt{x+ib} = \pm \left(\sqrt{\frac{ x+a }{2}} + i \frac{b}{x} \sqrt{\frac{ x-a }{2}} \right)$ — ① $\sqrt{-6+8i} = \pm (\sqrt{2} + i2\sqrt{2})$ — ①	29	x is binary — ① $3 \times \left(\frac{7}{15}\right) = \frac{-88}{15}$ — ①			
23	$+ = 2$ Real = 3 — ① $- = 1$ Imaginai = 2 — ① $0 = 0$	30	$\tan^{-1}(\cos^{-1}(-\frac{2}{7}) - \frac{\pi}{2})$ $\tan^{-1}(\pi - \cos^{-1}(\frac{2}{7}) - \frac{\pi}{2})$ $\tan^{-1}(\frac{\pi}{2} - \cos^{-1}(\frac{2}{7}))$ $\cot^{-1}(\cos^{-1}(\frac{2}{7}))$ $\cot^{-1}(\cot^{-1}(\frac{2}{3\sqrt{5}})) \in (0, \pi)$ $\theta = \cot^{-1}(\frac{2}{3\sqrt{5}})$	w.k.T $\cos^{-1}(-x) = \pi - \cos^{-1}x$ $\cos^{-1}(-\frac{2}{7}) = \pi - \cos^{-1}(\frac{2}{7})$		
24	$a = \sqrt{2}$ — ① $y^2 = -\sqrt{2}x$ — ①					
25	$f'(x) = 2x - 2$ — ① $f''(x) > 0$ (2, 10) — ①					
26	$r < 10.5$ $dr = 0.25$ $A = \pi r^2$ — ① $dA = 2\pi r \cdot dr$ $dA = 5.25\pi$ — ①					
27	$f(x)$ even function — ① $\int_{-\log 2}^{\log 2} e^{- x } dx = 1$ — ①	31	$A = \begin{bmatrix} 0 & 3 \\ -2 & -1 \end{bmatrix}$ $(A)^{-1} = \frac{1}{6} \begin{bmatrix} -7 & -3 \\ 2 & 0 \end{bmatrix}$ — ① $B^{-1} = \frac{1}{2} \begin{bmatrix} -1 & 3 \\ 0 & -2 \end{bmatrix}$ $A^{-1} = \frac{1}{3} \begin{bmatrix} 4 & 3 \\ -1 & 0 \end{bmatrix}$ $B^{-1}A^{-1} = \frac{1}{6} \begin{bmatrix} -7 & -3 \\ 2 & 0 \end{bmatrix}$ — ① P.T			
		32	$z = \cos 2\theta + i \sin 2\theta$ $\bar{z} = \cos 2\theta - i \sin 2\theta$ — ① $(\frac{1+i}{1-i})^{30} = (2)^{30} = \cos 60\theta + i \sin 60\theta$ — ②			

(33) $\theta = \sin^{-1} x \quad \text{--- (1)}$

$\theta = \cos^{-1} \left(\frac{\sqrt{1-x^2}}{x} \right) \quad \text{--- (1)}$

P.T --- (1)

(34) $\vec{t} = \vec{r} \times \vec{F} \quad \text{--- (1)}$

$\vec{t} = 3\hat{i} - 11\hat{j} - 7\hat{k} \quad \text{--- (1)}$

DC = $\frac{3}{\sqrt{179}}, \frac{-11}{\sqrt{179}}, \frac{-7}{\sqrt{179}} \quad \text{--- (1)}$

(35) $f(x) = \log(1+x) \quad f(0) = 0$
 $f'(x) = \frac{1}{1+x} \quad f'(0) = 1$
 $f(x) = \frac{-1}{(1+x)^2} \quad f'(0) = -1$
 $f''(x) = \frac{2}{(1+x)^3} \quad f''(0) = 2$ --- (2)

$\log(1+x) = x - \frac{x^2}{2} + \frac{x^3}{3} - \frac{x^4}{4} + \dots \quad \text{--- (1)}$

(36) $T = 2\pi \sqrt{\frac{l}{g}} \quad \frac{dT}{T} \times 100 = 2\% \quad \text{--- (1)}$

$\log T = \log \frac{2\pi}{\sqrt{g}} + \frac{1}{2} \log l \quad \text{--- (1)}$

$T = 1\% \quad \text{--- (1)}$

(37) $\frac{dy}{dx} = e^x \cdot e^y \neq 2e^y$

$e^{-y} dy = (e^x + nx) dx \quad \text{--- (1)}$

$e^x + e^{-y} = \frac{x^2}{2} + c \quad \text{--- (2)}$

(38) $\sum f(x) = 1 \quad k = 8 \quad \text{--- (2)}$

$P(x \geq 1) = \frac{7}{8} \quad \text{--- (1)}$

(39)

P	Q	$\neg P$	$P \rightarrow Q$	$\neg(P \vee Q)$
T	T	F	T	T
T	F	F	F	F
F	T	T	T	T
F	F	T	T	T

P.T

(40) $\int_{-\frac{1}{\sqrt{2}}}^x \frac{1}{\sqrt{1-t^2}} dt = \frac{\pi}{2}$

$\left[\sin^{-1} \left(\frac{t}{1} \right) \right]_{-\frac{1}{\sqrt{2}}}^x = \frac{\pi}{2}$

$\sin^{-1} x - \sin^{-1} \left(\frac{-1}{\sqrt{2}} \right) = \frac{\pi}{2}$

$\sin^{-1} x - \sin^{-1} \left(-\sin \frac{\pi}{4} \right) = \frac{\pi}{2}$

$\sin^{-1} x - \sin^{-1} \left(\sin -\frac{\pi}{4} \right) = \frac{\pi}{2}$

$\sin^{-1} x + \frac{\pi}{4} = \frac{\pi}{2}$

$\sin^{-1} x = \frac{\pi}{2} - \frac{\pi}{4}$

$\sin^{-1} x = \frac{2\pi - \pi}{4}$

$\sin^{-1} x = \frac{\pi}{4}$

$x = \sin \left(\frac{\pi}{4} \right)$

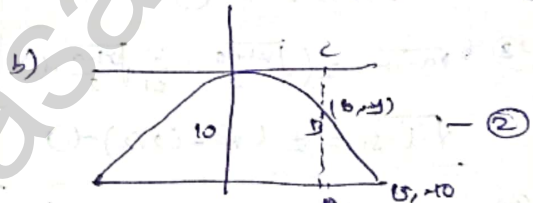
$x = \frac{1}{\sqrt{2}}$

(41) a) $\begin{bmatrix} 2 & 3 & 5 & 9 \\ 0 & -15 & -45 & -47 \\ 0 & 0 & \lambda-5 & \mu-9 \end{bmatrix} \quad \text{--- (2)}$

(i) no solution $\lambda = 5, \mu \neq 9 \quad \text{--- (1)}$

(ii) unique solution $\lambda \neq 5, \mu \in \mathbb{R} \quad \text{--- (1)}$

(iii) infinite solution $\lambda = 5, \mu = 9 \quad \text{--- (1)}$

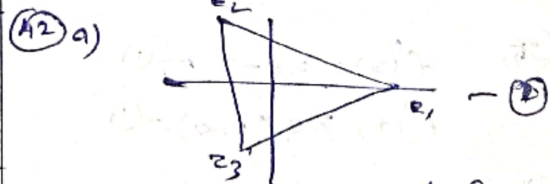


$x^2 = -49y \quad \text{--- (1)}$

DE = 11.6

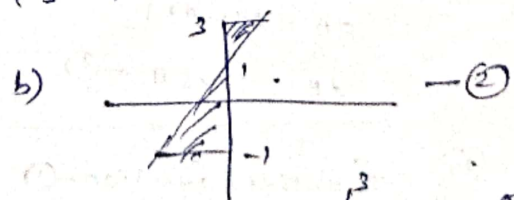
AC = AB + BC

AB = 10 - 1.6 = 8.4 --- (2)



$|z_1 - z_2| = \sqrt{3} \quad |z_2 - z_3| = \sqrt{3} \quad \text{--- (1)}$

$|z_3 - z_1| = \sqrt{3}$



P.T = $\int_{-1}^1 (-x) dx + \int_1^3 x dx \quad \text{--- (1)}$

= 2 --- (2)

(43) a) u is not homogeneous - (1)

$$f(x) = \frac{x+y}{\sqrt{x+y}} = \sin u \quad (1)$$

$$\text{degree} = \frac{1}{2} \quad (1)$$

$$x \frac{d(\sin u)}{dx} + y \frac{d(\sin u)}{dy} = \frac{1}{2} \sin u \quad (2)$$

$$\cos u \cdot x \frac{du}{dx} + \cos u \cdot y \frac{du}{dy} = \frac{1}{2} \sin u \quad (2)$$

$$x \frac{du}{dx} + y \frac{du}{dy} = \frac{1}{2} \tan u$$

$$b) \int_0^{\pi} f(x) \cdot dx = 1 \quad (1)$$

$$k = \frac{1}{4}$$

Distribution function

$$F(x) = \begin{cases} 0 & x < 1 \\ \frac{x-1}{4} & 1 \leq x \leq 5 \\ 1 & x \geq 5 \end{cases} \quad (3)$$

$$(ii) P(2 < x < 4) = \frac{1}{2} \quad (1)$$

(44) a) $\alpha = \tan^{-1}(\frac{1}{2})$ $\beta = \cos^{-1}(\frac{4}{5})$

$\alpha = \sin^{-1}(\frac{1}{\sqrt{5}}$ $\beta = \sin^{-1}(\frac{3}{5})$

$$= \sin(\alpha + \beta)$$

$$= \sin(\sin^{-1}(\frac{1}{\sqrt{5}}) + \sin^{-1}(\frac{3}{5})) \quad (2)$$

$$= \sin(\sin^{-1}(\frac{-2}{5\sqrt{5}})) \quad (2)$$

$$= \frac{-2}{5\sqrt{5}} \quad (1)$$

b) Vector equation:

$$\vec{r} = \vec{a} + s(\vec{b}-\vec{a}) + t\vec{c}$$

$$= (-\hat{i} + 2\hat{j}) + s(3\hat{i} - \hat{j}) + t(\hat{i} + \hat{j} - 2\hat{k}) \quad (1)$$

non-parametric form:

$$(\vec{r}-\vec{a}) \cdot (\vec{b}-\vec{a}) \times \vec{c} = 0$$

$$\vec{r} \cdot (\hat{i} + 2\hat{j} + 3\hat{k}) = 3 \quad (2)$$

Cartesian form:

$$x + 2y + 3z = 3 \quad (3)$$

$$\vec{b} \times \vec{c} \times \vec{c} = \hat{i} + 2\hat{j} + 3\hat{k}$$

(45) a) $\vec{a} \times \vec{b} = 4\hat{i} + 4\hat{j}$

$$\vec{c} \times \vec{d} = 8\hat{i} + 2\hat{j} + 6\hat{k} \quad (2)$$

$$(\vec{a} \times \vec{b}) \cdot (\vec{c} \times \vec{d}) = -24\hat{i} + 24\hat{j} - 40\hat{k}$$

$$(\vec{a} \cdot \vec{b}) \cdot \vec{d} = 24 \quad (\vec{a} \cdot \vec{b} \cdot \vec{c}) = 12 \quad (3)$$

$$(\vec{a} \cdot \vec{b} \cdot \vec{d}) \cdot \vec{c} = (\vec{a} \cdot \vec{b} \cdot \vec{c}) \cdot \vec{d} = -24\hat{i} + 24\hat{j} - 40\hat{k}$$

b) $\frac{dp}{dt} \propto p$ $k = 0.05$

$$p = ce^{kt} \quad (2)$$

$$P = 1000 \quad t = 0$$

$$c = 10000$$

$$P = 10000 e^{kt} \quad (1)$$

$$t = \frac{3}{2} \text{ year} \quad P = ?$$

$$P = 10000 e^{0.075} \quad (2)$$

(46) a) $f(x) = 4x^3 + 3x^2 - 6x + 1$

$$f'(x) = 12x^2 + 6x - 6$$

$$f''(x) = 24x + 6$$

Critical point $f'(x) = 0$ $x = \frac{1}{2}, -1$

$$-\infty \quad -1 \quad \frac{1}{2} \quad \infty$$

$-\infty, -1$	$-$	\uparrow	local maxima (-1/6)
$-1, \frac{1}{2}$	$+$	\downarrow	
$\frac{1}{2}, \infty$	$+$	\uparrow	

$$f''(x) = 0 \quad x = -\frac{1}{4} \quad \text{minima } (\frac{1}{2}, -\frac{3}{4})$$

$$-\infty \quad -\frac{1}{4} \quad \infty$$

$-\infty, -\frac{1}{4}$	$-$	\downarrow
$-\frac{1}{4}, \infty$	$+$	\uparrow

$$\text{at } x = -\frac{1}{4} \quad \text{Point inflection } (\frac{1}{4}, \frac{21}{8})$$

b)

	0	1	2	3	4
0	0	1	2	3	4
1	1	2	3	4	0
2	2	3	4	0	1
3	3	4	0	1	2
4	4	0	1	2	3

all properties

47) The equation of a circle
 $x^2 + y^2 + 2gx + 2fy + c = 0$

at (1,1) $2g + 2f + c = -2$ — (1)

at (2,4) $4g + 16f + c = -20$ — (2)

at (5,3) $10g + 6f + c = -34$ — (3)

(1) - (2) $-2g - 14f = 18$

(2) - (3) $-6g + 10f = 14$

$g + 7f = -9$ — I

$f = -\frac{10}{13}$ $g = -\frac{47}{13}$

$c = \frac{88}{13}$

$x^2 + y^2 + 2\left(-\frac{47}{13}\right)x + 2\left(-\frac{10}{13}\right)y + \frac{88}{13} = 0$

$\times 13 \Rightarrow 13x^2 + 13y^2 - 94x - 20y + 88 = 0$

48) $y = x^3$ — (1), $x^2 + 6y = 7$ — (2)

$x^2 + 6x^3 = 7$

$x^2(1 + 6x) = 7$

$x^2 = 7$

$x = \pm\sqrt{7}$

at $x = \sqrt{7}$:

$y = x^3$

$y = (\sqrt{7})^3$

$y = 7\sqrt{7}$

$(\sqrt{7}, 7\sqrt{7})$ point

at $x = -\sqrt{7}$

$y = (-\sqrt{7})^3$

$y = -7\sqrt{7}$

$(-\sqrt{7}, -7\sqrt{7})$ point

$1 + 6x = 7$

$6x = 7 - 1$

$6x = 6$

$x = 1$

at $y = x^3$

at $x = 1$ $y = 1^3$

$y = 1$

$(1, 1)$ point

$y = x^3$

$\frac{dy}{dx} = 3x^2$

at (1,1) $m_1 = 3$

$x^2 + 6y = 7$

$2x + 6\frac{dy}{dx} = 0$

$6\frac{dy}{dx} = -2x$

$\frac{dy}{dx} = -\frac{x}{3}$

$\frac{dy}{dx} = -\frac{x}{3}$

at (1,1) $m_2 = -\frac{1}{3}$

$m_1 \times m_2 = 3 \times -\frac{1}{3}$

$= -1$

Given the two curves are
 orthogonally.

