

RKR EDUCATIONAL INSTITUTIONS, UDUMALPET.

NESA MATHS-9750351441

XII STANDARD. (MAR-2025)

MATHEMATICS KEY.

PART-A (\*-creative)

S. NO.	ANSWER & OPTION		S. NO.	ANSWER & OPTION	
	A-TYPE	B-TYPE		A-TYPE	B-TYPE
1.	a) N	b) $\frac{1}{\sqrt{2}}$	11.	* b) $\pm \frac{1}{\sqrt{2}}(1+i)$	c) $\frac{\pi a^3}{6}$
2.	d) 2	a) $\pi$	12.	b) $1+i$	* a) 1, 2
3.	* d) $\frac{1}{5}$	d) $2 \times 4$	13.	d) 0.25	b) $\frac{\pi}{6}$
4.	d) 2.5	a) N	14.	c) $\frac{\pi}{2}$	a) 19
5.	* a) 1, 2	* d) $\frac{1}{5}$	15.	a) (1,0)	b) $1+i$
6.	a) 19	a) (1,0)	16.	b) $\frac{\pi}{6}$	c) $\frac{\pi}{2}$
7.	b) $y=x^2+2$	d) 2.5	17.	c) $\frac{\pi a^3}{6}$	* b) $\pm \frac{1}{\sqrt{2}}(1+i)$
8.	b) [1,2]	* a) $\frac{f'(x)}{f(x)}$	18.	b) $\frac{1}{\sqrt{2}}$	b) $y=x^2+2$
9.	d) $2 \times 4$	b) [1,2]	19.	a) $\pi$	d) 0.25
10.	b) 2	d) 2	20.	* b) $\frac{f'(x)}{f(x)}$	b) 2

PART-B

21.	$ adj A  = 9 \quad \textcircled{1m}$ $A^{-1} = \frac{1}{ adj A } (adj A)$ $A^{-1} = \frac{1}{3} \begin{bmatrix} -1 & 2 & 2 \\ 2 & 2 & 1 \end{bmatrix} \quad \textcircled{1m}$
22.	$Re(\frac{1}{z}) = Re(\frac{1}{x+iy} \times \frac{x-iy}{x-iy}) \quad \textcircled{1m}$ $= \frac{x}{x^2+y^2} \quad \textcircled{1m}$
23.	$y = -\tan^{-1}(-\sqrt{3}) \quad \textcircled{1m}$ $\tan y = -\sqrt{3}$ $y = -\frac{\pi}{3} \in (-\frac{\pi}{2}, \frac{\pi}{2}) \quad \textcircled{1m}$

24.  $y = 4x + c \Rightarrow m = 4$   
 $x^2 + y^2 = 9 \Rightarrow a^2 = 9 \quad \textcircled{1m}$   
 $c^2 = a^2(1+m^2)$   
 $c = \pm 3\sqrt{17} \quad \textcircled{1m}$

25.  $x+5 \overline{) x^2 - 6x + 7} \quad \textcircled{1m}$   
 $\underline{x^2 + 5x}$   
 $-11x + 7$   
 $\underline{-11x - 55}$   
 $62$   
 Slant asymptote is  $y = x - 11 \quad \textcircled{1m}$

26.  $F(\lambda x, \lambda y) = \frac{\lambda^2}{\lambda} (F(x, y))$   
 $= \lambda^1 (F(x, y)) \quad \textcircled{1m}$   
 Degree  $[n=1] \quad \textcircled{1m}$

27.  $\frac{dy}{\sqrt{1-y^2}} = \frac{dx}{\sqrt{1-x^2}} \quad \textcircled{1m}$   
 $\sin^{-1} y = \sin^{-1} x + c \quad \textcircled{1m}$

28.  $f(x)$  is p.d.f then  $\int_{-\infty}^{\infty} f(x) dx = 1$   
 $\int_0^4 c x^2 dx = 1 \quad \textcircled{1m}$   
 $c (\frac{x^3}{3})_0^4 = 1$   
 $c = \frac{1}{21} \quad \textcircled{1m}$

29. Let  $\alpha = -2+i$  &  $\beta = -2-i \quad \textcircled{1m}$   
 $x^2 - x(\alpha + \beta) + \alpha\beta = 0$   
 $x^2 + 4x + 5 = 0 \quad \textcircled{1m}$

30. If  $f(2a-x) = f(x)$  then  
 $\int_0^{2a} f(x) dx = 2 \int_0^a f(x) dx$   
 $\sin(\pi-x) = \sin x \quad \textcircled{1m}$   
 $\int_0^{\pi} f(x) dx = 2 \int_0^{\frac{\pi}{2}} f(x) dx \quad \textcircled{1m}$

31.  $|A| = -1$  ①m  
 $\text{adj} A = \begin{bmatrix} 2 & -5 \\ 1 & -2 \end{bmatrix}$   
 $A^{-1} = \frac{1}{-1} \begin{bmatrix} 2 & -5 \\ 1 & -2 \end{bmatrix}$  ①m  
 $X = A^{-1}B$   
 $\begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} -11 \\ 4 \end{bmatrix} \therefore x = -11, y = 4$  ①m

32.  $|z_1| = 2$   $|z_2| = |6+8i| = 10$  ①m  
 $||z_1| - |z_2|| \leq |z_1 + z_2| \leq |z_1| + |z_2|$   
 $|2 - 10| \leq |z + 6 + 8i| \leq 2 + 10$  ①m  
 $8 \leq |z + 6 + 8i| \leq 12$  ①m

34.  $\tan^{-1} \frac{2}{11} + \tan^{-1} \frac{7}{24}$   
 $= \tan^{-1} \left[ \frac{\frac{2}{11} + \frac{7}{24}}{1 - (\frac{2}{11} \times \frac{7}{24})} \right]$  ①m  
 $= \tan^{-1} \left( \frac{125}{250} \right)$  ①m  
 $= \tan^{-1} \frac{1}{2}$  ①m

33.  $\begin{vmatrix} 7 & -43 & -43 & 7 \\ 0 & -7 & 50 & -7 \\ 7 & -50 & 7 & 0 \end{vmatrix}$  ①m  
 $7x^2 - 50x + 7 = 0$   
 $x = 7, \frac{1}{7}$  ①m  
 $\therefore x = -1, 7, \frac{1}{7}$  ①m

35.  $[\vec{a} + \vec{c}, \vec{a} + \vec{b}, \vec{a} + \vec{b} + \vec{c}]$   
 $= \begin{vmatrix} 1 & 0 & 1 \\ 1 & 1 & 0 \\ 1 & 1 & 1 \end{vmatrix} [\vec{a} \ \vec{b} \ \vec{c}]$  ①m  
 $= (1(1-0) - 0 + 1(1-1)) [\vec{a} \ \vec{b} \ \vec{c}]$  ①m  
 $= [\vec{a} \ \vec{b} \ \vec{c}]$  ①m

36.  $u = x^2y + 3xy^4$   
 $x = e^t, y = \sin t$   
 $u = e^{2t} \sin t + 3e^t \sin^4 t$  ①m  
 $\frac{du}{dt} = 2e^{2t} \sin t + e^{2t} \cos t$  ①m  
 $+ 3[e^t + \sin^3 t \cos t + \sin^4 t \cdot e^t]$   
 $= 2e^{2t} \sin t + e^{2t} \cos t + 3e^t \sin^4 t$   
 $+ 12e^t \sin^3 t \cos t$  ①m

37.  $I = \int_0^{\frac{\pi}{2}} \frac{dx}{4+5\cos^2 x} = \int_0^{\frac{\pi}{2}} \frac{\sec^2 x dx}{\sec^2 x + 5}$  ①m  
 Let  $t = \tan x \Rightarrow dt = \sec^2 x dx$   
 $I = \int_0^{\infty} \frac{dt}{6+t^2} = \frac{\pi}{2\sqrt{6}}$  ①m

38.  $E(x) = 200 \times \frac{1}{600} + (100 \times \frac{4}{600})$   
 $+ 50 \times (\frac{6}{600}) + 0$   
 $= 1.5$  ②m  
 Loss  $E(x) = -2 + 1.5$   
 $= -0.5$  ①m

39\*  $f(x) = x^3 + 2x + 1$   
 $f(x) = f(a) + f'(a)(x-a)$   
 $+ \frac{f''(a)}{2!}(x-a)^2 + \dots$  ①m  
 $x^2 + 2x + 1 = 13 + 14(x-2) + 6(x-2)^2$   
 $+ \dots$  ②m

40\*  $\frac{3}{2} * m = \frac{87}{10}$   
 $\frac{3}{2} + m - (\frac{3}{2} * m) + 7 = \frac{87}{10}$  ①m  
 $-m = \frac{4}{10}$  ①m  
 $m = -\frac{2}{5}$  ①m

PART-D

41. a)

$$\Delta = 6 \text{ ①m}$$

$$\Delta_1 = 12 \text{ ①m}$$

$$\Delta_2 = -6 \text{ ①m}$$

$$\Delta_3 = 24 \text{ ①m}$$

$$x_1 = \frac{\Delta_1}{\Delta} = 2$$

$$y_1 = \frac{\Delta_2}{\Delta} = -1$$

$$z_1 = \frac{\Delta_3}{\Delta} = 4$$

$$x_1 = 2, y_1 = -1, z_1 = 4 \text{ ①m}$$

41. b)

$$m = \frac{dy}{dx} = \frac{2 \cos t}{-7 \sin t} \text{ ①m}$$

Tangent:  $-y - y_1 = m(x - x_1) \text{ ①m}$

$$(y - 2 \sin t) = \frac{-2 \cos t}{7 \sin t} (x - 7 \cos t)$$

$$2x \cos t + 7y \sin t = 14 \text{ ①m}$$

Normal:  $-y - y_1 = -\frac{1}{m}(x - x_1) \text{ ①m}$

$$7x \sin t - 2y \cos t = 45 \sin t \cos t \text{ ①m}$$

42. a)

$$(z-1)^3 = -8 \text{ ①m}$$

$$(z-1)^3 = (-2)^3 (1)^3 = (-2)^3 (1)$$

$$z-1 = (-2)(1)^{\frac{1}{3}}$$

$$1-z = 2(1)^{\frac{1}{3}} \text{ ②m}$$

$$1-z = 2(1, \omega, \omega^2) \text{ ①m}$$

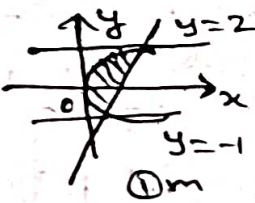
$$z = 1-2, 1-2\omega, 1-2\omega^2$$

$$z = -1, 1-2\omega, 1-2\omega^2 \text{ ①m}$$

42. b)

$$y^2 = x, y = x - 2$$

$$x - y = y^2 - 2$$

$$\Rightarrow y = 2, -1 \text{ ①m}$$


$$A = \int_{-1}^2 (x_1 - x_2) dy \text{ ①m}^*$$

$$= \int_{-1}^2 (y+2 - y^2) dy \text{ ①m}$$

$$= \frac{9}{2} \text{ ①m}$$

43. a)

$$\frac{1}{3} \begin{vmatrix} 6 & -5 & -38 & -5 & 6 \\ 0 & 2 & -1 & -13 & -6 \\ 6 & -3 & -39 & -18 & 0 \\ 0 & 18 & 45 & 18 & \end{vmatrix}$$

$$3 \begin{vmatrix} 6 & -3 & -39 & -18 & 0 \\ 0 & 18 & 45 & 18 & \end{vmatrix}$$

$$-2 \begin{vmatrix} 6 & 15 & 6 & 0 \\ 0 & -12 & -6 & \end{vmatrix} \text{ ④m}$$

$$-\frac{1}{2} \begin{vmatrix} 6 & 3 & 0 \\ 0 & -3 & \end{vmatrix} \text{ ①m}$$

The roots are  $3, \frac{1}{3}, -2, -\frac{1}{2}$

43. b)

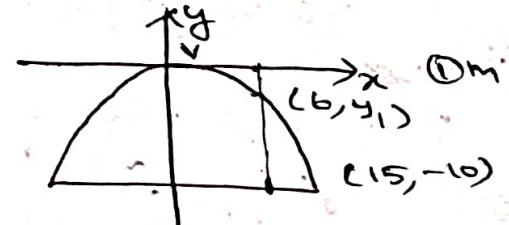
$$\frac{dy}{dx} = \frac{3y}{2x} + \frac{x}{2y} \text{ ①m}$$

put  $y = vx$  &  $\frac{dy}{dx} = vx \frac{dv}{dx} \text{ ①m}$

$$\int \frac{2v}{v^2-1} dv = \int \frac{dx}{x} \text{ ②m}$$

$$y^2 - x^2 = cx^3 \text{ ①m}$$

44. a)



The parabola is open downward.

$$x^2 = -4ay \text{ ①m}$$

$$(x, y) = (15, -10)$$

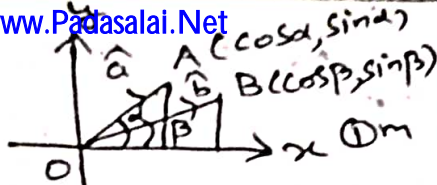
$$4a = \frac{225}{10} \text{ ①m}$$

$$x^2 = -\frac{225}{10} y$$

$$(x, y) = (6, y_1) \Rightarrow y_1 = -1.6 \text{ ①m}$$

Height =  $10 - 1.6 = 8.4 \text{m ①m}$

44  
b)



$$\hat{a} = \cos\alpha \hat{i} + \sin\alpha \hat{j} \quad \text{①m}$$

$$\hat{b} = \cos\beta \hat{i} + \sin\beta \hat{j} \quad \text{①m}$$

$$\hat{a} \cdot \hat{b} = (\hat{a} | \hat{b}) \cos(\alpha - \beta) = \cos(\alpha - \beta) \quad \text{①m}$$

$$\hat{a} \cdot \hat{b} = \cos\alpha \cos\beta + \sin\alpha \sin\beta \quad \text{①m}$$

$$\cos(\alpha - \beta) = \cos\alpha \cos\beta + \sin\alpha \sin\beta \quad \text{①m}$$

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$$\vec{r} \cdot (-9\hat{i} + 8\hat{j} - \hat{k}) = 13 \quad \text{①m}$$

$$9x - 8y + z + 13 = 0 \quad \text{①m}$$

45  
a)

$$\frac{(x-h)^2}{a^2} + \frac{(y-k)^2}{b^2} = 1 \quad \text{①m}^*$$

c (0, 1)

$$2ae = 4 \Rightarrow ae = 2 \quad \text{①m}$$

$$\frac{2b^2}{a} = 6 \Rightarrow b^2 = 3a \quad \text{①m}$$

$$b^2 = a^2(1 - e^2) = a^2 - (ae)^2 \quad \text{①m}$$

$$3a = a^2 - 4 \Rightarrow a^2 - 3a - 4 = 0$$

$$a = 4 \quad | \quad a = -1 \text{ (not possible)}$$

$$a^2 = 16 \text{ \& } b^2 = 12 \quad \text{①m}$$

$$\frac{(x-0)^2}{16} + \frac{(y-1)^2}{12} = 1 \quad \text{①m}$$

47  
a)

Diagram ①m

$$V = \pi r^2 h = \pi r^2 (a-r) \left(\frac{b}{a}\right)$$

$$V = \frac{\pi b}{a} (ar^2 - r^3) \quad \text{①m}$$

$$V' = \frac{\pi b}{a} (2ar - 3r^2)$$

$$V' = 0 \Rightarrow r = \frac{2a}{3} \quad \text{①m}$$

$$V'' = \frac{\pi b}{a} (2a - 6r) \quad \text{①m}$$

$V''$  at  $r = \frac{2a}{3} < 0$ , volume is maximum.

$$V = \frac{\pi b}{a} \frac{4a^2}{9} \left(a - \frac{2a}{3}\right) = \frac{4}{9} \text{ (volume of cone)} \quad \text{①m}$$

45  
a)

x → ships arrive safely.

$$p = \frac{8}{9}, \quad q = \frac{1}{9} \quad \text{①m}$$

(i)  $n = 6, x = 3$

$$P(X=x) = {}^n C_x p^x q^{n-x}$$

$$P(X=3) = {}^6 C_3 \left(\frac{8}{9}\right)^3 \left(\frac{1}{9}\right)^3$$

$$= {}^6 C_3 \left(\frac{8^3}{9^6}\right) \quad \text{②}^*$$

(ii)  $n = 4, x = 0$

$$P(X=x) = {}^n C_x p^x q^{n-x}$$

$$P(X=0) = {}^4 C_0 \left(\frac{8}{9}\right)^0 \left(\frac{1}{9}\right)^4$$

$$= \left(\frac{1}{9}\right)^4 \quad \text{②}^*$$

46  
b)

A - population at time t.

$$\frac{dA}{dt} \propto A \Rightarrow \frac{dA}{dt} = kA$$

$$A = ce^{kt} \rightarrow \text{①} \quad \text{①m}$$

(i)  $t = 0, A = A_0$

$$c = A_0, A = A_0 e^{kt} \quad \text{①m}$$

(ii)  $t = 50, A = 2A_0$

$$2A_0 = A_0 e^{50k}$$

$$k = \frac{1}{50} \log 2 \quad \text{①m}$$

(iii)  $t = t_1, A = 3A_0$

$$t_1 = 50 \left(\frac{\log 3}{\log 2}\right) \quad \text{①m}$$

46  
a)

$$\vec{b} = 2\hat{i} + 3\hat{j} + 6\hat{k}; \vec{c} = \hat{i} + \hat{j} - \hat{k}$$

Point (0, 1, -5) ①m

$$(\vec{r} - \vec{a}) \cdot (\vec{b} \times \vec{c}) = 0 \quad \text{①m}^*$$

$$\vec{a} = \hat{j} - 5\hat{k}$$

$$\vec{b} \times \vec{c} = -9\hat{i} + 8\hat{j} - \hat{k} \quad \text{①m}$$

47  
b)

P	Q	r	$q \vee r$	$P \wedge (q \vee r)$	$P \wedge Q$	$P \wedge r$	$(P \wedge Q) \vee (P \wedge r)$
T	T	T	T	T	T	T	T
T	T	F	T	T	T	F	T
T	F	T	T	T	F	T	T
T	F	F	F	F	F	F	F
F	T	T	T	F	F	F	F
F	T	F	T	F	F	F	F
F	F	T	T	F	F	F	F
F	F	F	F	F	F	F	F

①m      ①m      ①m      ①m

$$\therefore P \wedge (q \vee r) \equiv (P \wedge Q) \vee (P \wedge r) \quad \text{①m}$$