

11th Physics - Unit 1 - One Marks Solutions

1. NATURE OF PHYSICAL WORLD AND MEASUREMENT

1. One of the combinations from the fundamental physical constants is $\frac{hc}{G}$. The unit of this expression is.

Solution

$$\frac{hc}{G} \Rightarrow \frac{\text{Applying SI units}}{[Nm\ s] [ms^{-1}]} \Rightarrow \frac{kg^2}{Nm^2 kg^2}$$

2. If the error in the measurement of radius is 2% then the error in the determination of volume of the sphere will be

Solution Volume of the sphere $V = \frac{4}{3} \pi r^3$

$$V \propto r^3$$

$$\frac{\Delta V}{V} \times 100 = 3 \frac{\Delta r}{r} \times 100$$

$$\frac{\Delta V}{V} \times 100 = 3 \times 2\%$$

$$= 6\%$$

3. If the length and time period of an oscillating pendulum have errors of 1% and 3% respectively then the error in measurement of acceleration due to gravity is

Soln $T = k \sqrt{\frac{l}{g}} \Rightarrow T^2 \propto \frac{l}{g} \Rightarrow g = \frac{l}{T^2}$

$$\frac{\Delta g}{g} \times 100 = \frac{\Delta l}{l} \times 100 + 2 \frac{\Delta T}{T} \times 100$$

$$\neq \text{W/A } 6\% = 1\% + [2 \times 3\%]$$

$$= 7\%$$

4) The length of a body is measured as 3.51 m, if the accuracy is 0.01 m, then the percentage error in the measurement is

$$\begin{aligned}\text{Soln} \quad \text{Percentage error} &= \frac{\Delta a_m}{a_m} \times 100\% \\ &= \frac{0.01}{3.51} \times 100\% \\ &= \underline{\underline{0.28\%}}\end{aligned}$$

5) Which of the following has highest no. of significant figures?

a) $0.007 \text{ m}^2 \Rightarrow$ significant 1

b) $2.64 \times 10^{24} \text{ kg} \Rightarrow$ significant 3

c) $0.0006032 \text{ m}^2 \Rightarrow$ significant 4

d) $6.3200 \text{ J} \Rightarrow$ significant 5

Soln: Correct Answer : d. 6.3200 J

6) If $\pi = 3.14$, then the value of π^2 is

$$\text{Soln} \therefore \pi^2 = 3.14 \times 3.14$$

$$\pi^2 = 9.8596$$

Here the least no. of significant digits in the measured values is three. Hence the resultant when rounded off to three significant digits.

$$\pi^2 = \underline{\underline{9.86}} \quad \pi^2 = \underline{\underline{9.86}}$$

7. Which of the following pairs of physical quantities have same dimension?

- [a] force and power $[MLT^{-2}]$ and $[ML^2T^{-3}]$
 [b] torque and energy $[ML^2T^{-2}]$ and $[ML^2T^{-2}]$
 [c] torque and power $[ML^2T^{-2}]$ and $[ML^2T^{-3}]$
 [d] force and torque $[MLT^{-2}]$ and $[ML^2T^{-2}]$

ANSWER : [b] Torque and energy

8. The dimensional formula of planck's constant h is

Soln: $E = h\nu \Rightarrow h = \frac{E}{\nu}$

Dimensions of Energy $[ML^2T^{-2}]$

Dimensions of frequency $[T^{-1}]$

$$h = \frac{[ML^2T^{-2}]}{[T^{-1}]} \Rightarrow h = [ML^2T^{-1}]$$

9. The velocity of a particle v at an instant t is given by $v = at + bt^2$. The dimensions of b is

Soln: $v = u + at$

Comparing both eq

$$at + bt^2 = u + at$$

$$bt^2 = u + at - at$$

$$bt^2 = u \Rightarrow b = ut^{-2}$$

Applying Dimension

$$b = [LT^{-1}][T^{-2}] = [LT^{-3}]$$

10. The dimensional formula for gravitational constant

G is

Soln: $F = G \frac{m_1 m_2}{d^2} \Rightarrow G = \frac{F \cdot d^2}{m_1 m_2}$

Applying Dimension,

$$G = \frac{[MLT^{-2}][L^2]}{[M^2]} \Rightarrow G = [M^{-1}L^3T^{-2}]$$

11. The density of a material in CGS system of units is $4g\text{ cm}^{-3}$. In a system of units in which unit of length is 10 cm and unit of mass is 100g, then the value of density of material will be

Soln: $\rho_1 [M_1^a L_1^b T_1^c] = \rho_2 [M_2^a L_2^b T_2^c]$

$$\rho_2 = \rho_1 \left[\frac{M_1}{M_2} \right]^a \left[\frac{L_1}{L_2} \right]^b \left[\frac{T_1}{T_2} \right]^c$$

Dimensions of Density is $[ML^{-3}T^0]$

$$M_1 = 1g ; M_2 = 100g ; a = 1 ; b = -3$$

$$L_1 = 1\text{ cm} ; L_2 = 10\text{ cm} ; \rho_1 = 4\text{ g cm}^{-3}$$

$$\rho_2 = 4 \left[\frac{1g}{100g} \right]^1 \left[\frac{1\text{ cm}}{10\text{ cm}} \right]^{-3}$$

$$\rho_2 = 4 [10^{-2}] [10^{-1}]^{-3}$$

$$\rho_2 = 4 \times 10^{-2} \times 10^3$$

$$\rho_2 = 4 \times 10$$

$$\rho_2 = 40$$

12. If the force is proportional to square of velocity, then the dimension of proportionality constant is.

Soln: $F \propto v^2$

$$F = k v^2 \Rightarrow k = \frac{F}{v^2}$$

Applying Dimensions,

$$k = \frac{[MLT^{-2}]}{[LT^{-1}]^2} \Rightarrow k = \frac{[MLT^{-2}]}{[L^2 T^{-2}]}$$

$$k = [MLT^{-2}] [L^{-2} T^2] \Rightarrow k = [ML^{-1} T^0]$$

13) The dimension of $[\mu_0 \epsilon_0]^{-1/2}$ is

Soln: Unit of μ_0 is NA^{-2}

Unit of ϵ_0 is $C^2 m^{-2} N^{-1}$

$$[\mu_0 \epsilon_0]^{-1/2} = [NA^{-2} \cdot C^2 m^{-2} N^{-1}]^{-1/2}$$

$$= [C^2 m^{-2} A^{-2}]^{-1/2}$$

$$= [C^2 m^{-2} C^{-2} A^2 s^2]^{-1/2}$$

$$= [m^2 A^2 s^2]^{-1/2}$$

$$= [m s^{-1}]$$

This is unit of velocity.

[OR]

The speed of light is defined as the inverse of the square root of the product of permittivity by permeability:

$$c = \frac{1}{\sqrt{\mu_0 \epsilon_0}} \Rightarrow \text{ANSWER : } \underline{\underline{\text{Velocity}}}$$

14) Planck's constant $[h]$, speed of light in vacuum $[c]$ and Newton's Gravitational constant $[G]$ are taken as three fundamental constants. Which of the following combinations of these has the dimension of length?

$$\frac{\sqrt{hG}}{c^{3/2}} = \frac{[hG]^{1/2}}{[c]^{3/2}}$$

Applying Dimensions,

$$\frac{[hG]^{1/2}}{[c]^{3/2}} = \frac{[ML^2T^{-1}]^{1/2} [M^{-1}L^3T^{-2}]^{1/2}}{[LT^{-1}]^{3/2}} = \frac{[L^5T^{-3}]^{1/2}}{[LT^{-1}]^{3/2}}$$

$$= [L^{5/2} T^{-3/2} L^{-3/2} T^{3/2}]$$

$$= [L^{\frac{5-3}{2}}] \Rightarrow [L]$$

ANSWER : [a] $\frac{\sqrt{hG}}{c^{3/2}}$

15) A length - scale $[L]$ depends on the permittivity $[\epsilon]$ of a dielectric material, Boltzman constant $[k_B]$, the absolute temperature $[T]$, the no. per unit volume $[n]$ of certain charged particles, and the charge $[q]$ carried by each of the particles. Which of the following expression for L is dimensionally correct?

Answer : [b] $L = \sqrt{\frac{\epsilon k_B T}{n q^2}}$

Soln:-

$$\lambda = \left[\frac{\Sigma k_B T}{n q^2} \right]^{1/2}$$

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Let $d^3 N d\vec{m}^2$

$$\text{unit of } \Sigma = C^2 N^{-1} m^{-2}$$

$$\text{unit of } k_B = N m K^{-1}$$

$$\text{unit of } T = K$$

$$\text{unit of } n = m^{-3}$$

$$\text{unit of } q^2 = C^2$$

$$\lambda = \left[\frac{\Sigma k_B T}{n q^2} \right]^{1/2} = \left[\frac{C^2 N^{-1} m^{-2} \cdot N m K^{-1} \cdot K}{m^{-3} \cdot C^2} \right]^{1/2}$$

$$\lambda = \left[\frac{m^{-1}}{m^{-3}} \right]^{1/2}$$

$$\lambda = [m^{-1} \cdot m^3]^{1/2}$$

$$\lambda = [m^2]^{1/2}$$

$$\lambda = [m]$$

The dimension of length, [L]

So Dimensionally correct.

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