

Vellore District

SECOND REVISION TEST - 2025

Standard XII

Reg.No.

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MATHEMATICS

Time : 3.00 hrs

Part - I

Marks : 90
20 x 1 = 20

I. Choose the correct answer:

1. If $A = \begin{bmatrix} 2 & 0 \\ 1 & 5 \end{bmatrix}$ and $B = \begin{bmatrix} 1 & 4 \\ 2 & 0 \end{bmatrix}$ then $|\text{adj } AB| =$
 a) -40 b) -80 c) -60 d) -20
2. If $A = \begin{bmatrix} 3 & 1 & -1 \\ 2 & -2 & 0 \\ 1 & 2 & -1 \end{bmatrix}$ and $A^{-1} = \begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{bmatrix}$ then the value of a_{23} is
 a) 0 b) -2 c) -3 d) -1
3. The conjugate of a complex number is $\frac{1}{i-2}$. Then the complex number is
 a) $\frac{1}{i+2}$ b) $\frac{-1}{i+2}$ c) $\frac{-1}{i-2}$ d) $\frac{1}{i-2}$
4. z_1, z_2, z_3 are complex numbers such that $z_1 + z_2 + z_3 = 0$ and $|z_1| = |z_2| = |z_3| = 1$ then $z_1^2 + z_2^2 + z_3^2$ is
 a) 3 b) 2 c) 1 d) 0
5. If α, β and γ are the zeros of $x^3 + px^2 + qx + r$, then $\sum \frac{1}{\alpha}$ is
 a) $-\frac{q}{r}$ b) $-\frac{p}{r}$ c) $\frac{q}{r}$ d) $-\frac{p}{q}$
6. $\sin^{-1}\left(\tan \frac{\pi}{4}\right) - \sin^{-1}\left(\sqrt{\frac{3}{x}}\right) = \frac{\pi}{6}$, then x is a root of the equation
 a) $x^2 - x - 6 = 0$ b) $x^2 - x - 12 = 0$
 c) $x^2 + x - 12 = 0$ d) $x^2 + x - 6 = 0$
7. The circle $x^2 + y^2 = 4x + 8y + 5$ intersects the line $3x - 4y = m$ at two distinct points if
 a) $15 < m < 65$ b) $35 < m < 85$ c) $-85 < m < -35$ d) $-35 < m < 15$
8. If $P(x, y)$ be any point on $16x^2 + 25y^2 = 400$ with foci $F_1(3,0)$ and $F_2(-3,0)$ then $PF_1 + PF_2$ is
 a) 8 b) 6 c) 10 d) 12
9. If $|\vec{a}, \vec{b}, \vec{c}| = 1$, then the value of $\frac{\vec{a} \cdot (\vec{b} \times \vec{c})}{(\vec{c} \times \vec{a}) \cdot \vec{b}} + \frac{\vec{b} \cdot (\vec{c} \times \vec{a})}{(\vec{a} \times \vec{b}) \cdot \vec{c}} + \frac{\vec{c} \cdot (\vec{a} \times \vec{b})}{(\vec{c} \times \vec{b}) \cdot \vec{a}}$ is
 a) 1 b) -1 c) 2 d) 3
10. The angle between the lines $\frac{x-2}{3} = \frac{y+1}{-2}, z=2$ and $\frac{x-1}{1} = \frac{2y+3}{3} = \frac{z+5}{2}$ is
 a) $\frac{\pi}{6}$ b) $\frac{\pi}{4}$ c) $\frac{\pi}{3}$ d) $\frac{\pi}{2}$

11. The point on the curve $6y = x^3 + 2$ at which y-coordinate changes 8 times as fast as x-coordinate is
 a) (4,11) b) (4,-11) c) (-4,11) d) (-4,-11)
12. The maximum value of the function x^2e^{-2x} , $x > 0$ is
 a) $\frac{1}{e}$ b) $\frac{1}{2e}$ c) $\frac{1}{e^2}$ d) $\frac{1}{e^4}$
13. The approximate change in the volume V of a cube of side x metres caused by increasing the side by 1% is
 a) $0.3x dx m^3$ b) $0.03x m^3$ c) $0.03x^2 m^3$ d) $0.03x^3 m^3$
14. For any value of $n \in \mathbb{Z}$, $\int_0^{\pi} e^{\cos^2 x} \cos^3 [(2n+1)x] dx$ is
 a) $\frac{\pi}{2}$ b) π c) 0 d) 2
15. If $f(x) = \int_1^x \frac{e^{\sin u}}{u} du$, $x > 1$ and $\int_1^3 \frac{e^{\sin x^2}}{x} dx = \frac{1}{2}[f(a) - f(1)]$, then one of the possible value of a is
 a) 3 b) 6 c) 9 d) 5
16. The order and degree of the differential equation $\sqrt{\sin x} (dx + dy) = \sqrt{\cos x} (dx - dy)$ is
 a) 1, 2 b) 2, 2 c) 1, 1 d) 2, 1
17. The solution of the differential equation $\frac{dy}{dx} + \frac{1}{\sqrt{1-x^2}} = 0$ is
 a) $y + \sin^{-1}x = c$ b) $x + \sin^{-1}y = 0$ c) $y^2 + 2\sin^{-1}x = c$ d) $x^2 + 2\sin^{-1}y = 0$
18. A pair of dice numbered 1,2,3,4,5,6 of a six-sided die and 1,2,3,4 of a four-sided die is roed and the sum is determined. Let the random variable X denoted this sum. Then the number of elements in the inverse image of 7 is
 a) 1 b) 2 c) 3 d) 4
19. If $f(x) = \begin{cases} 2x & 0 \leq x \leq a \\ 0 & \text{otherwise} \end{cases}$ is a probability density function of a random variable, then the value of a is
 a) 1 b) 2 c) 3 d) 4
20. Which one of the following is incorrect? For any two propositions p and q, we have
 a) $\neg(p \vee q) \equiv \neg p \wedge \neg q$ b) $\neg(p \wedge q) \equiv \neg p \vee \neg q$
 c) $\neg(p \vee q) \equiv \neg p \vee \neg q$ d) $\neg(\neg p) \equiv p$

Part - II

II. Answer any 7 questions. (Q.No.30 is compulsory)

7 x 2 = 14

(21) If $z = (2 + 3i)(1 - i)$, then prove that $z^{-1} = \frac{5}{26} - i\frac{1}{26}$

(22) Find a polynomial equation of minimum degree with rational coefficients, having $2 - \sqrt{3}$ as a root.

- (23) Find the principal value of $\tan^{-1}(\sqrt{3})$
- (24) If $y = 4x + c$ is a tangent to the circle $x^2 + y^2 = 9$, find c
25. Show that the three vectors $2\hat{i} + 3\hat{j} + \hat{k}$, $\hat{i} - 2\hat{j} + 2\hat{k}$ and $3\hat{i} + \hat{j} + 3\hat{k}$ are coplanar.
- (26) Find df for $f(x) = x^2 + 3x$ and evaluate it for $x = 2$ and $dx = 0.1$
- (27) Prove that $\begin{bmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{bmatrix}$ is orthogonal
28. Show that the solution of $\frac{dy}{dx} = \sqrt{\frac{1-y^2}{1-x^2}}$ is $\sin^{-1}y = \sin^{-1}x + C$ or $\sin^{-1}x = \sin^{-1}y + C$
- (29) Find the points on the curve $y = x^3 - 3x^2 + x - 2$ at which the tangent is parallel to the line $y = x$
30. X is the number of tails occurred when three fair coins are tossed simultaneously. Find the values of the random variable X and number of points in its reverse images.

Part - III

III. Answer any 7 questions. (Q.No.40 is compulsory)

7 x 3 = 21

- (31) Show that the rank of the matrix $\begin{bmatrix} 0 & 1 & 2 & 1 \\ 0 & 2 & 4 & 3 \\ 8 & 1 & 0 & 2 \end{bmatrix}$ is 3
- (32) Which one of the points $10 - 8i$, $11 + 6i$ is closest to $1 + i$
- (33) If the sides of a cubic box are increased by 1, 2, 3 units respectively to form a cuboid, then the volume is increased by 52 cubic units. Show that the volume of the cuboid is 60 cubic units.
- (34) For what value of x , the inequality $\frac{\pi}{2} < \cos^{-1}(3x - 1) < \pi$ holds?
- (35) The maximum and minimum distances of the Earth from the Sun respectively are 152×10^6 km and 94.5×10^6 km. The Sun is at one focus of the elliptical orbit. Find the distance from the Sun to the other focus.
36. An egg of a particular bird is spherical in shape. If the radius to the inside of the shell is 4 mm and radius to the outside of the shell is 4.2 mm, prove that the approximate volume of the shell is 12.8π mm³.
37. Show that $\int_0^{\pi/3} \frac{\sec x \tan x}{1 + \sec^2 x} dx = \tan^{-1}(2) - \frac{\pi}{4}$
38. Two balls are chosen randomly from an urn containing 6 white and 4 black balls. Suppose that we win ₹30 for each black ball selected and the loss ₹20 for each white ball selected. If X denotes the winning amount, then find the values of X and number of points in its inverse images.
- (39) Show that $p \rightarrow q$ and $q \rightarrow p$ are not equivalent.
40. Solve : $x \cos y dy = e^x(x \log x + 1) dx$

Part - IV

IV. Answer all the questions.

7 x 5 = 35

41. (a) Solve the system of equations $x - y + 2z = 2$, $2x + y + 4z = 7$, $4x - y + z = 4$ by Cramer's rule. (OR)
- b) Show that $\int_0^1 \sqrt{\frac{1-x}{1+x}} dx = \frac{\pi}{2} - 1$.
42. (a) Prove that the local minimum values for the function $f(x) = 4x^6 - 6x^4$ attain at -1 and 1 . (OR)
- b) Show that the locus of $z = x + iy$ if $|z + i| = |z - 1|$ is $x + y = 0$
43. (a) Using vector method, prove that $\cos(\alpha - \beta) = \cos\alpha \cos\beta + \sin\alpha \sin\beta$ (OR)
- b) Solve: $(1 + x + xy^2) \frac{dy}{dx} + (y + y^3) = 0$
44. (a) Suppose the amount of milk sold daily at a milk booth is distributed with a minimum of 200 litres and a maximum of 600 litres with probability density function of random variable X is $f(x) = \begin{cases} k & 200 \leq x \leq 600 \\ 0 & \text{otherwise} \end{cases}$ Find (i) the value of k (ii) the distribution function (iii) the probability that daily sales will fall between 300 litres and 500 litres. (OR)
- b) Find the vector equation (any form) or Cartesian equation of a plane passing through the points $(2, 2, 1)$, $(9, 3, 6)$ and perpendicular to the plane $2x + 6y + 6z = 9$
45. a) Show that the area of the region bounded by $3x - 2y = 0$, $x = -3$ and $x = 1$ is $\frac{15}{2}$. (OR)
- b) On lighting a rocket cracker it gets projected in a parabolic path and reaches a maximum height of 4 m when it is 6 m away from the point of projection. Finally it reaches the ground 12 m away from the starting point. Show that the angle of projection is $\tan^{-1}\left(\frac{4}{3}\right)$
46. a) If $\cos^{-1}x + \cos^{-1}y + \cos^{-1}z = \pi$ and $0 < x, y, z < 1$, show that $x^2 + y^2 + z^2 + 2xyz = 1$ (OR)
- b) A boy is walking along the path $y = ax^2 + bx + c$ through the points $(-6, 8)$, $(-2, -12)$ and $(3, 8)$. He wants to meet his friend at $P(7, 60)$. Will he meet his friend? (Use Gaussian Elimination method)
47. a) Prove that the ellipse $x^2 + 4y^2 = 8$ and the hyperbola $x^2 - 2y^2 = 4$ intersect orthogonally. (OR)
- b) Identify the type of conic and find centre, foci and vertices of $18x^2 + 12y^2 - 144x + 48y + 120 = 0$
