

UNIT - 1 - Electrostatics

Exercise Problems.

① $Q = 50 \text{ nC}$
 $= 50 \times 10^{-9} \text{ C}$
 $n = ?$

$Q = ne$
 $n = \frac{Q}{e} = \frac{50 \times 10^{-9}}{1.6 \times 10^{-19}}$
 $n = 31.25 \times 10^{10} \text{ electrons}$

$$\frac{F}{W} = \frac{23.04 \times 10^{23}}{588}$$

$$= 0.03918 \times 10^{23}$$

$$F/W = 3.918 \times 10^{21}$$

② No. of electrons in the human body $= 10^{28}$
 loss of electrons $= 1\%$
 No. of electrons in the human body after 1% loss $= \frac{1}{100} \times 10^{28}$
 $n = 10^{26} \text{ electrons}$

$Q = ne$
 $= 10^{26} \times 1.6 \times 10^{-19}$

$Q = 1.6 \times 10^7$

$F = \frac{1}{4\pi\epsilon_0} \times \frac{q_1 q_2}{r^2}$ $[q_1 = q_2 = 1.6 \times 10^7 \text{ C}]$
 $r = 1 \text{ m}$

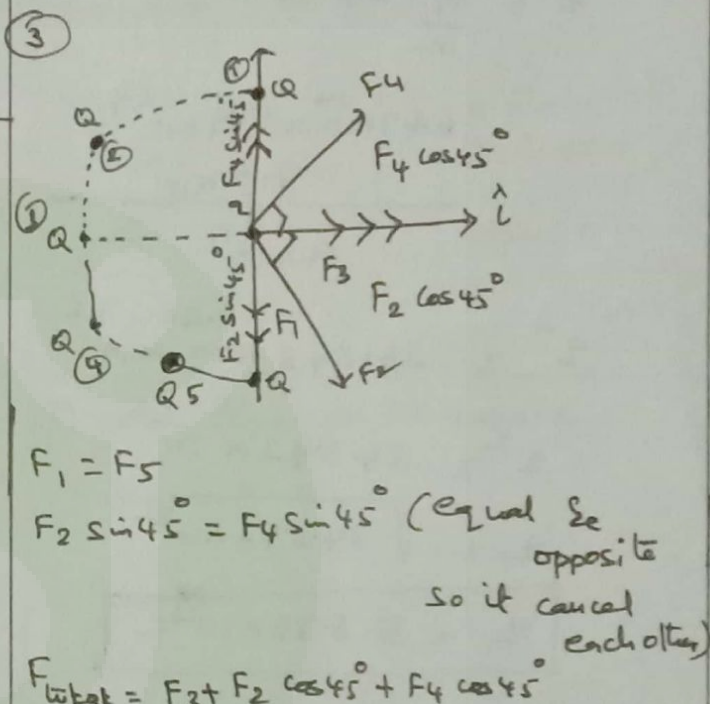
$$= \frac{9 \times 10^9 \times 1.6 \times 10^7 \times 1.6 \times 10^7}{1^2}$$

$$= 9 \times 2.56 \times 10^{23}$$

$F = 23.04 \times 10^{23} \text{ N}$

Mass of the man $= 60 \text{ kg}$
 weight $= 60 \times 9.8 \text{ [W=mg]}$

$W = 588 \text{ N}$



$F_{\text{net}} = F_3 + F_2 \cos 45^\circ + F_4 \cos 45^\circ$

$$= \frac{kqQ}{R^2} + \frac{kqQ}{R^2} \frac{1}{\sqrt{2}} + \frac{kqQ}{R^2} \frac{1}{\sqrt{2}}$$

$$= \frac{kqQ}{R^2} + \frac{2kqQ}{\sqrt{2}R^2}$$

$$= \frac{kqQ}{R^2} + \frac{\sqrt{2}kqQ}{R^2}$$

$$\vec{F}_{\text{total}} = \frac{kQ^2}{R^2} [1 + \sqrt{2}] \text{ N } \hat{i}$$

$\hat{i} \rightarrow \text{Force acting along x axis}$

4) For balance the gravitational force of attraction between Earth and moon.

a) $F_e = F_g$

$$\frac{K q^2}{r^2} = \frac{G M_E M_M}{r^2}$$

$$q^2 = \frac{G M_E M_M}{K}$$

$$= \frac{6.67 \times 10^{-11} \times 5.9 \times 10^{24} \times 7.9 \times 10^{22}}{9 \times 10^9}$$

$$q^2 = 34.543 \times 10^{-20} \times 10^{46}$$

$$q^2 = 34.543 \times 10^{26}$$

$$q = \sqrt{34.543 \times 10^{26}}$$

$$q = 5.877 \times 10^{13} \text{ C}$$

b) $r = r/2$

$$\frac{K q(1/2)}{(r/2)^2} = \frac{G M_E M_M}{(r/2)^2}$$

$$K(q^2) = G M_E M_M$$

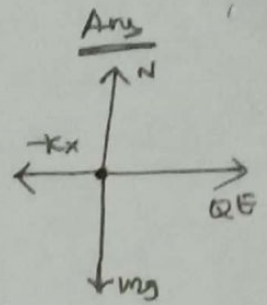
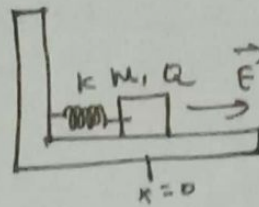
$$q^2 = \frac{G M_E M_M}{K}$$

$$q = 5.877 \times 10^{13} \text{ C}$$

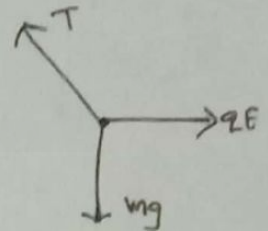
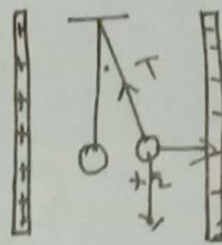
If the distance between the Earth and Moon is halved the charge will remain same

5)

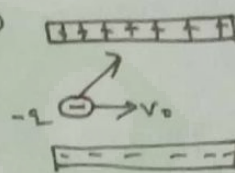
a)



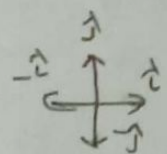
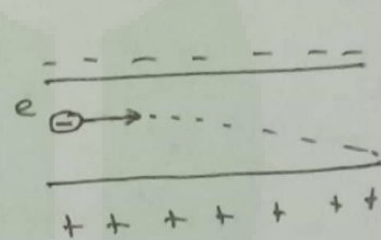
b)



c)



6)



$$F = ma$$

$$F = eE$$

$$eE = ma$$

$$a = \frac{eE}{m}$$

$$\vec{a} = \frac{eE}{m} (-\hat{j}) = -\frac{eE}{m} \hat{j}$$

$$\vec{v} = \vec{u} + \vec{a}t$$

$$\vec{v} = v_0 \hat{i} - \frac{eE}{m} t (\hat{j})$$

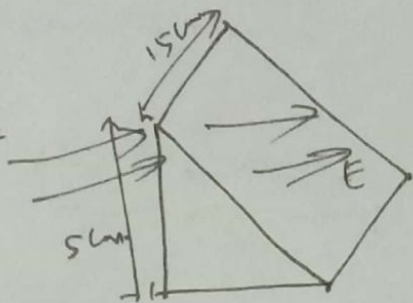
$$s = ut + \frac{1}{2} at^2$$

$$\vec{r} = \vec{u}t + \frac{1}{2} \vec{a}t^2$$

$$\vec{r} = v_0 \hat{i} t - \frac{1}{2} \frac{eE}{m} t^2 \hat{j}$$



$$E = 2 \times 10^3 \text{ N/C}$$



$$\begin{aligned} \int ds &= s = 2 \times 5 \\ &= 15 \times 10^{-2} \times 5 \times 10^{-4} \\ \int ds &= s = 75 \times 10^{-4} \text{ m}^2 \end{aligned}$$

a) vertical rectangular surface

Here $\theta = 0^\circ$

$$\phi = \oint E ds \cos \theta$$

$$= \oint E ds$$

$$= E \oint ds$$

$$= 2 \times 10^3 \times 75 \times 10^{-4}$$

$$\boxed{\phi = 15 \text{ Nm}^2 \text{C}^{-1}}$$

b) slanted surface

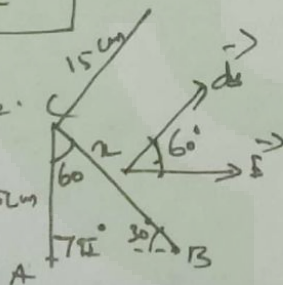
$$\theta = 60^\circ$$

$$\phi = \oint E ds \cos \theta$$

$$= 2 \times 10^3 \times 150 \times 10^{-4} \times \frac{1}{2}$$

$$= 150 \times 10^{-1}$$

$$\boxed{\phi = 15 \text{ Nm}^2 \text{C}^{-1}}$$



$$\begin{aligned} \Delta ABC \\ \sin 30^\circ &= \frac{5 \times 10^{-2}}{x} \end{aligned}$$

$$\begin{aligned} x &= \frac{5 \times 10^{-2}}{\sin 30^\circ} \\ &= \frac{5 \times 10^{-2}}{1/2} \end{aligned}$$

$$\boxed{x = 10 \times 10^{-2} \text{ m}}$$

$$\begin{aligned} \int ds &= s = 2 \times x \\ &= 10 \times 10^{-2} \times 15 \times 10^{-2} \\ &= 150 \times 10^{-4} \end{aligned}$$

c) entire surface:

$\phi = 0$ (closed surface net charge is zero)

in vertical field lines are entering into the surface; in slanted surface same amount of field lines are going outward from the surface.

$$\text{Net flux} = -15 + 15$$

$$\boxed{\phi = 0}$$

entering into the surface = -15
getting out from the surface = +15

8) refer figure in the question.

i) region A

$$E = -\frac{dv}{dx}$$

$$= -\frac{(8-5)}{(0.2-0)} = -\frac{3}{0.2}$$

$$\boxed{E = -(-15) = 15 \text{ Vm}^{-1}}$$

ii) region B

There is no change in the potential with respect to x

$$\text{so } dv = 0$$

$$\boxed{E = 0}$$

iii) region C

$$E = -\frac{dv}{dx}$$

$$= -\frac{(7-5)}{(0.6-0.4)} = -\frac{2}{0.2}$$

$$\boxed{E = -10 \text{ Vm}^{-1}}$$

iv) region D:

$$E = -\frac{dv}{dr}$$

$$= -\frac{(7-1)}{(0.8-0.6)}$$

$$= -\frac{6}{0.2} = -30$$

$$E = -(-30) = 30 \text{ Vm}^{-1}$$

⑨ $d = 0.6 \text{ mm} = 0.6 \times 10^{-3} \text{ m}$

$$E = 3 \times 10^6 \text{ Vm}^{-1}$$

a) $V = E \times d$

$$= 3 \times 10^6 \times 0.6 \times 10^{-3}$$

$$= 3 \times 6 \times 10^6 \times 10^{-4}$$

$$V = 18 \times 10^2 = 1800 \text{ V}$$

b) If the gap between the electrodes is increased, (at constant electric field $\Rightarrow E$) the potential also increases

$$V \propto d \quad (E \text{ is constant})$$

~~7/10/11/12/13/14/15/16/17/18/19/20/21/22/23/24/25/26/27/28/29/30/31/32/33/34/35/36/37/38/39/40/41/42/43/44/45/46/47/48/49/50/51/52/53/54/55/56/57/58/59/60/61/62/63/64/65/66/67/68/69/70/71/72/73/74/75/76/77/78/79/80/81/82/83/84/85/86/87/88/89/90/91/92/93/94/95/96/97/98/99/100~~

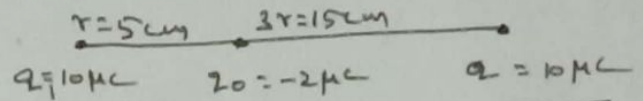
c) $d = 1 \text{ mm} = 1 \times 10^{-3} \text{ m}$

$$V = Ed = 3 \times 10^6 \times 1 \times 10^{-3}$$

$$= 3 \times 10^3$$

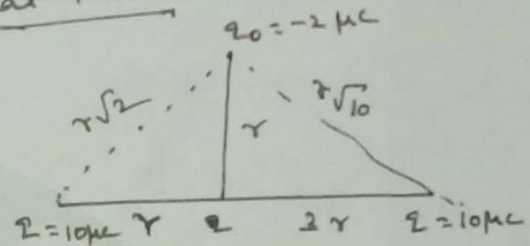
$$V = 3000 \text{ V}$$

⑩ Initial Position:



$$U_i = -\frac{Kq_1q_2}{r} - \frac{Kq_2q_3}{3r} + \frac{Kq_1q_3}{4r}$$

Final Position:



$$U_f = -\frac{Kq_1q_2}{r\sqrt{2}} - \frac{Kq_2q_3}{r\sqrt{10}} + \frac{Kq_1q_3}{4r}$$

$$W = U_f - U_i = -\frac{Kq_1q_2}{r\sqrt{2}} - \frac{Kq_2q_3}{r\sqrt{10}} + \frac{Kq_1q_3}{4r}$$

$$+ \frac{Kq_1q_2}{r} + \frac{Kq_2q_3}{3r} - \frac{Kq_1q_3}{4r}$$

$$= \frac{Kq_1q_2}{r} \left[-\frac{1}{\sqrt{2}} - \frac{1}{\sqrt{10}} + \frac{1}{3} + \frac{1}{1} \right]$$

$$= \frac{Kq_1q_2}{r} \left[\frac{4}{3} - \left(\frac{\sqrt{2} + \sqrt{10}}{\sqrt{20}} \right) \right]$$

$$= \frac{9 \times 10^9 \times 2 \times 10^{-6} \times 10^{-6}}{5 \times 10^{-2}} \left[\frac{4}{3} - \frac{4.576}{4.472} \right]$$

$$= \frac{9 \times 10^4 \times 10^{-3}}{5 \times 10^{-2}} [1.233 - 1.023]$$

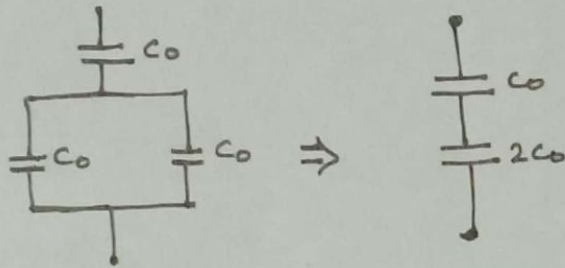
$$= 36 \times 10^{-1} [0.31]$$

$$= 3.6 \times 0.31$$

$$W = 1.116 \text{ J}$$

To separate the negative charge from positive charge work is done on the system

11) a)



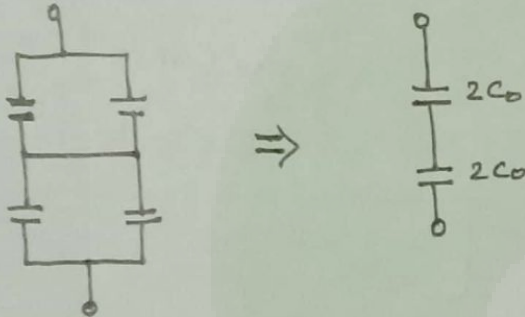
$$C_p = C_0 + C_0 = 2C_0$$

$$\frac{1}{C_s} = \frac{1}{C_0} + \frac{1}{2C_0} = \frac{2C_0 + C_0}{2C_0^2}$$

$$\frac{1}{C_s} = \frac{3C_0}{2C_0^2}$$

$$C_s = \frac{2C_0^2}{3C_0} = \frac{2}{3}C_0$$

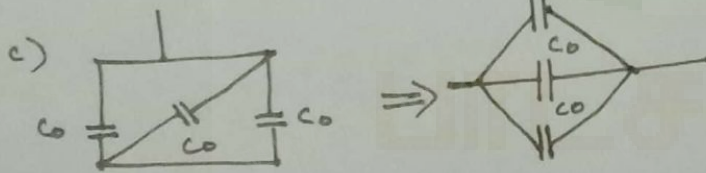
b)



$$C_p = C_0 + C_0 = 2C_0$$

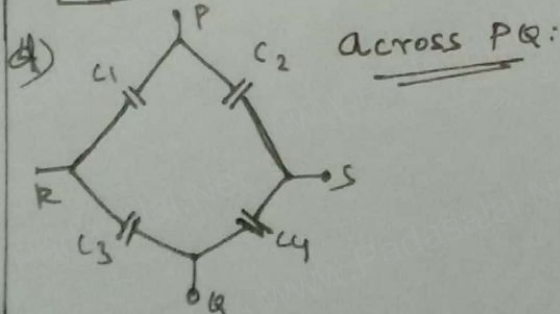
$$\frac{1}{C_s} = \frac{1}{2C_0} + \frac{1}{2C_0} = \frac{4C_0}{4C_0^2} = \frac{1}{C_0}$$

$$C_s = C_0$$



$$C_p = C_1 + C_2 + C_3 = C_0 + C_0 + C_0$$

$$C_p = 3C_0$$



C_1 and C_2 are in series

$$\frac{1}{C_{s1}} = \frac{1}{C_1} + \frac{1}{C_2}$$

$$C_{s1} = \frac{C_1 C_2}{C_1 + C_2}$$

C_3 and C_4 are in series

$$\frac{1}{C_{s2}} = \frac{1}{C_3} + \frac{1}{C_4}$$

$$C_{s2} = \frac{C_3 C_4}{C_3 + C_4}$$

C_{s1} and C_{s2} are in parallel

$$C_p = C_{s1} + C_{s2}$$

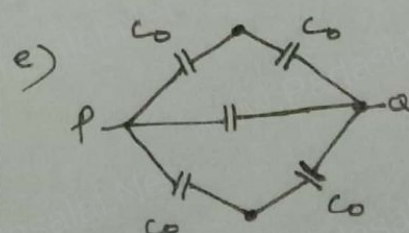
$$= \frac{C_1 C_2}{C_1 + C_2} + \frac{C_3 C_4}{C_3 + C_4}$$

$$= \frac{C_1 C_2 (C_3 + C_4) + C_3 C_4 (C_1 + C_2)}{(C_1 + C_2)(C_3 + C_4)}$$

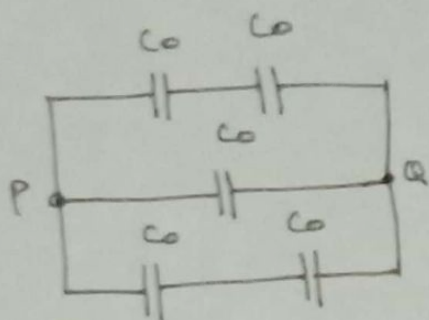
$$C_p = \frac{C_1 C_2 C_3 + C_1 C_2 C_4 + C_1 C_3 C_4 + C_2 C_3 C_4}{(C_1 + C_2)(C_3 + C_4)}$$

if we find across RS

also same as across PQ.

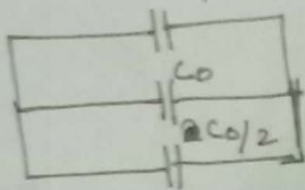


Equivalent circuit



$$\frac{1}{C_{S1}} = \frac{1}{C_0} + \frac{1}{C_0} = \frac{2}{C_0} \Rightarrow$$

$$\frac{1}{C_{S2}} = \frac{1}{C_0} + \frac{1}{C_0} = \frac{2}{C_0}$$



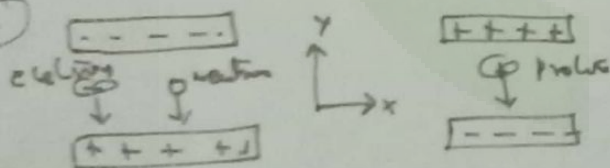
$$C_p = C_{S1} + C_{S2} + C_0$$

$$= \frac{C_0}{2} + \frac{C_0}{2} + C_0$$

$$= \frac{2C_0}{2} + C_0$$

$$C_p = 2C_0$$

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$$V = 5V;$$

$$m_e = 9.1 \times 10^{-31} \text{ kg}$$

$$m_p = 1.6 \times 10^{-27} \text{ kg}$$

$$g = 10 \text{ m/s}^2$$

$$s = h = d = 1 \times 10^{-3} \text{ m.}$$

a) Time of flight for electron and proton

for electron:

$$s = ut + \frac{1}{2} at^2 \quad u = 0$$

$$s = \frac{1}{2} at^2$$

$$t^2 = \frac{2s}{a}$$

$$a = F/m = \frac{Ee}{m} = \frac{Ve}{dm} \quad \left[\because E = \frac{V}{d} \right]$$

$$t_e = \sqrt{\frac{2s}{a}} = \sqrt{\frac{2 \cdot s \cdot d \cdot m_e}{V \cdot e}}$$

$$= \sqrt{\frac{2 \times 10^{-3} \times 10^{-3} \times 9.1 \times 10^{-31}}{5 \times 1.6 \times 10^{-19}}}$$

$$= \sqrt{\frac{18.2 \times 10^{-27}}{8 \times 10^{-19}}}$$

$$= \sqrt{2.275 \times 10^{-27+19}}$$

$$= \sqrt{2.275 \times 10^{-8}}$$

$$= 1.5 \times 10^{-9} \text{ s}$$

$$t_e = 1.5 \text{ ns}$$

Proton

$$t_p = \sqrt{\frac{2 \cdot s \cdot d \cdot m_p}{V \cdot e}}$$

$$= \sqrt{\frac{2 \times 10^{-3} \times 10^{-3} \times 1.67 \times 10^{-27}}{5 \times 1.6 \times 10^{-19}}}$$

$$= \sqrt{\frac{3.34 \times 10^{-13}}{8 \times 10^{-19}}}$$

$$= \sqrt{0.4175 \times 10^{-14}}$$

$$= \sqrt{4.175 \times 10^{-15}}$$

$$= 0.646 \times 10^{-7}$$

$$= 64.6 \times 10^{-9} \text{ s}$$

$$t_p = 64 \text{ ns}$$

b) Neutron has no charge.
So it does not experience any electrostatic force, so it will experience only gravitational pull.

$$s = ut + \frac{1}{2}at^2 \quad u=0$$

$$s = \frac{1}{2}gt^2$$

$$t^2 = \frac{2s}{g}$$

$$t = \sqrt{\frac{2s}{g}} = \sqrt{\frac{2 \times 10^{-3}}{10}}$$

$$= \sqrt{0.2 \times 10^{-3}}$$

$$= \sqrt{2 \times 10^{-4}}$$

$$t_m = 1.414 \times 10^{-2} \text{ s}$$

d) $t_e = 1.5 \text{ ns}$

$t_p = 6.4 \text{ ns}$

$t_m = 1.414 \times 10^{-2} \text{ s}$

$$t_m = 14.14 \text{ ms}$$

So the time of flight for electron is very less. So the electron will reach the bottom quickly when comparing with other two (proton & neutron)

(13) $E = 3 \times 10^6 \text{ Vm}^{-1}$; $d = 1000 \text{ m}$.

a) $E = V/d \Rightarrow E = V/d$

$V = E \cdot d$

$$= 3 \times 10^6 \times 1000$$

$$V = 3 \times 10^9 \text{ V}$$

b) $Q = 25 \text{ C}$

$U = ?$

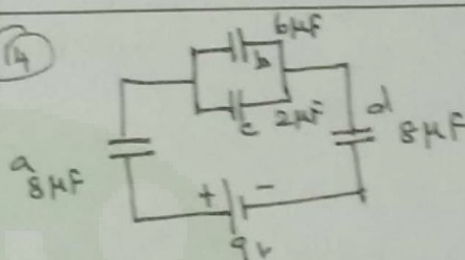
The work done is stored as electrostatic potential energy

$$W = U = V \cdot Q$$

$$= 3 \times 10^9 \times 25$$

$$U = 75 \times 10^9 \text{ J}$$

(14)



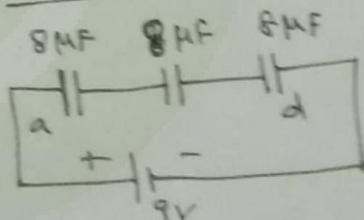
b & c capacitors are in parallel combination so,

$$C_p = C_b + C_c$$

$$= 6 + 2$$

$$C_p = 8 \mu\text{F}$$

Simplified diagram



In above diagram the capacitors are in series

$$\frac{1}{C_s} = \frac{1}{8} + \frac{1}{8} + \frac{1}{8} = \frac{3}{8}$$

$$C_s = \frac{8}{3} \mu\text{F}$$

a) Charges on each capacitor

Total charge on the capacitor on C_s

$$Q = C_s V$$

$$= \frac{8}{3} \times 10^{-6} \times 9$$

$$Q = 24 \mu\text{C}$$

In Series combination the charge on each capacitor is same.

$$\text{So : } q_a = 24 \mu\text{C}$$

$$q_d = 24 \mu\text{C}$$

$$q_{b \& c} = 24 \mu\text{C}$$

In given diagram.

q_b and q_c are different.

(because b & c capacitor are not in series, it is in parallel combination: so the charges across b & c are different)

charge on b

[to find charge on b & c the voltage across a, b & c, d are 3 volt ($\because qv = 3+3+3$)]

$$q_b = C_b \times V_b$$

$$= 6 \times 10^{-6} \times 3$$

$$q_b = 18 \mu\text{C}$$

charge on c.

$$q_c = C_c \times V_c$$

$$= 2 \times 10^{-6} \times 3$$

$$= 6 \times 10^{-6}$$

$$q_c = 6 \mu\text{C}$$

b) Potential difference across them

$$V_a = \frac{q_a}{C_a} = \frac{24 \times 10^{-6}}{8 \times 10^{-6}} = 3\text{V}$$

$$V_b = \frac{q_b}{C_b} = \frac{18 \times 10^{-6}}{6 \times 10^{-6}} = 3\text{V}$$

$$V_c = \frac{q_c}{C_c} = \frac{6 \times 10^{-6}}{2 \times 10^{-6}} = 3\text{V}$$

$$V_d = \frac{q_d}{C_d} = \frac{24 \times 10^{-6}}{8 \times 10^{-6}} = 3\text{V}$$

c) Energy stored in each capacitor across

$$U_a = \frac{1}{2} C_a V_a^2$$

$$= \frac{1}{2} \times 8 \times 10^{-6} \times (3)^2$$

$$U_a = 36 \times 10^{-6} \text{ J}$$

across (b)

$$U_b = \frac{1}{2} C_b V_b^2$$

$$= \frac{1}{2} \times 6 \times 10^{-6} \times (3)^2$$

$$U_b = 27 \times 10^{-6} \text{ J}$$

across (c)

$$U_c = \frac{1}{2} C_c V_c^2$$

$$= \frac{1}{2} \times 2 \times 10^{-6} \times (3)^2$$

$$U_c = 9 \times 10^{-6} \text{ J}$$

across (d)

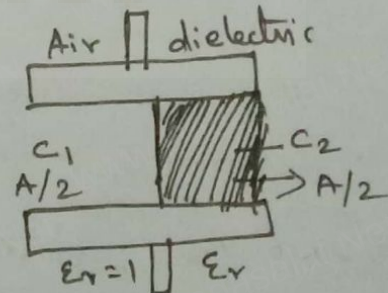
$$U_d = \frac{1}{2} C_d V_d^2$$

$$= \frac{1}{2} \times 8 \times 10^{-6} \times (3)^2$$

$$U_d = 36 \times 10^{-6} \text{ J}$$

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i)



$\epsilon_r = 1$ for air medium

In the above diagram C_1 and C_2 are in parallel combination.

$$C_1 = \frac{\epsilon_0 A}{d/2}$$

$$C_1 = \frac{\epsilon_0 A}{2d}$$

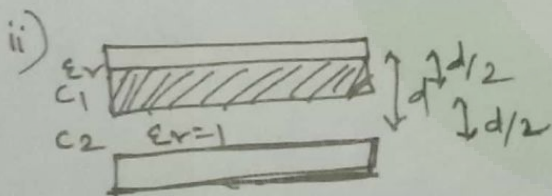
$$C_2 = \frac{\epsilon_0 \epsilon_r A}{d}$$

$$C_2 = \frac{\epsilon_0 \epsilon_r A}{2d}$$

$$C_p = C_1 + C_2$$

$$= \frac{\epsilon_0 A}{2d} + \frac{\epsilon_0 \epsilon_r A}{2d}$$

$$C_p = \frac{\epsilon_0 A}{2d} [1 + \epsilon_r]$$



$$C_1 = \frac{\epsilon_0 \epsilon_r A}{d/2} \quad [\text{in medium}]$$

$$C_1 = \frac{2\epsilon_0 \epsilon_r A}{d}$$

$$C_2 = \frac{\epsilon_0 A}{d/2} \quad [\text{in Air}]$$

$$C_2 = \frac{2\epsilon_0 A}{d}$$

C_1 and C_2 are in series combination.

$$\frac{1}{C_s} = \frac{1}{C_1} + \frac{1}{C_2}$$

$$= \frac{1}{\frac{2\epsilon_0 \epsilon_r A}{d}} + \frac{1}{\frac{2\epsilon_0 A}{d}}$$

$$= \frac{d}{2\epsilon_0 \epsilon_r A} + \frac{d}{2\epsilon_0 A}$$

$$\frac{1}{C_s} = \frac{d}{2\epsilon_0 A} \left[\frac{1}{\epsilon_r} + 1 \right]$$

$$\frac{1}{C_s} = \frac{d}{2\epsilon_0 A} \left[\frac{\epsilon_r + 1}{\epsilon_r} \right]$$

$$C_s = \frac{2\epsilon_0 A}{d} \left[\frac{\epsilon_r}{\epsilon_r + 1} \right]$$